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Lecture Note on
Digital Electronics

Diploma 3rd Semester
BRANCH-ECE

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CONTENTS

Unit-1:BasicsofDigitalElectronics

A Digital system is an interconnection of digital modules and it is a system that manipulates discrete elements of information that is represented internally in the binary form. Now a day's digital systems are used in wide variety of industrial and consumer products such as automated industrial machinery, pocket calculators, microprocessors, digital computers, digital watches, TV games and signal processing and so on.

Number System-Binary, Octal, Decimal, Hexadecimal - Conversion from one system to another number system.

Number:
The way of quantifying anything , represented through various combination of symbolsis called number.

Digit:
Thevarioussymbolsrepresentingasinglenumberinanynumbersystemiscalleddigit. E.g.Decimalnumbersystem(Arabicnumerals):Digits:0,1,2,3,4,5,6,7,8,9.

Radix/Base(r):
Themaximumnumberofdifferentdigitsofanynumbersystem.E.gDecimalNS,r=10

Numbersystem:
The properly structured number formation is called Number system. In number system there are different symbols and each symbol has an absolute value and also has place value.

In general a number in a system having base or radix ' r ' can be written as

Number various combination digits according to position

Nr=[Integerpart.Fractionalpart]

↑Radixpoint

= $d_n d_{n-1}...d_1 d_0 . d_{-1}d_{-2}...d_-$

$_m$The value,

$N_{10} = d_n x r^n + d_{n-1} x r^{n-1} + ... + d_1 x r^1 + d_0 x r^0 + d_{-1} x r^{-1} + d_{-2} x r^{-2} + ... + d_{-m} x r^{-m}$

* TherightmostdigitofanynumberiscalledLeastSignificantDigit

* ThelefmostdigitofanynumberiscalledMostSignificantDigit

TYPESOFNUMBERSYSTEM:-

Therearefourtypesofnumbersystems.Theyare

1. Decimalnumbersystem

2. Binarynumbersystem

3. Octalnumbersystem

4. Hexadecimalnumbersystem

DECIMALNUMBERSYSTEM:-•

Thedecimalnumbersystemcontaintenuniquesymbols0,1,2,3,4,5,6,7,8and9.

• Indecimalsystem10symbolsareinvolved,sothebaseorradixis10.

• Itisapositionalweightedsystem.

$$(d_n \times 10^n) + (d_{n-1} \times 10^{n-1}) + (d_{n-2} \times 10^{n-2}) + \ldots + (d_0 \times 10^0) + (d_{-1} \times 10^{-1}) + (d_{-2} \times 10^{-2}) + \ldots + (d_{-m} \times 10^{-m})$$

For example:-

$$9256.26 = 9 \times 1000 + 2 \times 100 + 5 \times 10 + 6 \times 1 + 2 \times (1/10) + 6 \times (1/100)$$
$$= 9 \times 10^3 + 2 \times 10^2 + 5 \times 10^1 + 6 \times 10^0 + 2 \times 10^{-1} + 6 \times 10^{-2}$$

BINARYNUMBERSYSTEM:-

• Thebinarynumbersystemisapositionalweightedsystem.

• Thebaseorradixofthisnumbersystemis2.

• Ithastwoindependentsymbols,Thesymbolsusedare0and1.

• Abinarydigitiscalledabit

$$(d_n \times 2^n) + (d_{n-1} \times 2^{n-1}) + (d_{n-2} \times 2^{n-2}) + \ldots + (d_0 \times 2^0) + (d_{-1} \times 2^{-1}) + (d_{-2} \times 2^{-2}) + \ldots + (d_{-k} \times 2^{-k})$$

OCTALNUMBERSYSTEM:-

• Itisalsoapositionalweightedsystem.

• Itsbaseorradixis8.

• Ithas8independentsymbols0,1,2,3,4,5,6and7.

• Itsbase8=2^3,every3-bitgroupofbinarycanberepresentedbyanoctaldigit.

HEXADECIMALNUMBERSYSTEM:-

• Thehexadecimalnumbersystemisapositionalweightedsystem.

• Thebaseorradixofthisnumbersystemis16.

• Thesymbolsusedare0,1,2,3,4,5,6,7,8,9,A,B,C,D,EandF

• The base 16 = 24 , every 4 – bit group of binary can be represented by an hexadecimal digit.

CONVERSIONFROMONENUMBERSYSTEMTOANOTHER:-

1. BINARYNUMBERSYSTEM:-

(a) Binary to decimal conversion:- In this method, each binary digit of the number is multiplied by its positional weight and the product terms are added to obtain decimal number.

$$(111.101)_2 = (1 \times 2^2) + (1 \times 2^1) + (1 \times 2^0) + (1 \times 2^{-1}) + (0 \times 2^{-2}) + (1 \times 2^{-3})$$
$$= 4 + 2 + 1 + 0.5 + 0 + 0.125$$
$$= (7.625)_{10}$$

(b) Binary to Octal conversion:- For conversion binary to octal the binary numbers are divided into groups of 3 bits each, starting at the binary point and proceeding towards left and right.

(i) Convert (101111010110.110110011)₂ into octal.

Solution :

Group of 3 bits are	101	111	010	110	.	110	110	011
Convert each group into octal =	5	7	2	6	.	6	6	3

The result is **(5726.663)₈**

(c) Binary to Hexadecimal conversion:- For conversion binary to hexadecimal number the binary numbers starting from the binary point, groups are made of 4 bits each, on either side of the binary point.

(ii) Convert (01011111011.011111)₂ into hexadecimal.

Solution:

Given Binary number	010	1111	1011	.	0111	11
Group of 3 bits are =	0010	1111	1011	.	0111	1100
Convert each group into octal =	2	F	B	.	7	C

The result is **(2FB.7C)₁₆**

2. DECIMALNUMBERSYSTEM:-

(a) Decimal to binary conversion:- In the conversion the integer number are converted to the desired base using successive division by the base or radix.

Forexample:(i)Convert(52)₁₀intobinary.

(ii) Convert (105.15)₁₀ into binary.

Solution:

Integer part	Fraction part
2 | 105	$0.15 \times 2 = 0.30$
2 | 52 — 1	$0.30 \times 2 = 0.60$
2 | 26 — 0	$0.60 \times 2 = 1.20$
2 | 13 — 0	$0.20 \times 2 = 0.40$
2 | 6 — 1	$0.40 \times 2 = 0.80$
2 | 3 — 0	$0.80 \times 2 = 1.60$
2 | 1 — 1	
0 — 1	

Result of (105.15)₁₀ is **(1101001.001001)₂**

(b) Decimal to octal conversion:- To convert the given decimal integer number to octal, successively divide the given number by 8 till the quotient is 0.

(i) Convert $(378.93)_{10}$ into octal.

Solution:

8	378		$0.93 \times 8 = 7.44$
8	47	— 2	$0.44 \times 8 = 3.52$
8	5	— 7	$0.52 \times 8 = 4.16$
	0	— 5	$0.16 \times 8 = 1.28$

Result of $(378.93)_{10}$ is $(572.7341)_8$

(c) Decimal to hexadecimal conversion:-

(i) Convert $(2598.675)_{10}$ into hexadecimal.

Solution:

		Remainder				Hex
		Decimal	Hex			
16	2598			$0.675 \times 16 = 10.8$		A
16	162	— 6	6	$0.800 \times 16 = 12.8$		C
16	10	— 2	2	$0.800 \times 16 = 12.8$		C
	0	— 10	A	$0.800 \times 16 = 12.8$		C

Result of $(2598.675)_{10}$ is $(A26.ACCC)_{16}$

3. OCTAL NUMBER SYSTEM:-

(a) Octal to binary conversion:- To convert a given a octal number to binary, replace each octal digit by its 3- bit binary equivalent.

For example:

Convert $(367.52)_8$ into binary.

Solution:

Given Octal number is

	3	6	7	.	5	2

Convert each group octal to binary

=	011	110	111	.	101	010

Result of $(367.52)_8$ is $(011110111.101010)_2$

(b) Octal to decimal conversion:- For conversion octal to decimal number, multiply each digit in the octal number by the weight of its position and add all the product terms

For example: -

Convert $(4057.06)_8$ to decimal
Solution:

$(4057.06)_8$ = $4 \times 8^3 + 0 \times 8^2 + 5 \times 8^1 + 7 \times 8^0 + 0 \times 8^{-1} + 6 \times 8^{-2}$

= $2048 + 0 + 40 + 7 + 0 + 0.0937$

= $(2095.0937)_{10}$

Result is $(2095.0937)_{10}$

(c) Octal to hexadecimal conversion:- For conversion of octal to Hexadecimal, first convert the given octal number to binary and then binary number to hexadecimal

(4) HEXADECIMAL NUMBER SYSTEM :- (a)Hexadecimal to binary conversion:- For conversionof hexadecimal to binary, replace hexadecimal digit by its 4 bit binary group

Convert $(3A9E.B0D)_{16}$ into binary.

Solution:

Given Hexadecimal number is   3   A   9   E   .   B   0   D

Convert each hexadecimal = 0011   1010   1001   1110   .   1011   0000   1101
digit to 4 bit binary

Result of $(3A9E.B0D)_8$ is $(0011101010011110.101100001101)_2$

(b)Hexadecimal to decimal conversion:- For conversion of hexadecimal to decimal, multiply eachdigitin the hexadecimalnumberby itspositionweightandaddall those product terms.

Convert $(A0F9.0EB)_{16}$ to decimal

Solution:

$(A0F9.0EB)_{16}$ = $(10 \times 16^3)+(0 \times 16^2)+(15 \times 16^1) +(9 \times 16^0) +(0 \times 16^{-1}) +(14 \times 16^{-2}) +(11 \times 16^{-3})$
           = $40960 + 0 + 240 + 9 + 0 +0.0546 + 0.0026$
           = $(41209.0572)_{10}$

Result is $(41209.0572)_{10}$

((c) Hexadecimal to Octal conversion:- For conversion of hexadecimal to octal, first convert the given hexadecimal number to binary and then binary number to octal

Arithmetic Operation-Addition, Subtraction, Multiplication, Division, 1's & 2's complement of Binary numbers& Subtraction using complements method

1. BINARYADDITION:-

Thebinaryadditionrulesareasfollows   carry   carry

0+0=0;   0+1=1;   1+0=1;   1+1=10,   SUM,   1+1+1=11   SUM

Add $(100101)_2$ and $(1101111)_2$.
Solution :-

             100101
    +   1101111
       10010100

Result is $(10010100)_2$

2. BINARYSUBTRACTION:-

Thebinarysubtractionrulesareasfollows

0-0=0;   1-1=0;   1-0=1;   0-1=11,   withaborrowof1

Substract $(111.111)_2$ from $(1010.01)_2$.
Solution :-

$$
\begin{array}{r}
1010.010 \\
-\quad 111.111 \\
\hline
0010.011 \\
\end{array}
$$

Result is $(0010.011)_2$

3. BINARYMULTIPLICATION:-

Thebinarymultiplicationrules areasfollows 0 x 0

= 0 ;   1 x 1 = 1 ;   1 x 0 = 0 ;   0x1=0

Multiply $(1101)_2$ by $(110)_2$.
Solution :-

$$
\begin{array}{r}
1101 \\
\times\quad 110 \\
\hline
0000 \\
1101 \\
+\quad 1101 \\
\hline
1001110 \\
\end{array}
$$

Result is $(1001110)_2$

4.BINARYDIVISION:-

The binary division is very simple and similar to decimal number system.

So we have only 2 rules0 ÷ 1 = 0   1 ÷ 1 = 1

$$
\begin{array}{r}
110\,)\,101101\,(\,111.1 \\
-\ \underline{110} \\
1010 \\
\underline{110} \\
1001 \\
\underline{110} \\
110 \\
\underline{110} \\
000 \\
\end{array}
$$

Result is $(111.1)_2$

1'sCOMPLEMENTREPRESENTATION:-

The 1's complement of a binary number is obtained by changing each 0 to 1 and each 1 to0.

Find (1100)$_2$ 1's complement.

Solution :-

Given	1	1	0	0
1's complement is	0	0	1	1

Result is **(0011)$_2$**

2'sCOMPLEMENTREPRESENTATION:-

The 2's complement of a binary number is a binary number which is obtained by adding 1 to the 1's complement of a number.

2'scomplement=1'scomplement+1

Find (1010)$_2$ 2's complement.

Solution :-

Given	1	0	1	0
1's complement is	0	1	0	1
+				1
2's complement	0	1	1	0

Result is **(0110)$_2$**

SIGNEDNUMBER:-

Insign – magnitude form, additional bitcalled the signbitis placed in front of the number.If the signbitis 0, the number is positive. If it is a 1, the number is negative.

```
0  1  0  1  0  0  1  =  +41
↑
Sign bit

1  1  0  1  0  0  1  =  -41
↑
Sign bit
```

SUBSTRACTIONUSINGCOMPLEMENTMETHOD:

1'sCOMPLEMENT:-

In 1's complement subtraction, add the 1's complement of subtrahend to the minuend. If there is a carry out, then the carry is added to the LSB. This is called end around carry. If the MSB is 0, the result is positive. If the MSB is 1, the result is negative and is in its 1's complement form. Then take its 1's complement to get the magnitude in binary.

Subtract (10000)₂ from (11010)₂ using 1's complement.

```
Solution:-
   1 1 0 1 0              1 1 0 1 0              =   26
-  1 0 0 0 0    =>     +  0 1 1 1 1  (1's complement)   = - 16
                Carry  →  1 0 1 0 0 1                 + 10
                       +          1
                          0 1 0 1 0   = +10
```

Result is **+10**

2'sCOMPLEMENT:-

In 2's complement subtraction, add the 2's complement of subtrahend to the minuend. If there is a carry out, ignore it. If the MSB is 0, the result is positive. Ifthe MSB is1, the resultis negative and is in its 2's complement form. Then take its 2's complement to get the magnitude in binary.

Subtract (1010100)₂ from (1010100)₂ using 2's complement.

```
Solution:-
   1 0 1 0 1 0 0            1 0 1 0 1 0 0           =    84
-  1 0 1 0 1 0 0   =>    +  0 1 0 1 1 0 0  (2's complement)  = -  84
                           1 0 0 0 0 0 0 0 ( Ignore the carry)      0
                        =           0 (result = 0)
```

Hence MSB is 0. The answer is positive. So it is +0000000 = **0**

DigitalCode&itsapplication& distinguishbetweenweighted& non-weight Code, Binary codes, excess-3 and Gray codes.

DIGITALCODES:-

In practice the digital electronics requires to handle data which may be numeric, alphabets and special characters. This requires the conversion of the incoming data into binary format before it can be processed. There is various possible ways of doing this and this process is called encoding. To achieve the reverse of it, we use decoders.

WEIGHTEDANDNON-WEIGHTEDCODES

 Therearetwotypesofbinarycodes

1) **Weighted binary codes** : In weighted codes, for each position (or bit) ,there is specific weight attached. For example, in binary number, each bit is assigned particular weight 2^n where'n'is the bit number forn = 0,1,2,3,4 the weights are 1,2,4,8,16 respectively. Example :-BCD

 2) Non-weightedbinarycodes:

Non-weighted codes are codes which are not assigned with any weight to each digit position, i.e., each digit position within the number is not assigned fixed value. Example:- Excess – 3 (XS -3) code and Gray codes

BINARY CODED DECIMAL (BCD):-BCD is a weighted code. In weighted codes, each successive digit from right to left represents weights equal to some specified value and to get the equivalent decimal number add the products of the weights by the corresponding binary digit. 8421 is the most common because 8421 BCD is the most natural amongst the other possible codes.

BCDADDITION:-

 Addition of BCD (8421) is performed by adding two digits of binary, starting from least significant digit. In case if the result is an illegal code (greater than 9) or if there is a carry outof one then add 0110(6) and add the resulting carry to the next most significant.

Add 679.6 from 536.8 using BCD addition.

Solution:-

```
   6 7 9 . 6           0110  0111  1001 . 0110    ( 679.6 in BCD)
 + 5 3 6 . 8      =>+ 0101  0011  0110 . 1000     (536.8 in BCD)
   1 2 1 6 . 4         1011  1010  1111 . 1110    ( All are illegal codes)
                     + 0110 +0110 +0110 .+0110    ( Add 0110 to each)
                0001  0010  0001  0110 . 0100
                  1     2     1     6  .  4        ( corrected sum = 1216.4)
```
Result is **1216.4**

BCDSUBTRACTION:-

The BCD subtraction is performed by subtracting the digits of each 4 – bit group of the subtrahend from corresponding 4 – bit group of the minuend in the binary starting from the LSD.Ifthereisnoborrowfromthenexthighergroup[thennocorrectionisrequired.If there is a borrow from the next group, then 6 (0110) is subtracted from the difference termof this group.

Subtract 147.8 from 206.7 using 8421 BCD code.

Solution:-

```
   2 0 6 . 7          0010  0000  0110 . 0111    ( 206.7 in BCD)
 - 1 4 7 . 8     =>- 0001  0100  0111 . 1000     (147.8 in BCD)
     5 8 . 9          0000  1011  1110 . 1111    ( Borrows are present)
                          - 0110 -0110 .- 0110
                     0101  1000 . 1001
                       5     8  .  9             ( corrected difference = 58.9)
```
Result is $(58.9)_{10}$

EXCESSTHREE(XS-3)CODE:-

The Excess-3 code, also called XS-3, is a non- weighted BCD code. This derives it name from the fact that each binary codeword isthecorresponding8421 codewordplus 0011(3).Itis a sequential code. It is a self complementing code.

Excess-3 code is non-weighted and self complementary code. A self complementary binary codes are always compliment themselves. The complement of a binary number can be obtained from that number by replacing 0's with 1's and 1's with 0's. The sum of binary number and itscomplementis alwaysequaltodecimal9.In otherwords,the1's complement of anexcess-3 code isthe excess-3code forthe9'scomplementofthecorrespondingdecimal number.

For example, the excess-3 code for decimal number 5 is 1000 and 1's complement of 1000 is 0111, which is excess-3 code for decimal number 4,andit is 9's complement of number 5.

ASCIICODE:-

The American Standard Code for Information Interchange (ASCII) pronounced as 'ASKEE' is widely used alphanumeric code. This is basically a 7 bit code. The number of different bit patterns thatcanbecreated with7bits is 27=128, the ASCIIcanbe used toencodeboth the uppercase and lowercase characters of the alphabet (52 symbols) and some special symbols in addition to the 10 decimal digits. It is used extensively for printers and terminals thatinterface with small computersystems. The table shown belowshows the ASCII groups.

GRAYCODE:-

The gray code is a non-weighted code. It is not a BCD code. It is cyclic code becausesuccessive words in this differ in one bit position only i.eitis a unit distance code. Gray codeisusedininstrumentationanddataacquisitionsystemswherelinearorangular displacement is measured.

BINARY-TO–GRAYCONVERSION:-

If an n-bit binary number is represented by B_n B_{n-1} ----- B_1 and its gray code equivalent by G_n G_{n-1} ----- G_1, where B_n and G_n are the MSBs , then gray code bits are obtained from the binary code as follows

$$G_n = B_n$$
$$G_{n-1} = B_n \oplus B_{n-1}$$
.
.
.
.
$$G_1 = B_2 \oplus B_1$$

Where the symbol $\oplus$ stands for Exclusive OR (X-OR)

GRAY- TO - BINARY CONVERSION:-

If an n-bit gray number is represented by G_n G_{n-1} ------- G_1 and its binary equivalent by B_n B_{n-1} ----- B_1, then binary bits are obtained from Gray bits as follows :

$$B_n = G_n$$
$$B_{n-1} = B_n \oplus G_{n-1}$$
.
.
.
.
$$B_1 = B_2 \oplus G_1$$

Logic gates: AND, OR, NOT, NAND, NOR, Exclusive-OR, Exclusive-NOR-- Symbol, Function, expression, truth table & timing diagram

LOGICGATES:-
- Logicgatesarethefundamentalbuildingblocksofdigitalsystems.
- Thereare3basictypesofgatesAND,ORandNOT.
- Logic gates are electronic circuits because they are made up of a number of electronic devices and components.
- Inputs and outputs of logic gates can occur only in 2 levels(logic 1, logic 0). These two levels are termed HIGH and LOW, or TRUE and FALSE, or ON and OFF
- *The table which lists all the possible combinations of input variables and the corresponding output of any logic circuit/device, called a **truth table**.*

DIFFERENTTYPESOFLOGICGATES

NOTGATE(INVERTER):-
- ANOTgate,alsocalledandinverter,hasonlyoneinputandoneoutput.
- Itisadevicewhoseoutputisalwaysthecomplementofitsinput.
- The output of a NOT gate is the logic 1 state when its input is in logic 0 state and the logic 0 state when its inputs is in logic 1 state.

IC No. :- 7404

Logic Symbol

A ——▷o—— out

Truth table

INPUT A	OUTPUT $\overline{A}$
0	1
1	0

ANDGATE:-
- AnANDgatehastwoormoreinputsbutonlyoneoutput.
- Theoutputislogic1stateonlywheneachoneofitsinputsisatlogic1state.
- Theoutputislogic0stateevenifoneofitsinputsisatlogic0state.

IC No.:- 7408

Logic Symbol

A
B ——D—— Q

Truth Table

		OUTPUT
A	B	Q=A . B
0	0	0
0	1	0
1	0	0
1	1	1

ORGATE:-
- AnORgatemayhavetwoormoreinputsbutonlyoneoutput.
- Theoutputislogic1state,evenifoneofitsinputis1
- Theoutputislogic0state,onlywheneachoneofitsinputsisinlogicstate.

IC No.:- 7432

Logic Symbol

Truth Table

INPUT		OUTPUT
A	B	Q=A + B
0	0	0
0	1	1
1	0	1
1	1	1

NANDGATE:-

• NANDgateisacombinationofanANDgateandaNOTgate.

• The output is logic 0 when each of the input is logic 1 and for any other combinationof inputs, the output is logic 1.

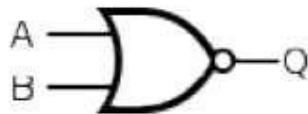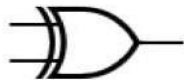ICNo.:-7400twoinputNANDgate

Logic Symbol

Truth Table

INPUT		OUTPUT
A	B	Q= $\overline{A \cdot B}$
0	0	1
0	1	1
1	0	1
1	1	0

NORGATE:-

• NORgateisacombinationofanORgateandaNOTgate.

• The output is logic 1, only when each one of its input is logic 0 and for any other combination of inputs the output is a logic 0 level.

ICNo.:-7402twoinputNORgate

Logic Symbol

Truth Table

INPUT		OUTPUT
A	B	Q= $\overline{A + B}$
0	0	1
0	1	0
1	0	0
1	1	0

EXCLUSIVE–OR(X-OR)GATE

• AnX-ORgateisatwoinput,oneoutputlogiccircuit.

• The output is logic 1 when one and only one of its two inputs is logic 1. When both the inputs is logic 0 or when both the inputs is logic 1, the output is logic 0.

IC No.:- 7486

Logic Symbol

INPUTS are **A** and **B**

OUTPUT is **Q** = A $\oplus$ B

= A$\overline{B}$ + A$\overline{B}$

Truth Table

INPUT		OUTPUT
A	B	Q = A $\oplus$ B
0	0	0
0	1	1
1	0	1
1	1	0

EXCLUSIVE–NOR(X-NOR)GATE

• AnX-NORgateisthecombinationofanX-ORgateandNOTgate

- AnX-NORgateisatwoinput,oneoutputlogiccircuit.
Theoutputislogic1onlywhenboththeinputsarelogic0orwhenboththeinputsis1.

- Theoutputislogic0whenoneoftheinputsislogic0andotheris1

IC No.:- 74266

Logic Symbol

OUT =A B + $\overline{A}$ $\overline{B}$

= A XNOR B

INPUT		OUTPUT
A	B	OUT =A XNOR B
0	0	1
0	1	0
1	0	0
1	1	1

UniversalGates&itsRealisation

UNIVERSALGATES:-

There are 3 basic gates AND, OR and NOT, there are two universal gates NAND and NOR.
Both NAND and NOR gates can perform all logic functions i.e. AND, OR, NOT, EXOR and
EXNOR.

NAND GATE:-

a) Inverter from NAND gate

Input   = A
Output Q = $\overline{A}$

b) AND gate from NAND gate

Input s are A and B
Output Q = A.B

c) OR gate from NOR gate

Inputs are **A** and **B**
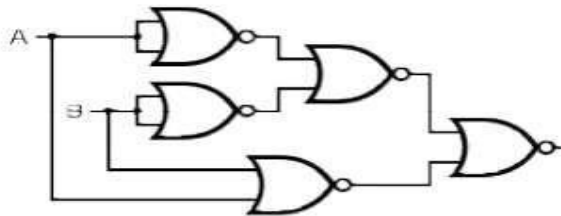Output **Q = A+B**

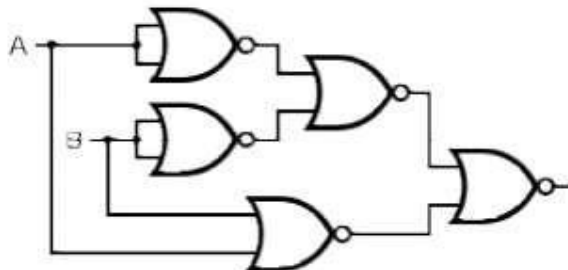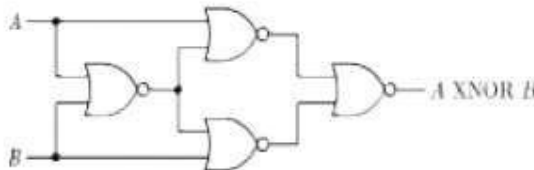## d) NAND gate from NOR gate

Inputs are **A** and **B**
Output **Q = $\overline{A.B}$**

e) EX-OR gate from NOR gate

Inputs are **A** and **B**
Output **Q = A $\overline{B}$ + $\overline{A}$B**

e) EX-OR gate from NOR gate

Inputs are **A** and **B**
Output **Q = A $\overline{B}$ + $\overline{A}$B**

f) EX-NOR gate From NOR gate

Inputs are **A** and **B**
Output **Q = A B + $\overline{A}$ $\overline{B}$**

Booleanalgebra,Booleanexpressions,Demorgan'sTheorems.

BOOLEANALGEBRAINTRODUCTION:-

• Switchingcircuitsarealsocalledlogiccircuits,gatescircuitsanddigitalcircuits.

• Booleanalgebraisasystemof mathematical logic. Itisanalgebraicsystemconsisting of the set of elements (0,1), two binary operators called OR and AND and unary operator called NOT.

• Itisthebasicmathematicaltoolintheanalysisandsynthesisofswitchingcircuits.

• Itisawaytoexpresslogicfunctionsalgebraically.

AXIOMSANDLAWSOFBOOLEANALGEBRA:-

Axioms or postulates of Boolean algebra are set of logical expressions that are accepted without proof and upon which we can build a set of useful theorems.

Axiom1: 0.0=0	Axiom5: 0+0=0	Axiom9: $\bar{1}$=0
Axiom2: 0 .1=0	Axiom6: 0+1=1	Axiom10: $\bar{0}$=1
Axiom3: 1.0=0	Axiom7: 1+0 =1	
Axiom4: 1.1=1	Axiom8: 1+1=1	

1. **ComplementationLaws:-**

   The term complement simply means to invert, i.e. to changes 0s to 1s and 1s to 0s.
   The five laws of complementation are as follows:
   Law1: $\bar{0}$=1
   Law2: $\bar{1}$=0
   Law3: ifA = 0,then $\bar{A}$= 1
   Law4: ifA=1,then $\bar{A}$=0
   Law5: $\bar{\bar{A}}$=0(doublecomplementationlaw)

2. **ORLaws:-**

   The four OR laws are asfollows
   Law 1: A + 0 = A (Null law)
   Law 2: A + 1 = 1(Identity law)
   Law 3: A + A = A
   Law4: A+ $\bar{A}$= 1

3. **ANDLaws:-**

   The four AND laws are as follows
   Law 1: A . 0 = 0 (Null law)
   Law 2: A . 1 =A (Identity law)
   Law 3: A . A = A
   Law4: A . $\bar{A}$=0

4. **CommutativeLaws:-**

   Commutative laws allow change in position of AND or OR variables. There are two commutative laws.
   Law 1: A+B = B +A
   Law 2: A . B = B . A

5. **AssociativeLaws:-**

   The associative laws allow grouping of variables. There are 2 associative laws.
   Law 1: (A + B) + C = A + (B + C)
   Law2: (A.B)C=A(B.C)

6. **DistributiveLaws:-**

The distributive laws allow factoring or multiplying out of expressions. There are two distributive laws.

Law 1: A (B + C) = AB + AC

Law 2: A + BC= (A+B) (A+C)

Proof:

RHS=(A+B)(A+C)=AA+AC+BA+BC

=A+AC+AB+BC

=A(1+C+B)+BC

=A.1+ BC   (1+C+B=1+B=1,   FROMORLaw2)

=A+ BC=LHS

7. **RedundantLiteralRule(RLR):-**

Law1: $A+\bar{B}=A+B$

Proof

$A+\bar{B}=(A+\bar{})(A+B)$

=1.(A+B)

=A+B

Law2: $A(\bar{}+B)= AB$

Proof

$A(\bar{}+B)=A\bar{}+AB=0+AB=AB$

8. **Idempotence Laws:-**Idempotence means same value. Law 1:   A. A = A

Law2:   A+A=A

9. **AbsorptionLaws:-**

Therearetwolaws:

Law1:   A+A·B=A

Proof: A+A·B

               =A(1+B)

               =A·1=A

Law2:   A(A+B)=A

Proof: A(A+B)

             = A·A+A·B

             =A+AB

             =A(1+B)

             =A·1=A

12.DeMorgan'sTheorem:-

DeMorgan'stheoremrepresentstwolawsinBooleanalgebra.

This law states that the complement of a sum of variables is equal to the product of their individual complements.

Law1: $\overline{\square + \square} = \bar{\square}\cdot\bar{\square}$

Proof

A	B	A + B	$\overline{A + B}$
0	0	0	1
0	1	1	0
1	0	1	0
1	1	1	0

=

A	B	$\overline{A}$	$\overline{B}$	$\overline{A}\,\overline{B}$
0	0	1	1	1
0	1	1	0	0
1	0	0	1	0
1	1	0	0	0

Law2: $\overline{A}.\overline{B}=\overline{A}+\overline{B}$

This law states that the complement of a product of variables is equal to the sum of their individual complements.

Proof

A	B	A . B	$\overline{A . B}$
0	0	0	1
0	1	0	1
1	0	0	1
1	1	1	0

=

A	B	$\overline{A}$	$\overline{B}$	$\overline{A} + \overline{B}$
0	0	1	1	1
0	1	1	0	1
1	0	0	1	1
1	1	0	0	0

Represent Logic Expression: SOP & POS forms

SUM - OF - PRODUCTS FORM:-

• This is also called disjunctive Canonical Form (DCF) or Expanded Sum of Products Form or Canonical Sum of Products Form.

• In this form, the function is the sum of a number of products terms where each product term contains all variables of the function either in complemented or uncomplemented form.

The or product term which contains all the variables of the functions either in complemented uncomplemented form is called a **minterm**.

• Themintermisdenotedasmo,m1,m2….An'n'variablefunctioncanhave2^n minterms.

$f (A, B, C) =\sum m (1, 2, 3, 5)$

PRODUCT-OF-SUMSFORM:-

• This form is also called as Conjunctive Canonical Form (CCF) or Expanded Product - of– Sums•This is by considering the combinations for which f = 0

• Eachtermisasumofallthevariables.

The sum term which contains each of the 'n' variables in either complemented or uncomplemented form is called a **maxterm.**

• Maxterm is represented as M0, M1, M2, …….

$f(A, B, C) = \Pi M (0, 4, 6, 7)$

Karnaughmap(3 &4Variables)& Minimizationoflogical expressions, don't care conditions

KARNAUGHMAPORK-MAP:-

- The K- map is a chart or a graph, composed of an arrangement of adjacent cells, each representing a particular combination of variables in sum or product form
- .•The K-map is systematic method of simplifying the Boolean expression.

Mapping of SOP Expression:-

- The n variable K-map has 2^n squares. These squares are called cells.
- A '1' is placed in any square indicates that corresponding minterm is included in the output expression, and a 0 or no entry in any square indicates that the corresponding minterm does not appear in the expression for output.

Unit-2: Combinational logic circuits

COMBINATIONAL LOGIC CIRCUIT

- A combinational circuit consists of logic gates whose outputs at any time are determined from only the present combination of inputs.

- A combinational circuit performs an operation that can be specified logically by a set of Boolean functions. It consists of an interconnection of logic gates. Combinational logic gates react to the values of the signals at their inputs and produce the value of the output signal, transforming binary information from the given input data to a required output data.

Half adder

The most basic arithmetic operation is the addition of two binary digits. This simple addition consists of four possible elementary operations: 0+0=0, 0+1=1, 1+0=1, and 1+1=10.

The first three operations produce a sum of one digit, but when both augend and addend bits are equal to 1; the binary sum consists of two digits. The higher significant bit of this result is called a carry.
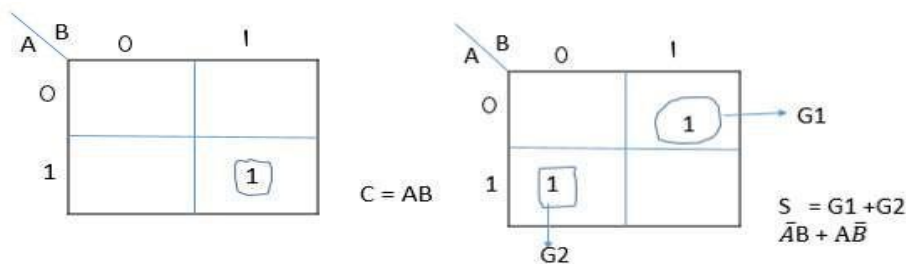
When the augend and addend numbers contain more significant digits, the carry obtained from the addition of two bits is added to the next higher order pair of significant bits.

A combinational circuit that performs the addition of two bits is called a half adder.

- This circuit needs two binary inputs and two binary outputs.

The input variables designate the augend and addend bits; the output variables produce the sum and carry. Symbols x and y are assigned to the two inputs andS (for sum) and C (for carry) to the outputs. The truth table for the half adder is listed in the belowtable.

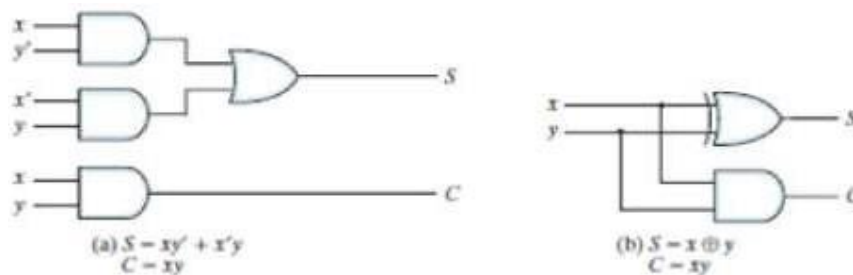| Input		Output	
A	B	Carry	Sum
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

C = AB

S = G1 +G2
ĀB + AB̄

• The C output is 1 only when both inputs are 1. The S output represents the least significant bit of the sum.•The simplified Boolean functions for the two outputs can be obtaineddirectly from the truth table.

Thesimplifiedsum-of-productsexpressionsare   S=A'B+AB'   C=AB

• The logic diagram of the half adder implemented in sum of products is shown in the below figure. It can be also implemented with an exclusive-OR and an AND gate.

(a) S = xy' + x'y
C = xy

(b) S = x⊕y
C = xy

Fulladder

One that performs the addition of three bits (two significant bits and a previous carry) is a full adder. The names of the circuits stem from the fact that two half adders can be employed to implement a full adder.

• A full adder is a combinational circuit that forms the arithmetic sum of three bits. •It consists of three inputs and two outputs. Two of the input variables, denoted by x and y , represent the twosignificant bits to beadded. The third input,z ,represents the carry from

the previous lower significant position. The two outputs are designated by the symbols S for sum and C for carry. The simplified expressions are
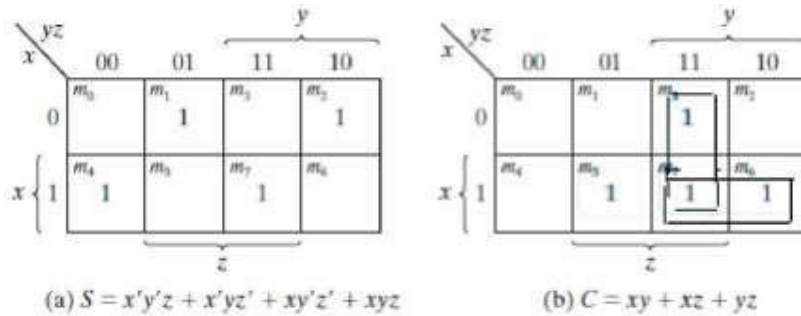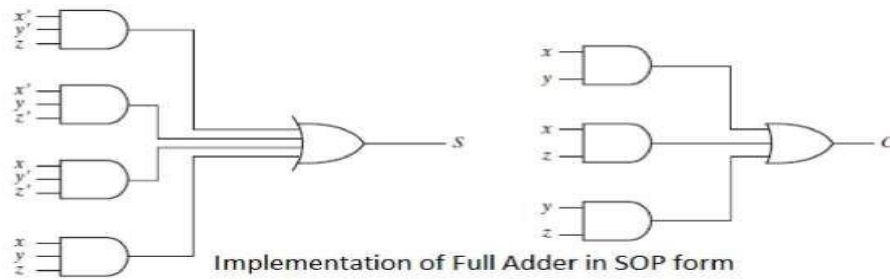
$S = x'y'z + x'yz' + xy'z' + xyz$

$C = xy + xz + yz$

• The logic diagram for the full adder implemented in sum-of-products form is shown in figure

x	y	z	C	S
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

Truth Table

(a) $S = x'y'z + x'yz' + xy'z' + xyz$ (b) $C = xy + xz + yz$

K-Map for full adder

Implementation of Full Adder in SOP form

It can also be implemented with two half adders and one OR gate as shown in the figure.
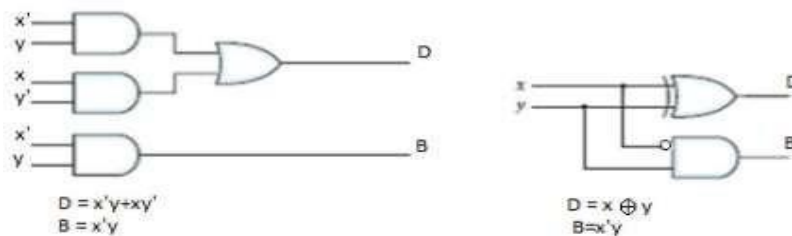
Half Adder

Half Subtractor

This circuit needs two binary inputs and two binary outputs.The subtraction operation isdone by using the following rules as: $0 - 0 = 0$; $0 - 1 = 1$ with borrow 1; $1 - 0 = 1$; $1 - 1 = 0$

Symbols x and y are assigned to the two inputs and D (for difference) and B (for borrow) to the outputs.•The truth table for the half subtractor is listed in the below table

x	y	D	B
0	0	0	0
0	1	1	1
1	0	1	0
1	1	0	0

The simplified Boolean functions for the two outputs can be obtained directly from the truth table. The simplified sum-of-products expressions are $D = x'y + xy'$ and $B = x'y$

The logic diagram of the half adder implemented insum of products is shownin the figure.Itcanbealsoimplementedwithanexclusive-ORandanANDgatewithoneinvertedinput.

D = x'y+xy'
B = x'y

D = x ⊕ y
B=x'y

FullSubtractor

A full subtractor is a combinational circuit that forms the arithmetic subtraction operation of threebits.Itconsistsofthreeinputsandtwooutputs.Twooftheinputvariables,denoted by x and y , represent the two significant bits to be subtracted. The third input, z , issubtracted from the result 0f the first subtraction.
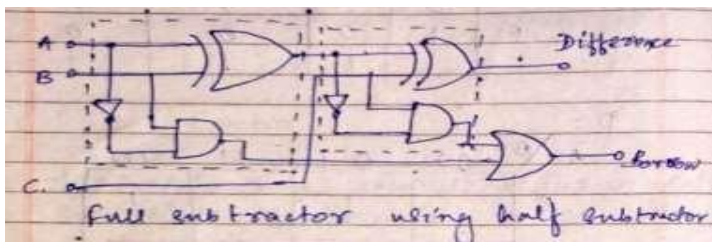

Truth Table

K-Map for full Subtractor

$D = x'y'z+x'yz'+xy'z'+xyz$

$B = x'z+x'y+yz$

full subtractor using half subtractor

The binary variable D gives the value of the least significant bit of the difference. The binary variable B gives the output borrow formed during the subtraction process.

ParallelBinary4bitadder

 Abinaryadderisadigitalcircuitthatproducesthearithmeticsumoftwobinarynumbers.

It can be constructed with full adders connected in cascade, with the output carry from each full adder connected to the input carry of the next full adder in the chain.

Addition of n-bit numbers requires a chain of n full adders or a chain of one-half adder andn-1 full adders. The interconnection of four full-adder (FA) circuits to provide a four-bit binary ripple carry adder is shown in the figure.
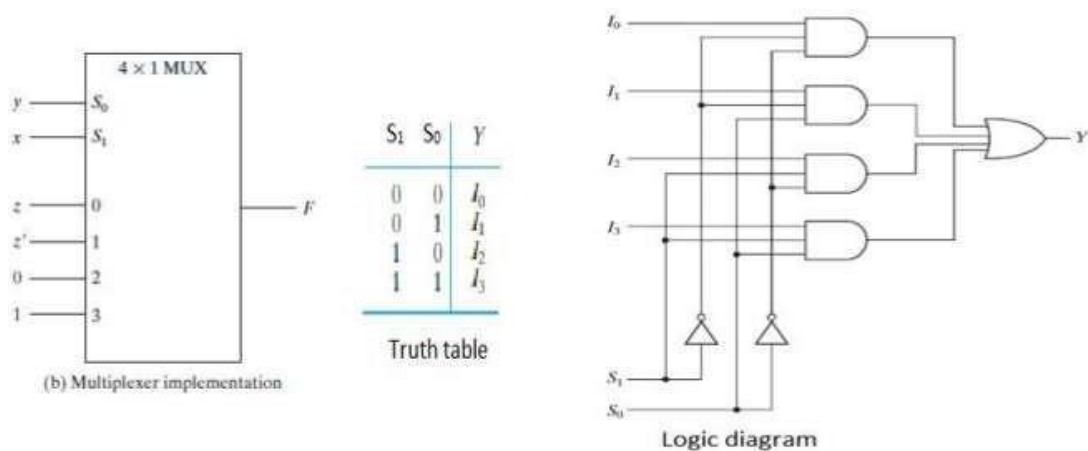

Four Bit Binary Adder

TheaugendbitsofAandtheaddend bitsofBare designated bysubscript numbers from right to left, with subscript 0 denoting the least significant bit. The carries are connected in a chainthrough thefull adders.Theinputcarrytothe adderisC_0, andit ripples through the full adders to the output carry C_4. The Soutputs generate the required sumbits.

Multiplexer(4:1)

A multiplexer is a combinational circuit that selects binary information from one of many input lines and directs it to a single output line.

• The selection of a particular input line is controlled by a set of selection lines. Normally, there are 2^n input lines and n selection lines whose bit combinations determine which inputis selected. A four-to-one-line multiplexer is shown in the below figure.
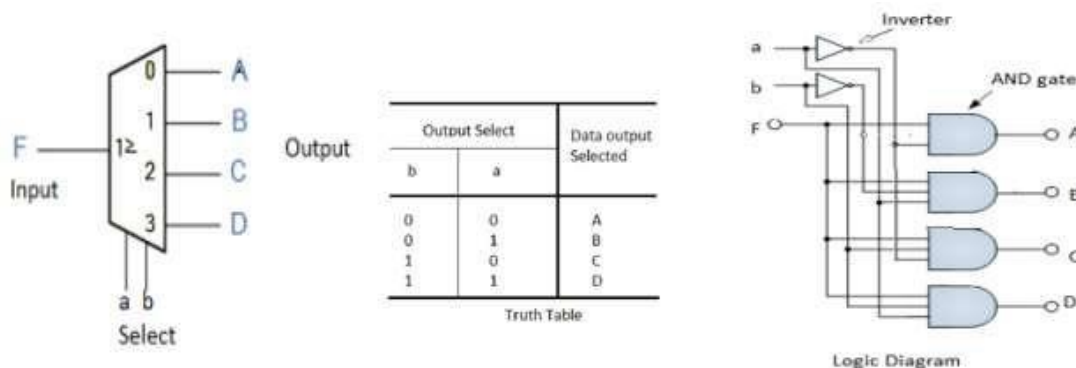

(b) Multiplexer implementation

Truth table

Logic diagram

Each of the four inputs, I0 through I3, is applied to one input of an AND gate. Selection lines S1 and S0 are decoded to select a particular AND gate. The outputs of the AND gates are applied to a single OR gate that provides the one-line output.

• A multiplexer is also called a **data selector**, since it selects one of many inputs and steers the binary information to the output line.

De-multiplexer(1:4)

The data distributor, known more commonly as a Demultiplexer or "Demux" for short, is the exact opposite of the Multiplexer. •The demultiplexer takes one single input data line and then switches it to any one of a number of individual output lines one at a time. The demultiplexer converts a serial data signal at the input to a parallel data at its output lines as shown below.

Truth Table

Logic Diagram

The functionof the demultiplexer is to switchone common data inputlineto any one ofthe4 output data lines A to D in our example above. As with the multiplexer the individual solid state switches areselected by the binary input address codeon the output select pins "a"and "b" as shown

Decoder

A decoder is a combinational circuit that converts binary information from n input lines to a maximum of 2^n unique output lines.

• The decoders presented here are called n -to- m -line decoders, where m … 2n. Their purpose is to generate the 2^n (or fewer) minterms of n input variables. Each combination of inputs will assert a unique output. The name decoder is also used in conjunction with other code converters, such as a BCD-to-seven-segment decoder.

Atwo-to-four-linedecoderwithanenableinputconstructedwithNANDgatesisshownin Fig. •The circuit operates with complemented outputs and a complement enable input. The decoder is enabled when E is equal to 0 (i.e., active-low enable). As indicated by the truth table, only one output can be equal to 0 at any given time; all other outputs are equal to 1.•The output whose value is equal to 0 represents the minterm selected by inputs A and B.•Thecircuitis disabled when E is equal to 1, regardless ofthe valuesof the othertwo inputs.
• When the circuit is disabled, none of the outputs are equal to 0 and none of the minterms are selected.
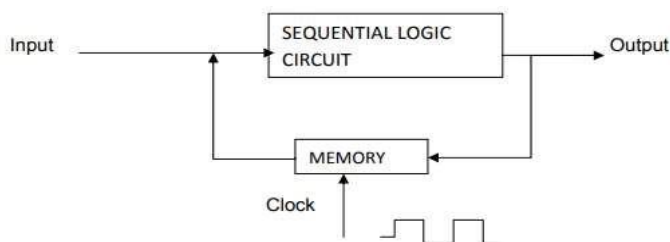
Unit-3:Sequential logicCircuits

SEQUENTIALLOGICCIRCUITSEQUENTIALCIRCUIT:

• It is a circuit whose output depends upon the present input, previous output and the sequence in which the inputs are applied.

HOWTHESEQUENTIALCIRCUITISDIFFERENTFROMCOMBINATIONALCIRCUIT?

In combinational circuit output depends upon present input at any instant of time and do not use memory. Hence previous input does not have any effect on the circuit. But sequential circuit has memory anddepends upon present input andprevious output.

Sequential circuits are slower than combinational circuits and these sequential circuits are harder to design.

TYPES:-

Sequentiallogiccircuits(SLC)areclassifiedas(i)SynchronousSLC(ii)AsynchronousSLC

• The SLC that are controlled by clock are called synchronous SLC and those which are not controlled by a clock are asynchronous SLC.

• **Clock**:-Arecurringpulseiscalledaclock.

FLIP-FLOPANDLATCH:-

• A flip-flop or latch is a circuit that has two stable states and can be used to store information.

• A flip-flop is a binary storage device capable of storing one bit of information. In a stable state, the output of a flip-flop is either 0 or 1.

• Latchisanon-clockedflip-flopanditisthebuildingblockfortheflip-flop.

• A storage element in digital circuit can maintain a binary state indefinitely until directed by an input signal to switch state.

• Storage element that operate with signal level are called latches and those operate with clock transition are called as flip-flops. SEQUENTIAL LOGIC CIRCUIT MEMORY

• The circuit can be made to change state by signals applied to one or more control inputs and will have one or two outputs.

• A flip-flop is called so because its output either flips or flops meaning to switch back and forth.

• A flip-flop is also called a bi-stable multi-vibrator as it has two stable states. The input signals which command the flip-flop to change state are called excitations.

• Flip-flopsarestoragedevicesandcanstore1or0.

• Flip-flops using the clock signal are called clocked flip-flops. Control signals are effective only if they are applied in synchronization with the clock signal.

• Clock-signalsmaybepositive-edgetriggeredornegative-edgetriggered.

• Positive-edge triggered flip-flops are those in which state transitions take place only at positive- going edge of the clock pulse.

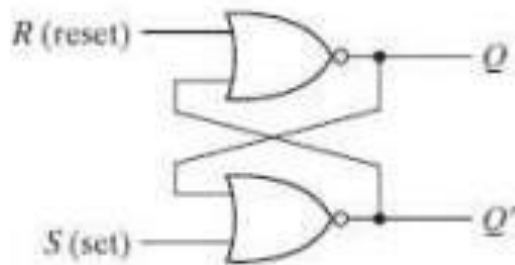Typesofflip-flopsinclude

a) SR(set-reset)F-F
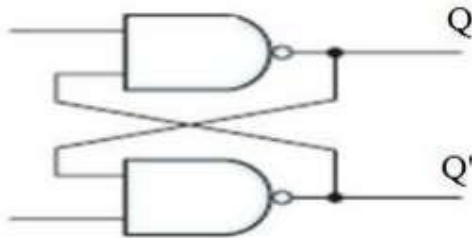
b) D(dataordelay)F-F

c) T(toggle)F-Fand

d) JKF-F

SRlatchusingNORgate:-

TheSRlatchisacircuitwithtwocross-coupledNORgatesortwocross-coupledNANDgates.
• IthastwooutputslabeledQandQ'.TwoinputsaretherelabeledSforsetandRfoereset.
• The latch has two useful states. When Q=0 and Q'=1 the condition is called reset state and when Q=1 and Q'=0 the condition is called set state. •Normally Q and Q' are complement of each other
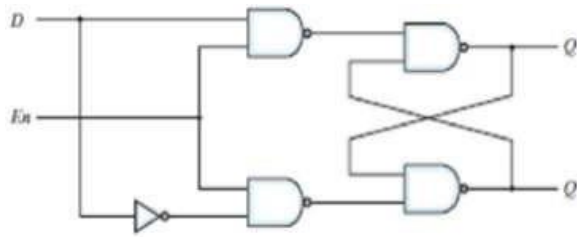
R (reset) ⟶ Q

S (set) ⟶ Q'

SRlatchusingNANDgate:-

Q

Q'

Input		Output		Comment
S	R	Q	Q_{Next}	
0	0	0	0	No change
0	0	1	1	
0	1	0	0	Reset
0	1	1	0	
1	0	0	1	Set
1	0	1	1	
1	1	0	X	Prohibited state
1	1	1	X	

RacingCondition:-

 In case of a SR latch when S=R=1 input is given both the output will try to become 0. This is called Racing condition.
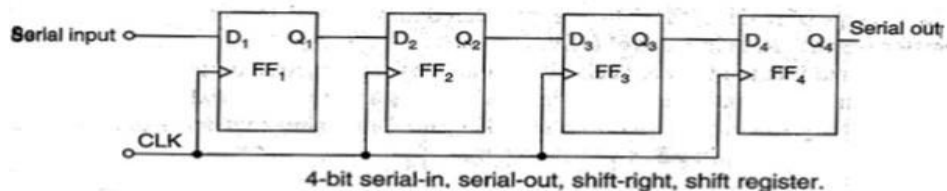
DLATCH:-

Unit-4:Registers,Memories&PLD

Shift Registers-Serial in Serial -out, Serial- in Parallel-out, Parallel in serial out and Parallel in parallel out

REGISTERSINTRODUCTION:-

• The sequential circuits known as register,are used for storage and transfer of binary information in a digital system.

• Aregisterhasnocharacteristicsinternalsequenceofstates.

• The storage capacity of a register is defined as the number of bits of digital data, it can store or retain.

SERIALIN,SERIALOUTSHIFTREGISTER:-

• This type of shift register accepts data serially, i.e., one bit at a time and also outputs data serially. •The logic diagram of a four bit serial in, serial out shift register is shown in below figure:
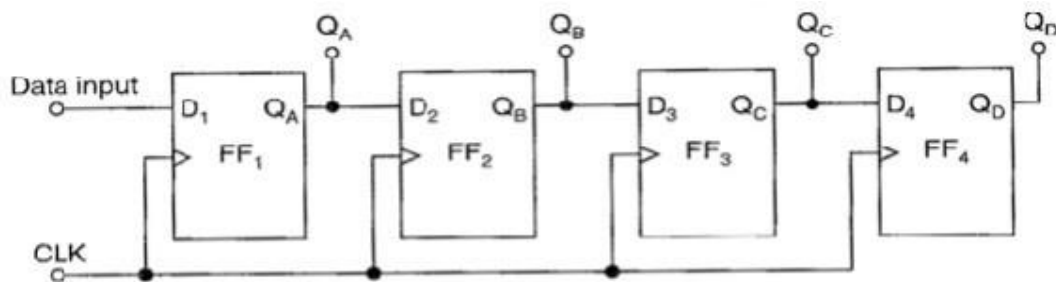

4-bit serial-in, serial-out, shift-right, shift register.

• In4stagesi.e.with4FFs,theregistercanstoreupto4bitsofdata.

• Serial data is applied at the D input of the first FF. The Q output of the first FF is connectedtothe Dinputof the second FF, the output ofthe second FFisconnectedtotheDinput of the third FF andthe Q output of the third FF is connected to the Dinput of thefourth FF.

ThedataisoutputtedfromtheQterminalofthelastFF.

• When a serial data is transferred to a register, each new bit is clocked into the first FF at the positive going edge of each clock pulse.

• The bit that is previously stored by the first FF is transferred to the second FF. •The bit that is stored by the second FF is transferred to the third FF, and so on.
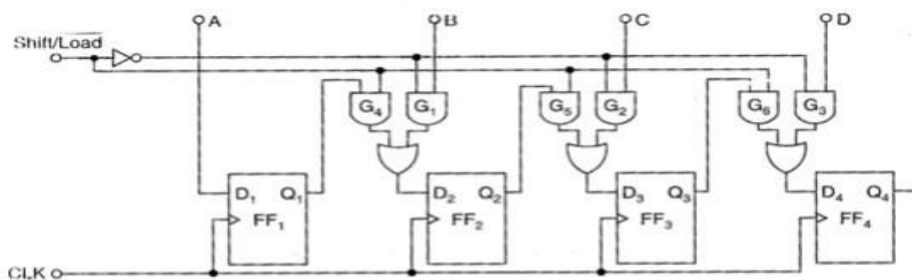
• ThebitthatwasstoredbythelastFFisshiftedout.

SERIAL IN, PARALLEL OUT SHIFT REGISTER:-

• In this type of register, the data bits are entered into the register serially,the data stored in the register serially, but the stored in the register is shifted out in the parallel form.

• When the data bits are stored once, each bits appears on its respective output line and all bits are available simultaneously.

• The logic diagram and logic symbol of a 4 bit serial in, parallel out shift register is given below.

PARALLEL IN, SERIAL OUT SHIFT REGISTER:-

• For parallel in, serial out shift register the data bits are entered simultaneously into their respective stages on parallel lines, but the data bits are transferred out of the register serially, i.e., on a bit by bit basis over a single line.

• The logic diagram and logic symbol of 4 bit parallel in, serial out shift register using D FFs is shown below.
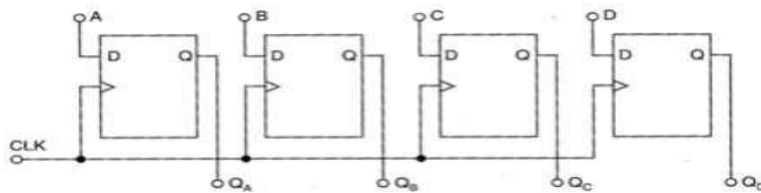

• There are four data lines A, B, C and D through which the data is entered into the register in parallel form.

• The signal Shift /LOAD allows 1. The data to be entered in parallel form into the register and 2. The data to be shifted out serially from terminal Q4.

• When Shift /LOAD line is HIGH, gates G1, G2, and G3 are disabled, but gates G4, G5 and G6 are enabled allowing the data bits to shift right from one stage to next.

• When Shift /LOAD line is LOW, gates G4, G5 and G6 are disabled, whereas gates G1, G2 and G3 are enabled allowing the data input to appear at the D inputs of the respective FFs.

• When clock pulse is applied, these data bits are shifted to the Q output terminals of the FFs and therefore the data is inputted in one step.

• The OR gate allows either the normal shifting operation or the parallel data entry depending on which AND gates are enabled by the level on the Shift/LOAD input.

PARALLELIN,PARALLELOUTSHIFTREGISTER:-

• In a parallel in, parallel out shift register, the data entered into the register in parallel form and also the data taken out of the register in parallel form. Immediately following the simultaneous entry of all data bits appear on the parallel outputs.

• Thefigureshownbelowisa4bitparallelinparalleloutshiftregisterusingDFFs.

Logic diagram of a 4 – bit parallel in, parallel out shift register

• DataappliedtotheDinputterminalsoftheFFs.

• When a clock pulse is applied at the positive edge of that pulse, the D inputs are shifted into the Q outputs of the FFs.

• The register now stores the data. The stored data is available instantaneously for shifting out in parallel form.

APPLICATIONSOFSHIFTREGISTERS

1. Time delays: •In digital systems, it is necessary to delay the transfe data have been completed, or to synchronize the arrival of data at a subsystem where it is processed with other data. •A shift register can beused to delay the arrival of serial data by a specificnumber ofclock pulses, since the number of stages corresponds to the number of clockpulses requiredto shift each bit completely through the register.•The total time delay canbe controlled by adjusting the clock frequency and by the number of stages in the register.•In practice,the clockfrequencyis fixedandthetotal delaycanbeadjustedonlyby controlling the number of stages through which the data is passed.

2. Serial / Parallel data conversion: •Transfer of data in parallel form is much faster than that in serial •Similarly the processing of data is much faster when all the data bits are available simultaneously. Thus in digital systems in which speed is important so to operate on data parallel form is used. •When large data is to be transmitted over long distance costly and impracticable. •It is convenient and economical to transmit data in serial form, since serial data transmission requires only one line.

Unit-5:A/DandD/AConverters

A **Digital to Analog Converter (DAC)** converts a digital input signal into an analog output signal. The digital signal is represented with a binary code, which is a combination of bits 0 and 1.
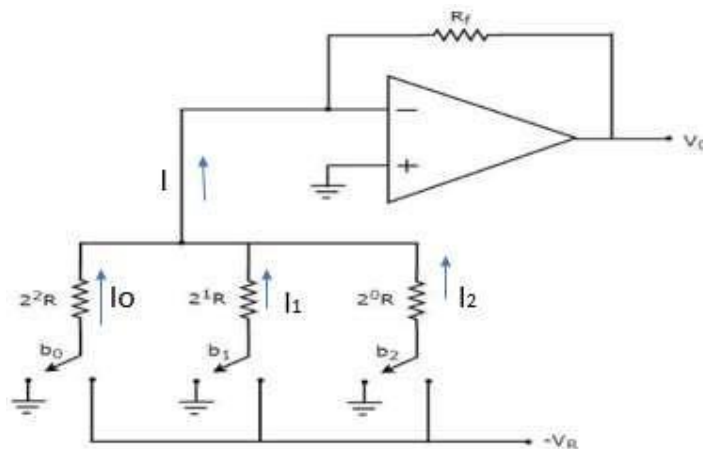
TypesofDACs

Therearе**twotypes**ofDACs

- WeightedResistorDAC
- R-2RLadderDAC

Binary-WeightedResistorDAC

A weighted resistor DAC produces an analog output, which is almost equal to the digital (binary) input by using **binary weighted resistors** in the inverting adder circuit. In short, a binary weighted resistor DAC is called as weighted resistor DAC. The **circuit diagram** of a 3-bit binary weighted resistor DAC is shown in the following figure –

The bits of a binary number can have only one of the two values. i.e., either 0 or 1. Let the **3-bit binary input** is b2 b1 b0. Here, the bits b2 and b0 denote the **Most Significant Bit (MSB) and Least Significant Bit (LSB)** respectively.

The **digital switches** shown in the above figure will be connected to ground, when the corresponding input bits are equal to '0'. Similarly, the digital switches shown in the above figure willbe connected to the negative reference voltage, –VR when the correspondinginput bits are equal to '1'.

In the above circuit, the non-inverting input terminal of an op-amp is connected to ground. Thatmeans zero voltsis appliedatthenon-invertinginputterminalofop-amp. TheOP-Amp is performing summation of all currents entering through its inverting terminal.

If the output voltage of the opamp is Vo, then

$V_0 = -I * R_f$

$Vo = -(I_0 + I_1 + I_2) * Rf$

$$=> \frac{V_0}{R_f} = \frac{V_R b_2}{2^0 R} + \frac{V_R b_1}{2^1 R} + \frac{V_R b_0}{2^2 R}$$

$$=> V_0 = \frac{V_R R_f}{R} \left\{ \frac{b_2}{2^0} + \frac{b_1}{2^1} + \frac{b_0}{2^2} \right\}$$

The**disadvantages**ofabinaryweightedresistorDACareasfollows−

- ThedifferencebetweentheresistancevaluescorrespondingtoLSB&MSBwill increase as the number of bits present in the digital input increases.
- Itisdifficulttodesignmoreaccurateresistorsasthenumberofbitspresentinthe digital input increases.

SuccessiveApproximationA/DConverter:

This is the most widely usedA/D converter.The basic principle of this type of A/Dconverteris that the unknown analog input voltage is approximated against an n-bit digital value by trying one bit at a time, beginning with the MSB. This type of ADC operates by successively dividing the voltage range by half, as explained in the following steps. It consists of a successive approximation register (SAR), DAC and comparator. The output of SAR is given ton-bit DAC. The equivalent analog output voltage of DAC, VD is applied to the non-inverting input of the comparator. The second input to the comparator is the unknown analog input voltage VA. The output of the comparator is used to activate the successive approximation logic of SAR. The configurationof successive approximation process for a 4-bit conversion is explained here When the start command is applied, the SAR sets the MSB to logic 1 and other bits are made logic 0, so that the trial code becomes 1000

(1) The MSB is initially set to 1 with the remaining three bits set as 000. The digital equivalent voltage is compared with the unknown analog input voltage.
(2) If the analog input voltage is higher than the digital equivalent voltage, the MSB isretained as 1 and the second MSB is set to 1. Otherwise, the MSB is set to 0 and the second MSB is set to 1. Comparison is made as given in step (1) to decide whether to retain or reset the second MSB.
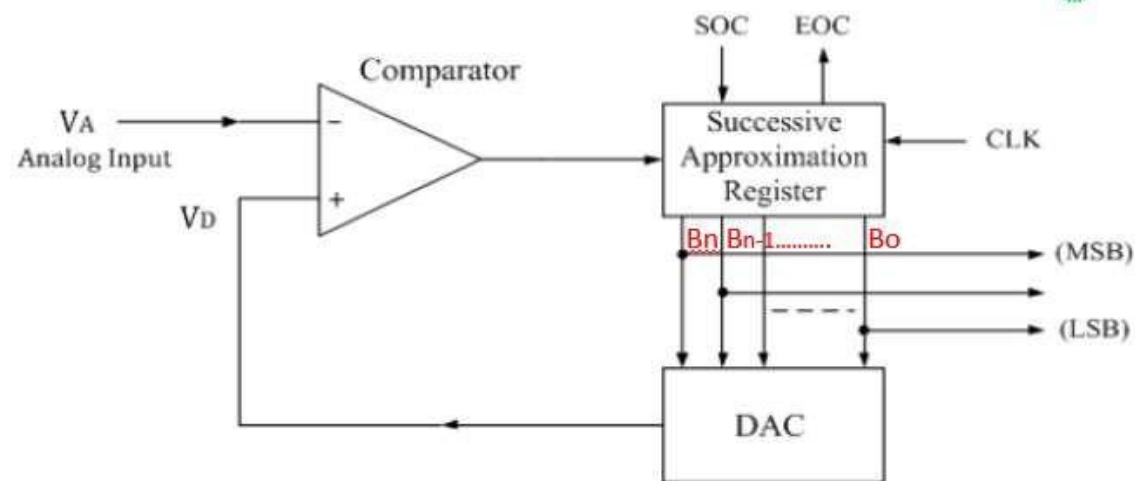Theabovestepsaremoreaccuratelyillustratedwiththehelpofanexample.
Let us assume that the 4-bit ADC is used and the analog input voltage is VA = 11 V. when the conversion starts, the MSB bit is set to 1.
NowVA=11V>VD=8V=[1000]2
SincetheunknownanaloginputvoltageVAishigherthantheequivalentdigitalvoltage

Since the analog input (26.1 V) is less than D/A output (i.e. 32 V) the MSB is set to zero. Then 1 is placed in bit next to MSB. Now the output of D/A is 16 V. Since analog input is more than16V, this 1 is retained in this bit position. Next 1 is placed in thirdbit position.

Now the D/A outputis 24 V whichisless than analog input. Therefore this1 bit is retained and 1 is placed in the next bit. Now the D/A output is 28 V, which is more than analog input. Thereforethis1bitissettozeroand1isplacedin5thbitpositionproducingaD/Aoutput of 26 V. It is less than analog input. Therefore this 1 bit is retained. Now 1 is placed in LSB producing a D/A output of 27 V which is more than analog input. Therefore LSB is set to zero and the converter gives an output of 26 V. The successive approximation method of A/D converter is very fast and takes only about 250 ns/ bit

Unit-6:LOGIC FAMILIES

 A circuit configuration or approach used to produce a type of digital integrated circuit is called Logic Family.

Byusinglogicfamilieswecangeneratedifferentlogicfunctions,whenfabricatedinthe form of an IC with the same approach, or in other words belonging to the same logic family, will have identical electrical characteristics.The set of digital ICs belonging to the same logic family are electrically compatible with each other.

 Some common Characteristics of the Same Logic Family include Supply voltage range, speedof response, power dissipation, input and output logic levels, current sourcing and sinking capability, fanout, noise margin, etc.

TYPESOFLOGICFAMILYACCORDINGTOICFABRICATION

• The entire range of digital ICs is fabricated using either bipolar devices or MOS devices or a combination of the two.

Bipolar familiesinclude:-

 Diode logic (DL)

Resistor-Transistorlogic(RTL)

 Diode-transistor logic (DTL) Transistor-

Transistor logic (TTL)

Emitter Coupled Logic (ECL), (also known as Current Mode Logic(CML))
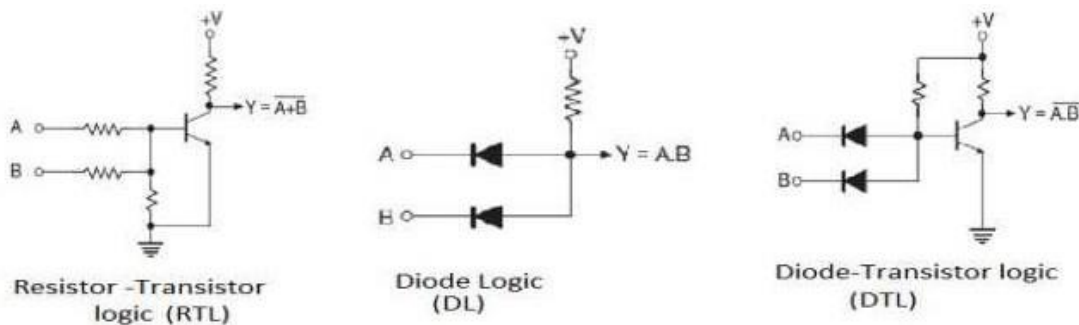
Integrated Injection logic (I2L)

TheBi-MOSlogicfamilyusesbothbipolarandMOSdevices.

MOSfamiliesinclude:-

The PMOS family (using P-channel MOSFETs)

TheNMOSfamily(usingN-channelMOSFETs)

TheCMOSfamily(usingbothN-andP-channeldevices)

Resistor -Transistor logic (RTL)   Diode Logic (DL)   Diode-Transistor logic (DTL)

CHARACTERISTICSOFLOGICFAMILY:-

DCSupplyVoltage:-

• The nominal value of the dc supply voltage for TTL (transisitor-transistor logic) and CMOS (complementary metal-oxide semiconductor) devices is +5V. this voltage is connected to Vccor VDD pin of an IC package and ground is connected to the GND pin.

NoiseImmunity:-

It is an unwanted signal that is superimposed on the normal operating signal. Noise may be due to various factors like operating environment, radiations, stray electrical and magnetic fields.

In digital logic circuits, the binary values 0 and 1 represent the LOW and HIGH voltage levels. Due to the interference of the noises, the voltage levels may increase or decrease. This may lead to the wrong operation of the device.

• Noiseistheunwantedvoltagethatisinducedinelectricalcircuitsandcanpresenta threat to the poor operation of the circuit. In order not to be adversely effected by noise, a logic circuit must have a certain amount of 'noise immunity'. •This is the ability to tolerate a certain amount of unwanted voltage fluctuation on its inputs without changing its outputstate is called Noise Immunity.

NoiseMargin:-

- Ameasureofacircuit'snoiseimmunityiscalled'noisemargin'whichisexpressedinvolts.
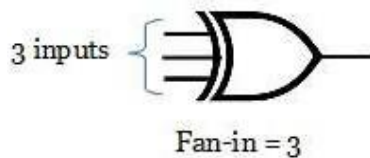- There are two values of noise margin specified for a given logic circuit: the HIGH (VNH) and LOW (VNL) noise margins

PowerDissipation:

It is the amount of power that the digital circuit dissipates. The power dissipated is determined by the average current, that is drawn from the supply voltage.
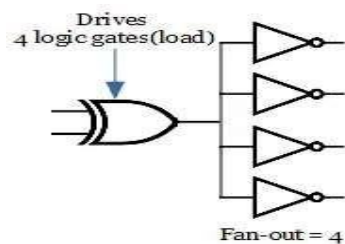
Propagationdelay

When a signal passes (propagates) through a logic circuit, it always experiences a time delayIt is the time interval between the application of the input pulse and the occurrence of the output. It is an important characteristic of the digital logic family. If the propagation delay is less, then the *speed* at which the IC operates will be faster.

Fan-inrefers to thenumber of inputsin a digital logic gate family. For the example givenin thefigurebelow,theEX-ORgatehasthreeinputs.Sofan-inforthegivenEX-ORgateis3.

FanOutofGates:-

- When theoutputofalogicgate is connected toone or moreinputs of othergates, a load on the driving gate is created. The maximum number of load gates that a given gate can drive is called the 'Fan-Out' of the gate. For example, the following circuithas an EX-OR gate, which drives 4 NOT gates. So fan-out of EX-OR gate is 4.

Reference

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2. ModernDigitalElectronicsbyRPJAINTMH
3. Fundamentalof Digital Electronics by Ananda Kumar-PHI Publication 3. Digital Electronics by P.RAJA ,SCITECH Publication