

JUNE 2024 PAPER 1 O' LEVEL MATHEMATICS
Suggested Answers (from MathScience Explained)

1 a) 3

b) 2,67 or $2\frac{2}{3}$

c) $1\frac{1}{5}$ or 1,2

2 a) $1\frac{1}{3}$ or 1,33

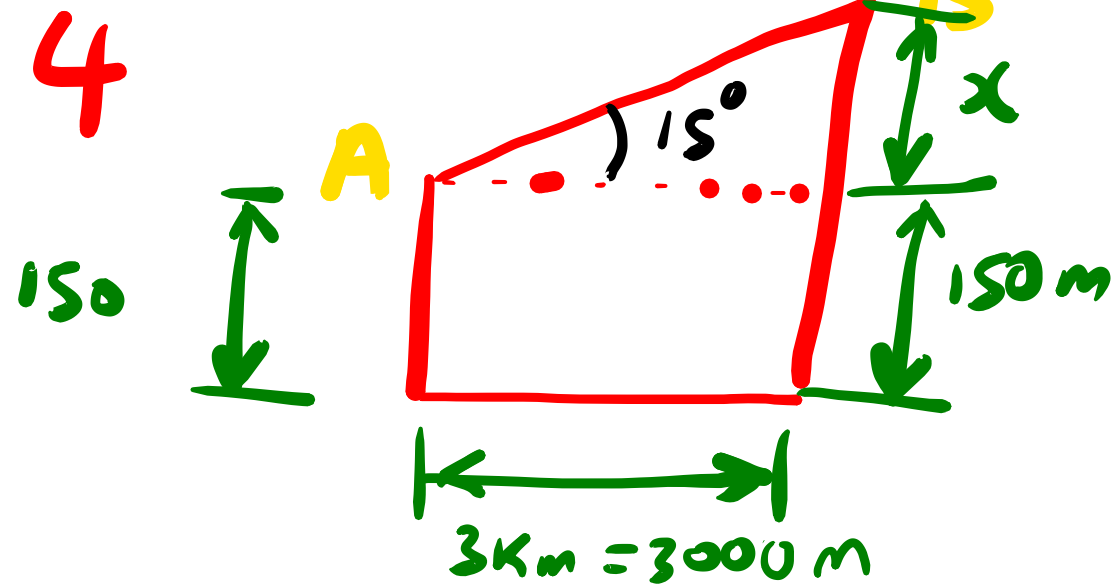
b) 11

c) 0,08

3 a) 2:3:5

b) $\frac{5}{10} \times 150$

75 sweets



$$\tan 15 = \frac{x}{3000}$$

$$\begin{aligned}
 x &= 3000 \times \tan 15 \\
 &= 3000 \times 0,0875 \\
 &= \underline{\underline{262,5}}
 \end{aligned}$$

$$\begin{aligned}
 \therefore \text{the height} &= 262,5 + 150 \\
 &= \underline{\underline{412,5 \text{ m}}}
 \end{aligned}$$

S. a) $\hat{PQR} = 30^\circ$

$$\begin{aligned}
 \text{b) } 30 + 300 + x + x &= 360 \\
 2x &= 30 \\
 x &= \underline{\underline{15}}
 \end{aligned}$$

Alternatively

$$\frac{60}{2} = 30$$

$$\frac{30}{2} = 15$$

$$\therefore x = \underline{\underline{15^\circ}}$$

$$6x = 3 - 3y \quad \dots (1)$$

$$2y = x - 8 \quad \dots (2)$$

$$2y = 3 - 3y - 8$$

$$\frac{5y}{5} = \frac{-5}{5}$$

$$y = \underline{-1}$$

$$x = 3 - 3(-1)$$

$$= 3 + 3$$

$$= \underline{6}$$

$$\underline{x = 6 \text{ and } y = -1}$$

7 Area of wall

$$6 \times 5 = 30 \text{ m}^2$$

Area of window =

$$\begin{array}{r} 1, 5 \\ \times 1, 2 \\ \hline 1, 50 \\ 30 \\ \hline 1, 80 \end{array}$$

$$\therefore 30 - 1, 8$$

$$= \underline{28, 2 \text{ m}^2}$$

8 a) (i) $\{1; 8\}$

(ii) $\{1; 8\}$

b) $\underline{B \subset A}$ or $\underline{A \supset B}$

9 a) $7, 32 \times 10^1$

b) $400 - 188 = 212$

$$\underline{2, 12 \times 10^2}$$

Alternatively

$$10^2(4 - 1,88)$$

$$10^2(2,12)$$

$$2,12 \times 10^2$$

10 a) (i) \$10 000

(ii) 3cm

$$\begin{array}{r|l} 2 & 432 \\ \hline 2 & 216 \\ 2 & 108 \\ 2 & 54 \\ 3 & 27 \\ 3 & 9 \\ 3 & 3 \end{array}$$

$$\therefore \underline{\underline{2^4 \times 3^3}}$$

$$\text{(ii)} \quad \underline{\underline{3}}$$

$$\text{II (a)} \quad 15 \times 80 = 1200$$

profit = SP - BP

$$\therefore \text{profit} = 1200 - 640$$

$$= \underline{\underline{\$560}}$$

$$b) \quad I = \frac{PRT}{100}$$

$$240 = \frac{4000 \times 3 \times T}{100}$$

$$\frac{120T}{120} = \frac{240}{120}$$

$$T = \underline{\underline{2 \text{ years}}}$$

$$12 a) \quad 5 - 45 \text{ am}$$

$$b(i) \quad \begin{array}{r} 0725 \\ - 0715 \\ \hline 10 \end{array}$$

$$\therefore \underline{\underline{10 \text{ minutes}}}$$

$$(ii) \quad \begin{array}{r} 660 \\ 0725 \\ - 0545 \\ \hline 1 \text{ hr } 40 \text{ min} \end{array}$$

$$\underline{\underline{1 \frac{2}{3} \text{ hr}}}$$

$$\text{Average speed} = \frac{\text{total distance}}{\text{total time}}$$

$$= 5 \div \frac{5}{3}$$

$$= \underline{\underline{3 \text{ km/hr}}}$$

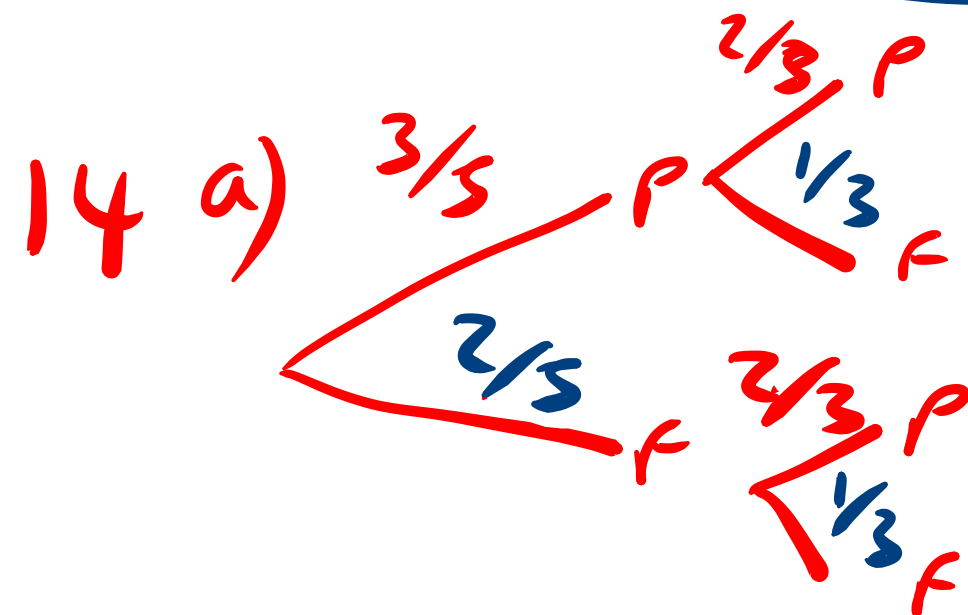
$$13 \text{ a) } S \hat{Q} T = \underline{\underline{30^\circ}}$$

$$\text{b) } T \hat{Q} P = \underline{\underline{50^\circ}}$$

$$\begin{aligned} \text{c) } S \hat{Q} P &= 180 - (30 + 50) \\ &= \underline{\underline{100}} \end{aligned}$$

$$P \hat{S} Q = S \hat{P} Q = \frac{100}{2} = \underline{\underline{50^\circ}}$$

$$\therefore P \hat{T} Q = \underline{\underline{80^\circ}}$$



$$\begin{aligned} \text{b) } & P(\text{pass; fail}) + P(\text{fail; pass}) \\ & \left(\frac{3}{5} \times \frac{1}{3} \right) + \left(\frac{2}{5} \times \frac{2}{3} \right) \\ & = \underline{\underline{\frac{7}{15}}} \end{aligned}$$

$$15 \text{ a) (i) } \underline{\underline{2(2x-y)}}$$

$$\text{(ii) } \underline{\underline{(2x-y)(2x+y)}}$$

$$\text{b) } \underline{\underline{2(2x-y)(2x+y)}}$$

16 a) direct variation

$$\text{b) } D = kL$$

$$7,5 = k \times 0,5$$

$$k = 15$$

$$\therefore \underline{\underline{D = 15L}}$$

$$\text{c) } \frac{480}{15} = \frac{15L}{15}$$

$$\underline{\underline{L = 32 \text{ litres}}}$$

$$17 \text{ a) } 360 - 240$$

$$\frac{120}{180 - 120} = 60$$

$$\therefore \text{N } 60^\circ \text{E}$$

Alternatively

$$240 - 180$$

60

$\therefore N 60^\circ E$

$$b) \quad 5x^2 = 5^2 + 8^2 - 2 \times 5 \times 8 \cos 120$$

$$= 25 + 64 - 80 \cos 120$$

$$= \sqrt{89 - 80 \cos 120}$$

$$= \sqrt{89 - 80(-0,5)}$$

$$= \sqrt{129}$$

$$18 \quad a) \quad 6 - 3y = 9$$

$$\frac{3y}{3} = \frac{-3}{3}$$

$$y = -1$$

$$b) \quad \begin{pmatrix} 2x+1 & 2x-3 \\ 3x+1 & 3x-3 \end{pmatrix}$$

$$\begin{pmatrix} 2 & -6 \\ 3 & -9 \end{pmatrix}$$

$$c) \begin{pmatrix} 1 & -x \\ -2 & 9 \end{pmatrix} \begin{pmatrix} 9 & x \\ 2 & 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

$$9 - 2x = 1$$

$$\underline{x = 4}$$

$$19 \text{ (a) } 7$$

b)

$$\begin{array}{r} 1'016_9 \\ + 881_9 \\ \hline \underline{2007_9} \end{array}$$

$$c) \begin{array}{r} 140_5 \\ - 1^3 23_5 \\ \hline \end{array}$$

$$\underline{12_5}$$

$$1 \times 5^1 + 2 \times 5^0 = 5 + 2$$

$$\begin{array}{r|l} 2 & 7 \\ \hline 2 & 3r1 \\ 2 & 1r1 \\ & 0r1 \end{array} \uparrow$$

$$\underline{\underline{1112}}$$

$$\begin{array}{r} 20 \text{ a)} \quad 9 \ 30 \\ + \quad 4 \ . \ 00 \\ \hline 13 \ 30 \end{array}$$

13 30 or 1:30 pm

$$\text{b)} \quad 6 + 6 = \underline{\underline{12 \text{ km}}}$$

$$\text{c)} \quad \text{Ave Speed} = \frac{12}{4} \\ = \underline{\underline{3 \text{ km/hr}}}$$

d) 1 hour

$$\text{21 a) (i)} \quad 8 + 4 = \underline{\underline{12}}$$

$$\text{(ii)} \quad \underline{\underline{-1}}$$

$$\text{(iii)} \quad \underline{\underline{\frac{1}{4}}}$$

$$\text{b)} \quad 3^x + 2x = 3^3$$

$$3x = 3$$

$$\underline{\underline{x = 1}}$$

$$22 \text{ a) } \underline{\underline{\triangle DCB}}$$

$$\text{b) } \triangle ACE \parallel \triangle DCB$$

$$\frac{AC}{DC} = \frac{AE}{DB} = \frac{CE}{CB}$$

$$\frac{x+3}{4} = \frac{6}{3}$$

$$\frac{x+3}{4} = 2$$

$$\underline{\underline{x = 5}}$$

$$\text{c) } \left(\frac{1}{2}\right)^2 = \frac{1}{4}$$

$$\begin{aligned} \text{Area } \triangle DCE &= \frac{1}{4} \times 24 \\ &= 6 \text{ cm}^2 \end{aligned}$$

$$\therefore \text{Area of } \triangle ADE$$

$$\Rightarrow 24 - 6$$

$$\underline{\underline{18 \text{ cm}^2}}$$

$$23a) \underline{9x + 2y = 360} \quad \dots (1)$$

$$9(180-x) = 2(180-y) + 1152$$

$$1620 - 9x = 360 - 2y + 1152$$

$$\underline{9x - 2y = 108} \quad \dots (2)$$

b)

$$9x + 2y = 360$$

$$9x - 2y = 108$$

$$4y = 252$$

$$y = 63^\circ$$

$$\begin{array}{r} 9x + 2y = 360 \\ + \quad + \\ 9x - 2y = 108 \\ \hline 18x = \underline{468} \\ \hline 18 \end{array}$$

$$x = 26$$

$$\underline{\underline{x = 26}} \quad \text{and} \quad \underline{\underline{y = 63}}$$

$$\begin{array}{l} 24 \quad a) \quad (i) \quad y = mx + c \\ \quad \quad \quad \quad \quad \quad -3 = 3(2) + c \\ \quad \quad \quad \quad \quad \quad c = -9 \\ \therefore \underline{\underline{y = 3x - 9}} \end{array}$$

(ii) parallel

$$b) \quad 2(2) + k^2 = 29$$

$$\sqrt{k^2} = \sqrt{25}$$

$$\underline{\underline{k = \pm 5}}$$