

# Ravi Maths Tuition

## Triangles

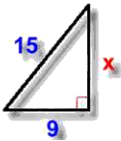
10th Standard

## Maths

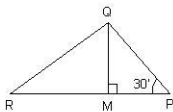
Multiple Choice Question

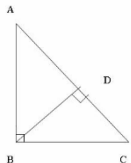
75 x 1 = 75

- 1) Given two triangles ABC and DEF ,AG and DH are perpendiculars on BC and EF respectively  $\angle B = \angle E$  ,  $AB=5, DE=8$  .What is  $\frac{AG}{DH} = ?$   
(a)  $\frac{5}{8}$  (b)  $\frac{2}{5}$  (c)  $\frac{3}{5}$  (d)  $\frac{3}{8}$
- 2) Which of the following cannot be the sides a right triangle?  
(a) 400mm, 300 mm, 500mm (b) 9 cm, 15 cm, 12 cm (c) 2 cm, 1 cm,  $\sqrt{5}$  cm (d) 9 cm, 5 cm, 7cm
- 3) In a triangle ABC,  $AC= \sqrt{180}$  , $AB=6$  , $BC=12$  .What is  $\angle B = ?$   
(a)  $90^\circ$  (b)  $30^\circ$  (c)  $45^\circ$  (d)  $60^\circ$
- 4) From the given figure, find the unknown x.

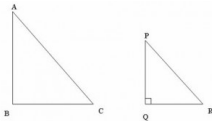


- (a) 12 (b) 225 (c) 10 (d) 144
- 5) Three squares are based on the sides of a right angled triangle. The area of the two smaller ones are 144 sq. cm and 256 sq. cm. What is the area of the third one?  
(a) 625 sq. cm (b) 361 sq. cm (c) 400 sq. cm (d) 900sq. cm
- 6) What is the diagonal length of a TV screen whose dimensions are 80 x 60 cm?  
(a) 10 (b) 100 (c) 20 (d) 100
- 7) Which of the following is a Pythagorean triplet?  
(a) (36,18,43) (b) (15,20,25) (c) (3,12,13) (d) (24,25,26)
- 8)  $QM \perp RP$  and  $PR^2 - PQ^2 = OR^2$  . If  $\angle QPM = 30^\circ$  , Then  $\angle MQR$  is

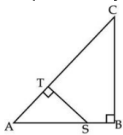


- (a)  $45^\circ$  (b)  $60^\circ$  (c)  $90^\circ$  (d)  $30^\circ$
- 9) 
- In the above figure,  $AB = c$ ,  $BC = a$ ,  $AC = b$ ,  $AD = y$ ,  $DB = p$ . Check which of the following options is correct?  
(a)  $cy=ap$  (b)  $ac=by$  (c)  $ay=cp$  (d)  $cy=ab$
- 10) In right triangle ABC right angled at B ,a line DE is drawn through the mid point D of AB and parallel to BC.If  $AB=9$  cm,  $BC=12$  cm.  $AE=?$   
(a) 13 cm (b) 10 cm (c) 8.5 cm (d) 7.5 cm

- 11) A boy is trying to catch fish sitting at a height of 12 m from the surface of the water. A big fish is at a horizontal distance of 5 m from him. What should be the length of his string to get the fish?  
(a) 10 (b) 13 (c) 7 (d) 15
- 12) Triangle PQR is an isosceles right triangle right angled at Q. If  $PR = \sqrt{50}$ . What is the value of each of the equal sides?  
(a)  $5\sqrt{2}$  (b) 5 (c) 2 (d)  $2\sqrt{5}$
- 13) Three numbers form a Pythagorean triplet. Two of them are 15 and 17 where 17 is the largest of them. The third number is  
(a) 8 (b) 12 (c) 13 (d) 5
- 14) The length of an altitude of an equilateral triangle of side  $a$  is  
(a)  $\frac{a}{2\sqrt{3}}$  (b)  $\frac{2a}{\sqrt{3}}$  (c)  $\frac{\sqrt{3}a}{2}$  (d)  $\frac{\sqrt{3}}{2a}$
- 15) Two friends A and B start from the same point in the Eastern and Northern directions at the same time. How far are they from each other when A has travelled 5 km and B has travelled 12 km. distance?  
(a) 8 km (b) 17 km (c) 10 km (d) 13 km
- 16) Two similar right triangles ABC and PQR are as shown in the figure. If  $AB = \sqrt{3}$ ,  $PQ = \sqrt{3}/2$ ,  $BC = 1$ . Find  $PR = ?$



- (a) 2 (b) 1 (c)  $2\sqrt{3}$  (d) 4
- 17) In figure,  $\triangle ABC \sim \triangle PQR$
- 
- (a)  $2 + \sqrt{3}$  (b)  $4 + \sqrt{3}$  (c)  $3 + 4\sqrt{3}$  (d)  $4 + 3\sqrt{3}$
- 18) In the given figure, T and B are right angles. If the lengths of AT, BC and AS (in centimeters) are 15, 16 and 17 respectively, then the length of TC (in centimeters) is:

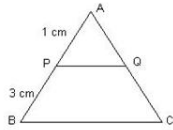


- (a) 18 (b) 12 (c) 19 (d) 16
- 19) In the given figure  $AD = 2$  cm,  $DB = 5$  cm,  $AC = 21$  cm and  $DE \parallel BC$ . Find  $AE = ?$   
(a) 6 (b) 5 (c) 8 (d) 7
- 20) In an equilateral triangle ABC, if  $AD \perp BC$ . Then  
(a)  $3AB^2 = 4AD^2$  (b)  $2AB^2 = 3AD^2$  (c)  $3AB^2 = 2AD^2$  (d)  $4AB^2 = 3AD^2$
- 21) In two triangles ABC and PQR, Given that  $\angle A = \angle R$  and  $\angle B = \angle Q$ , which of the following is true?  
(a)  $\triangle ABC \sim \triangle QRP$  (b)  $\triangle ABC \sim \triangle PQR$  (c)  $\triangle ABC \sim \triangle PRQ$  (d)  $\triangle ABC \sim \triangle RQP$
- 22) Triangles ABC, DEF are similar,  $\angle A = 75^\circ$ ,  $\angle B = 85^\circ$  so  $\angle F = ?$   
(a)  $20^\circ$  (b)  $30^\circ$  (c)  $10^\circ$  (d)  $35^\circ$
- 23) A vertical stick 30 m long casts a shadow 15 m long on the ground. At the same time, a tower casts a shadow 75 m long on the ground. The height of the tower is:  
(a) 200 m (b) 150 m (c) 25 m (d) 100 m

- 24) Given two triangles ABC and PQR such that,  $AB = 2\text{ cm}$ ,  $PQ = 3\text{ cm}$ ,  $\angle B = \angle Q$ ,  $BC = 5\text{ cm}$ ,  $QR = 7.5\text{ cm}$ . AG and PS are medians. Find  $\frac{AG}{PS} = ?$

(a)  $\frac{2}{5}$  (b)  $\frac{1}{5}$  (c)  $\frac{4}{5}$  (d)  $\frac{2}{3}$

- 25) In the adjoining figure,  $PQ \parallel BC$ , then what could be the values of AQ & QC respectively



(a) 3 cm and 6 cm (b) 2 cm and 6 cm (c) 3 cm and 4 cm (d) 1 cm and 6 cm

- 26) In given figure,  $DE \parallel BC$ , if  $AB = 7.6\text{ cm}$ ,  $AD = 1.9\text{ cm}$ , then  $AE : EC$  is :

(a) 1:4 (b) 4:1 (c) 1:3 (d) 3:1

- 27) In right triangle ABC, right angled at A, a perpendicular is dropped from A to BC, meeting BC at D. Then which of the following is true?

(a)  $\triangle ADC \sim \triangle ABD$  (b)  $\triangle DCA \sim \triangle DAB$  (c)  $\triangle DAC \sim \triangle DAB$  (d)  $\triangle DAC \sim \triangle DAB$

- 28)  $\triangle ABC \sim \triangle PQR$ ,  $\angle B = 50^\circ$  and  $\angle C = 70^\circ$  then  $\angle P$  is equal to

(a)  $50^\circ$  (b)  $60^\circ$  (c)  $40^\circ$  (d)  $70^\circ$

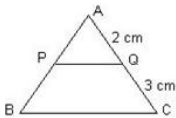
- 29)



The above two pictures of Gateway of India are:

(a) neither similar nor congruent (b) similar (c) dissimilar (d) congruent

- 30) In the adjoining figure,  $PQ \parallel BC$ , then what could be the values of AP & PB respectively



(a) 1 cm and 3 cm (b) 3 cm and 6 cm (c) 2 cm and 4 cm (d) 4 cm and 6 cm

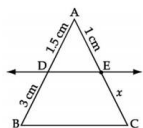
- 31) In triangle ABC, D and E are points on AB and AC such that  $DE \parallel BC$ . If  $AD = 4x-3$ ,  $AE = 8x-7$ ,  $BD = 3x-1$  and  $CE = 5x-3$ , find the value of x

(a) 1 (b)  $\frac{1}{2}$  (c)  $\frac{1}{2}, -1$  (d)  $1, -\frac{1}{2}$

- 32) Two congruent triangles are actually similar triangles with the ratio of corresponding sides as.

(a) 1:2 (b) 1:1 (c) 1:3 (d) 2:1

- 33) In figure,  $DE \parallel BC$ , then x equals to :



(a) 1.4 cm (b) 2 cm (c) 4 cm (d) 2.5 cm

- 34) Which geometric figures are always similar?

(a) Circles (b) Circles and all regular polygons (c) Circles and triangles (d) Regular polygons

- 35) In  $\triangle ABC$  and  $\triangle DEF$ ,  $\angle B = \angle E$ ,  $\angle F = \angle C$  and  $AB = 3DE$  then, the two triangles are

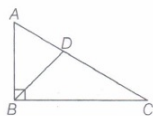
(a) congruent but not similar (b) similar but not congruent (c) neither congruent nor similar  
(d) congruent as well as similar

- 36) If  $\triangle ABC \sim \triangle DFE$ ,  $\angle A = 30^\circ$ ,  $\angle C = 50^\circ$ ,  $AB = 5$  cm,  $AC = 8$  cm and  $DF = 7.5$  cm. Then, which of the following is true?  
 (a)  $DE = 12$  cm,  $\angle F = 50^\circ$  (b)  $DE = 12$  cm,  $\angle F = 100^\circ$  (c)  $EF = 12$  cm,  $\angle D = 100^\circ$  (d)  $EF = 12$  cm,  $\angle D = 30^\circ$
- 37) If in  $\triangle ABC$  and  $\triangle DEF$ ,  $\frac{AB}{DF} = \frac{AC}{DE}$  then they will be similar, when  
 (a)  $\angle B = \angle E$  (b)  $\angle A = \angle D$  (c)  $\angle B = \angle D$  (d)  $\angle A = \angle F$
- 38) If  $ABC \sim QRP$   $\frac{ar(\triangle ABC)}{ar(\triangle PQR)} = \frac{9}{4}$ ,  $AB = 18$  cm and  $BC = 15$  cm then  $PR$  is equal to  
 (a) 10 cm (b) 12 cm (c)  $\frac{20}{3}$  cm (d) 8 cm
- 39) If  $S$  is a point on side  $PQ$  of a  $\triangle PQR$  such that  $PS = QS = RS$ , then  
 (a)  $PR \cdot QR = RS^2$  (b)  $QS^2 + RS^2 = QR^2$  (c)  $PP^2 + QP^2 = PQ^2$  (d)  $PS^2 + RS^2 = PR^2$
- 40)  $ABC$  and  $BDE$  are two equilateral triangles such that  $D$  is the mid-point of  $BC$ . Ratio of the areas of triangles  $ABC$  and  $BDE$  is  
 (a) 2 : 1 (b) 1 : 2 (c) 4 : 1 (d) 1 : 4
- 41) Sides of two similar triangles are in the ratio 4 : 9. Areas of these triangles are in the ratio  
 (a) 2 : 3 (b) 4 : 9 (c) 81 : 16 (d) 16 : 81
- 42) Tick the correct answer and justify : In  $\triangle ABC$ ,  $AB = 6\sqrt{3}$  cm,  $AC = 12$  cm and  $BC = 6$  cm. The angle  $B$  is :  
 (a)  $120^\circ$  (b)  $60^\circ$  (c)  $90^\circ$  (d)  $45^\circ$
- 43) If in two  $\triangle ABC$  and  $\triangle PQR$   $\frac{AB}{QR} = \frac{BC}{PR} = \frac{CA}{PQ}$ , then  
 (a)  $\triangle PQR \sim \triangle CAB$  (b)  $\triangle PQR \sim \triangle ABC$  (c)  $\triangle CBA \sim \triangle PQR$  (d)  $\triangle BCA \sim \triangle PQR$
- 44) It is given that,  $\triangle ABC \sim \triangle EDF$  such that  $AB = 5$  cm,  $AC = 7$  cm,  $DF = 15$  cm and  $DE = 12$  cm, then the sum of the remaining sides of the triangles is  
 (a) 23.05 cm (b) 16.8 cm (c) 6.25 cm (d) 24 cm
- 45) If in  $\triangle ABC$  and  $\triangle DEF$ ,  $\frac{AB}{DE} = \frac{BC}{FD}$  then they will be similar, when  
 (a)  $\angle B = \angle E$  (b)  $\angle A = \angle D$  (c)  $\angle B = \angle D$  (d)  $\angle A = \angle F$
- 46) In  $\triangle ABC$  and  $\triangle DEF$ ,  $\angle B = \angle E$ ,  $\angle F = \angle C$  and  $AB = 3DE$ . Then, the two triangles are  
 (a) congruent but not similar (b) similar but not congruent (c) neither congruent nor similar  
 (d) congruent as well as similar
- 47) If the lengths of the diagonals of rhombus are 16 cm and 12 cm. Then, the length of the sides of the rhombus is  
 (a) 9 cm (b) 10 cm (c) 8 cm (d) 20 cm
- 48) Two poles of height 6 m and 11 m stand vertically upright on a plane ground. If the distance between their foot is 12 m, then distance between their tops is  
 (a) 12 m (b) 14 m (c) 13 m (d) 11 m
- 49) If  $\triangle ABC \sim \triangle POR$  with  $\frac{BC}{OR} = \frac{1}{3}$  then  $\frac{ar(\triangle PRQ)}{ar(\triangle BCA)}$  is equal to  
 (a) 9 (b) 3 (c)  $\frac{1}{3}$  (d)  $\frac{1}{9}$
- 50) Sides of two similar triangles are in the ratio 4 : 9. Areas of these triangles are in the ratio  
 (a) 2 : 3 (b) 4 : 9 (c) 81 : 16 (d) 16 : 81
- 51) In a right angled  $\triangle ABC$  right angled at  $B$  if  $P$  and  $Q$  are points on the sides  $AB$  and  $BC$  respectively, then  
 (a)  $AQ^2 + CP^2 = 2(AC^2 + PQ^2)$  (b)  $2(AQ^2 + CP^2) = AC^2 + PQ^2$  (c)  $AQ^2 + CP^2 = AC^2 + PQ^2$   
 (d)  $AQ + CP = \frac{1}{2}(AC + PQ)$

- 52) The area of a right angled triangle is 40 sq cm and its perimeter is 40 cm. The length of its hypotenuse is

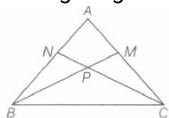
(a) 16 cm (b) 18 cm (c) 17 cm (d) data insufficient

- 53) In the figure given below,  $\angle ABC = 90^\circ$ ,  $AD = 15$  cm and  $DC = 20$  cm, If  $BD$  is the bisector of  $\angle ABC$ , What is the perimeter of the triangle  $ABC$ ?



(a) 74 cm (b) 84 cm (c) 91 cm (d) 105 cm

- 54) In the figure given below,  $AM : MC = 3 : 4$ ,  $BP : PM = 3 : 2$  and  $BN = 12$  cm. Then  $AN$  equals to

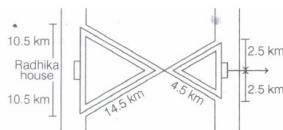


(a) 10 cm (b) 12 cm (c) 14 cm (d) 16 cm

- 55) Diagonal  $AC$  of a rectangle  $ABCD$  is produced to the point  $E$  such that  $AC : CE = 2 : 1$ ,  $AB = 8$  cm and  $BC = 6$  m. The length of  $DE$  is

(a)  $2\sqrt{19}$  cm (b) 15 cm (c)  $3\sqrt{17}$  cm (d) 13 cm

- 56) Radhika wants to visit her friend who recently moved to a new house. The road map between Radhika's home and her friend's as well as the distance known to Radhika are as shown in the figure given below:



To reach the friend's house, the shortest distance which Radhika has to travel, is

(a) 30.95 km (b) 32.5 km (c) 28.5 km (d) 35.35 km

- 57)  $O$  is the point of intersection of the diagonals  $AC$  and  $BD$  of a trapezium  $ABCD$  with  $AB \parallel DC$ . Through  $O$ , a line segment  $PQ$  is drawn parallel to  $AB$  meeting  $AD$  in  $P$  and  $BC$  in  $Q$ , then  $OP =$

(a)  $OP = OQ$  (b)  $OP = 2 OQ$  (c)  $OQ = 2 OP$  (d)  $OP = \frac{1}{3} OQ$

- 58) The area of the semi-circle drawn on the hypotenuse of a right angled triangle is equal

(a) sum of the areas of the semi-circles drawn on the other two sides of the triangle.  
 (b) difference of the areas of semi-circles drawn on the other two sides of the triangle  
 (c) product of the areas of semi-circles drawn on the other two sides of the triangle (d) None of these

- 59) In a  $\triangle PQR$ ,  $L$  and  $M$  are two points on base  $QR$ , such that  $L$ .  $\angle PQ = \angle QRP$  and  $\angle RPM = \angle RQP$ . Then, which of the following is/are true:

(i)  $\triangle PQL \sim \triangle RPM$

(ii)  $QL \times RM = PL \times PM$

(iii)  $PQ^2 = QR \times QL$

(a) Both (i) and (ii) (b) Both (ii) and (iii) (c) Both (i) and (iii) (d) All the three

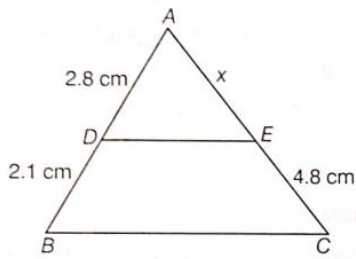
- 60)  $\triangle ABC$  is right angled at  $A$  with  $AB = 6$  cm,  $BC = 10$  cm. A circle with centre  $O$  has been inscribed inside the triangle. The radius of the in circle is

(a) 4 cm (b) 3 cm (c) 2 cm (d) 1 cm

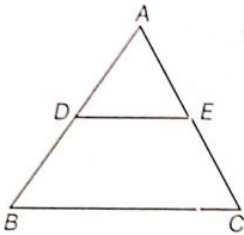
- 61) A 5 m long ladder is placed leaning towards a vertical wall such that it reaches the wall at a point 4 m high. If the foot of the ladder is moved 1.6 m towards the wall, then the distance by which the top of the ladder would slide upwards on the wall is

(a) 0.6 cm (b) 0.2 cm (c) 0.4 cm (d) 0.8 cm

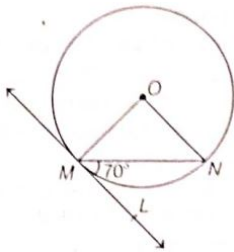
- 62) If in the given figure,  $DE \parallel BC$ .  
If  $AD = 2.8$  cm,  $DB = 2.1$  cm and  $EC = 4.8$  cm, then the value of  $x$  is



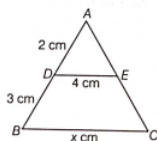
- (a) 3.6 cm (b) 2.4 cm (c) 6.4 cm (d) 4.8 cm
- 63) In a right angled  $\triangle ABC$ ,  $\angle A = 90^\circ$  and  $AB = AC$ . The value of  $\sin C$  is  
(a) 0 (b)  $\frac{\sqrt{3}}{2}$  (c)  $\frac{1}{2}$  (d)  $\frac{1}{\sqrt{2}}$
- 64) If the diagonals of a quadrilateral divide each other proportionally, then it is a  
(a) parallelogram (b) rectangle (c) square (d) trapezium
- 65) In  $\triangle ABC$ ,  $DE \parallel BC$  (as shown in the figure). If  $AD = 2$  cm,  $BD = 3$  cm and  $BC = 7.5$  cm, then the length of  $DE$  (in cm) is



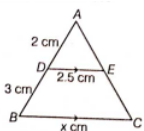
- (a) 2.5 (b) 3 (c) 5 (d) 6
- 66) In the given figure,  $O$  is the centre of the circle,  $MN$  is the chord and the tangent  $ML$  at point  $M$  makes an angle of  $70^\circ$  with  $MN$ . The measure of  $\angle MON$  is



- (a)  $120^\circ$  (b)  $140^\circ$  (c)  $70^\circ$  (d)  $90^\circ$
- 67)  $\triangle ABC \sim \triangle DEF$  and their perimeters are 32 cm and 24 cm, respectively. If  $AB = 10$  cm, then  $DE$  equals  
(a) 8 cm (b) 7.5 cm (c) 15 cm (d)  $5\sqrt{3}$  cm
- 68) In the given figure,  $DE \parallel BC$ . The value of  $x$  is

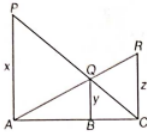


- (a) 6 (b) 12.5 (c) 8 (d) 10
- 69) In the given figure,  $AD = 2$  cm,  $DB = 3$  cm,  $DE = 2.5$  cm and  $DE \parallel BC$ . The value of  $x$  is

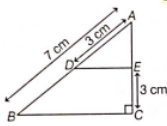


- (a) 6 (b) 3.75 cm (c) 6.25 cm (d) 7.5 cm

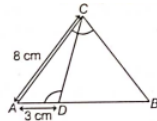
- 70) In  $\triangle ABC$  and  $\triangle DEF$ ,  $\frac{AB}{DE} = \frac{BC}{EF}$  Which of the following makes the two triangles similar?  
 (a)  $\angle A = \angle D$  (b)  $\angle B = \angle D$  (c)  $\angle B = \angle P$  (d)  $\angle A = \angle F$
- 71) If in  $\triangle ABC$  and  $\triangle PQR$ , we have  $\frac{AB}{QR} = \frac{BC}{PR} = \frac{CA}{PQ}$  then  
 (a)  $\triangle PQR \sim \triangle CAB$  (b)  $\triangle PQR \sim \triangle ABC$  (c)  $\triangle CBA \sim \triangle PQR$   
 (d)  $\triangle BCA \sim \triangle PQR$
- 72) In two  $\triangle PQR$  and  $\triangle ABC$ , it is given that  $\frac{AB}{BC} = \frac{PQ}{PR}$ . For these two triangles to be similar, which of the following should be true?  
 (a)  $\angle A = \angle P$  (b)  $\angle B = \angle Q$  (c)  $\angle B = \angle E$  (d)  $\angle A = \angle F$
- 73) In the given figure, PA QB and RC are each perpendicular to AC. If  $x = 8$  cm and  $z = 6$  cm, then  $y$  is equal to



- (a)  $56/7$  cm (b)  $7/56$  cm (c)  $25/7$  cm (d)  $24/7$  cm
- 74) In the given figure,  $DE \parallel BC$ . If  $AD = 3$  cm,  $AB = 7$  cm and  $EC = 3$  cm, then the length of  $AE$  is



- (a) 2 cm (b) 2.25 cm (c) 3.5 cm (d) 4 cm
- 75) In the given figure,  $\angle ACB = \angle CDA$ ,  $AC = 8$  cm and  $AD = 3$  cm, then  $BD$  is

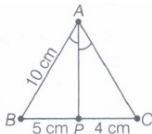


- (a)  $22/3$  cm (b)  $26/3$  cm (c)  $55/3$  cm (d)  $64/3$  cm

Fill up / 1 Marks

7 x 1 = 7

- 76) Two triangles are similar, if their corresponding angles are ..... and
- 77) Two triangles are similar, if their corresponding sides are in the same .....
- 78) If a line divides any two sides of a triangle in the same ratio, then the line is ..... to the third side.
- 79) If the diagonals of a quadrilateral divide each other proportionally, then it is a .....
- 80) If the areas of two similar triangles are ..... then they are congruent.
- 81) Pythagoras theorem state that, in a right triangle the ..... of the hypotenuse is equal to the ..... of the squares of the other two sides.
- 82) In the given figure, if AP is bisector of  $\angle A$ , then length of AC is.



True or False

6 x 1 = 6

- 83) If corresponding angles of two triangles are equal, then they are known as equiangular triangles.  
 (a) True (b) False
- 84) If two angles of one triangle are respectively equal to two angles of another triangle, then the two triangles are congruent.  
 (a) True (b) False

- 85) The ratio of the perimeters of two similar triangles is the same as the ratio of their corresponding sides.  
(a) True (b) False
- 86) If one angle of a triangle is equal to one angle of the other triangle and any two sides are proportional, then the two triangles are similar.  
(a) True (b) False
- 87) The hypotenuse of a right triangles is 6 m more than the twice of the shortest side. If the third side is 2 m less than the hypotenuse, then the perimeter of the triangle is 80 cm.  
(a) True (b) False
- 88) If two triangles are similar then the ratio of their corresponding sides is the same as the ratio of the corresponding medians.  
(a) True (b) False

Match the following

4 x 1 = 4

89) In  $\Delta ABC$ ,  $DE \parallel BC$  and  $AE : EC = 5 : 8$  then  $AD : DB$  (1) 9 cm

90) If  $\Delta ABC \sim \Delta DEF$  such that  $BC = 5$  cm,  $EF = 4$  cm and area of  $\Delta ABC = 100$  cm<sup>2</sup> then area of  $\Delta DEF$  is .....cm<sup>2</sup>. (2) 5 : 8

91) In right angled  $\Delta ABC$ ,  $AC = b$  cm,  $BC = a$  cm,  $AB = 6$  cm and  $\angle C = 90^\circ$ ,  $CD \perp AB$  and  $CD = 4$  cm. Then,  $ab$  is ..... cm. (3) 24

92) In  $\Delta ABC$ ,  $AD$  is bisector of  $\angle A$ , if  $BD = 4$  cm,  $DC = 6$  cm and  $AB = 6$  cm then  $AC$  is ..... cm. (4) 64

Assertion and reason

4 x 1 = 4

93) **Assertion:**  $\Delta ABC \sim \Delta POR$  such that  $ar(\Delta ABC) = 36$  cm<sup>2</sup> and  $ar(\Delta POR) = 49$  cm<sup>2</sup>. If  $AB = 6$  cm, then  $PQ = 10$  cm.

**Reason:** If  $\Delta ABC \sim \Delta DEP$ , then  $\frac{ar(\Delta ABC)}{ar(\Delta DEF)} = \frac{AB^2}{DE^2} = \frac{BC^2}{EF^2} = \frac{AC^2}{DF^2}$

**Codes:**

- (a) If both Assertion and Reason are correct and Reason is the correct explanation of Assertion.  
(b) If both Assertion and Reason are correct, but Reason is not the correct explanation of Assertion.  
(c) If Assertion is correct but Reason is incorrect.  
(d) If Assertion is incorrect but Reason is correct.

94) **Assertion:** In a rhombus of side 15 cm, one of the diagonals is 20 cm long. The length of the second diagonal is  $10\sqrt{6}$  cm.

**Reason:** The sum of the squares of the sides of a rhombus is equal to the sum of the squares of its diagonals.

**Codes:**

- (a) If both Assertion and Reason are correct and Reason is the correct explanation of Assertion.  
(b) If both Assertion and Reason are correct, but Reason is not the correct explanation of Assertion.  
(c) If Assertion is correct but Reason is incorrect.  
(d) If Assertion is incorrect but Reason is correct.

95) **Assertion:** In  $\Delta ABC$ ,  $\angle B = 90^\circ$  and  $BD \perp AC$ . If  $AD = 4$  cm and  $CD = 5$  cm then  $BD$  is  $2\sqrt{5}$  cm.

**Reason:** The ratio of the areas of two similar triangles are equal to the ratio of squares of any two corresponding sides.

**Codes:**

- (a) If both Assertion and Reason are correct and Reason is the correct explanation of Assertion.  
(b) If both Assertion and Reason are correct, but Reason is not the correct explanation of Assertion.  
(c) If Assertion is correct but Reason is incorrect.  
(d) If Assertion is incorrect but Reason is correct.

96) **Assertion:** In a quadrilateral  $ABCD$ ,  $\angle B = 90^\circ$ . If  $AD^2 = AB^2 + BC^2 + CD^2$ , then  $\angle ACD = 90^\circ$ .

**Reason:** In a triangle, if the square of one side is equal to the sum of the squares of the other two sides, then the angle opposite to the first side is a right angle.

**Codes:**

- (a) If both Assertion and Reason are correct and Reason is the correct explanation of Assertion.  
(b) If both Assertion and Reason are correct, but Reason is not the correct explanation of Assertion.  
(c) If Assertion is correct but Reason is incorrect.  
(d) If Assertion is incorrect but Reason is correct.

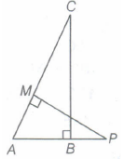


- 97) Fill in the blanks using the correct word given in brackets.
- (i) All circles are ----- (congruent, similar)
  - (ii) All squares are ----- (similar, congruent)
  - (iii) All ----- triangles are similar. (isosceles, equilateral)
  - (iv) Two polygons of the same number of sides are similar, if (a) their corresponding angles are ----- and (b) their corresponding sides are ----- (equal, proportional)

- 98) Give two different examples of pair of
- (i) similar figures
  - (ii) non-similar figures

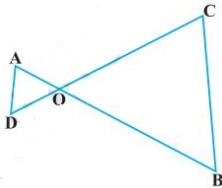
- 99) E and F are points on the sides PQ and PR respectively of a  $\Delta PQR$ . For the following case, state whether  $EF \parallel QR$ .  $PE = 3.9$  cm,  $EQ = 3$  cm,  $PF = 3.6$  cm and  $FR = 2.4$  cm

- 100) In the given figure, ABC and AMP are two right angled triangles, right angled at B and M, respectively. Prove that  $\triangle ABC \sim \triangle AMP$

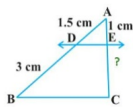


- 101) ABCD is a trapezium in which  $AB \parallel DC$  and its diagonals intersect each other at the point O. Show that  $\frac{AO}{BO} = \frac{CO}{DO}$ .

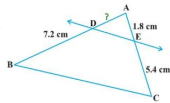
- 102) In the given figure,  $OA \cdot OB = OC \cdot OD$ . Show that  $\angle A = \angle C$  and  $\angle B = \angle D$ .



- 103) See the given Figure.  $DE \parallel BC$ . Find EC



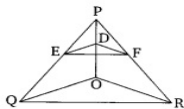
- 104) See the given Figure.  $DE \parallel BC$ . Find AD



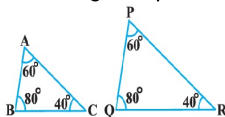
- 105) E and F are points on the sides PQ and PR respectively of a  $\Delta PQR$ . For the following case, state whether  $EF \parallel QR$ .  $PE = 4$  cm,  $QE = 4.5$  cm,  $PF = 8$  cm and  $RF = 9$  cm

- 106) E and F are points on the sides PQ and PR respectively of a  $\Delta PQR$ . For the following case, state whether  $EF \parallel QR$ .  $PQ = 1.28$  cm,  $PR = 2.56$  cm,  $PE = 0.18$  cm and  $PF = 0.36$  cm

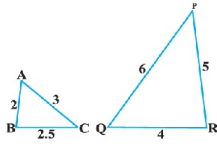
- 107) In the given figure,  $DE \parallel OQ$  and  $DF \parallel OR$ . Show that  $EF \parallel QR$ .



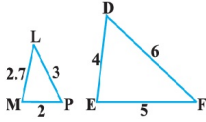
- 108) State which pair of triangles in the following figure are similar? Write the similarity criterion used by you for answering the question and also write the pairs of similar triangles in the symbolic form:



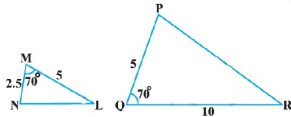
- 109) State which pair of triangles in the given figure are similar? Write the similarity criterion used by you for answering the question and also write the pairs of similar triangles in the symbolic form:



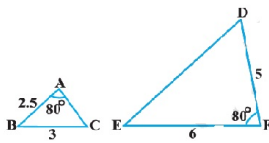
- 110) State which pair of triangles in the following figure are similar? Write the similarity criterion used by you for answering the question and also write the pairs of similar triangles in the symbolic form:



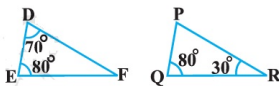
- 111) State which pair of triangles in the following figure are similar? Write the similarity criterion used by you for answering the question and also write the pairs of similar triangles in the symbolic form:



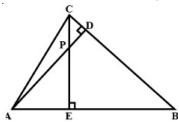
- 112) State which pair of triangles in the following figure are similar? Write the similarity criterion used by you for answering the question and also write the pairs of similar triangles in the symbolic form:



- 113) State which pair of triangles in the following figure are similar? Write the similarity criterion used by you for answering the question and also write the pairs of similar triangles in the symbolic form:

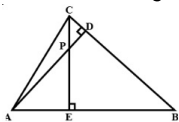


- 114) In the following figure, altitudes AD and CE of  $\triangle ABC$  intersect each other at the point P. Show that:



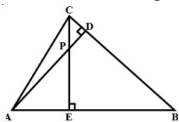
$$\triangle AEP \sim \triangle CDP$$

- 115) In the following figure, altitudes AD and CE of  $\triangle ABC$  intersect each other at the point P. Show that:



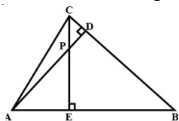
$$\triangle ABD \sim \triangle CBE$$

- 116) In the following figure, altitudes AD and CE of  $\triangle ABC$  intersect each other at the point P. Show that:



$$\triangle AEP \sim \triangle ADB$$

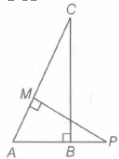
- 117) In the following figure, altitudes AD and CE of  $\triangle ABC$  intersect each other at the point P. Show that:



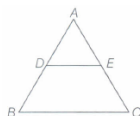
$$\triangle PDC \sim \triangle BEC$$

- 118) In the given figure, ABC and AMP are two right angled triangles, right angled at B and M, respectively. Prove that

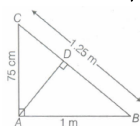
$$\frac{CA}{PA} = \frac{BC}{MP}$$



- 119) If the areas of two similar triangles are respectively  $81 \text{ cm}^2$  and  $49 \text{ cm}^2$ . Find the ratio of their corresponding medians.
- 120) If the sides of a triangle are 3 cm, 4 cm and 6 cm long, then determine whether the triangle is a right angled triangle.
- 121) Find the third side of a right angled triangle whose hypotenuse is of length  $p$  cm, one side of length  $q$  cm and  $p - q = 1$ .
- 122) Sides of triangles are given below. Determine which of them are right angled triangles? In case of a right angled triangle, write the length of its hypotenuse.  
7 cm, 24 cm and 25 cm
- 123) The perimeters of two similar  $\triangle ABC$  and  $\triangle PQR$  are respectively 18 cm and 12 cm. If  $PQ = 5$  cm, then find  $AB$ .
- 124) The lengths of the diagonals of a rhombus are 30 cm and 40 cm. Find the side of the rhombus.
- 125) Let  $\triangle ABC \sim \triangle DEF$  and their areas be  $64 \text{ cm}^2$  and  $121 \text{ cm}^2$ , respectively. If  $EF = 15.4$  cm, find the value of  $BC$ .
- 126) The areas of two similar triangles are  $121 \text{ cm}^2$  and  $64 \text{ cm}^2$ , respectively. If the median of the first triangle is 12.1 cm, find the corresponding median of the other.
- 127) In  $\triangle ABC$  and  $\triangle DEF$ , if  $\frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF} = \frac{5}{9}$ , find the ratio of  $ar(\triangle ABC) : ar(\triangle DEF)$
- 128) ABC is a triangle in which  $\angle A = 90^\circ$ ,  $AN \perp BC$ ,  $BC = 12$  cm and  $AC = 5$  cm. Find the ratio of the areas of  $\triangle ANC$  and  $\triangle ABC$ .
- 129) Is the triangle with sides 13 cm, 16 cm and 18 cm a right triangle? Give reason.
- 130) In a right angled triangle, if hypotenuse is 20 cm and the ratio of other two sides is 4 : 3, find the other sides.
- 131) A boy goes 24 m due East and 7 m due South. How far is he from the starting point?
- 132) An equilateral triangle is inscribed in a circle of radius 6 cm. Find its side.
- 133) In the given figure,  $DE \parallel BC$ .  $DE = 4$  cm,  $BC = 8$  cm, area of  $\triangle ADE = 25 \text{ sq.cm}$ . Find the area of  $\triangle ABC$

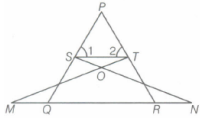


- 134) PQR is an equilateral triangle with each side of length  $2p$ . If  $PS \perp QR$ , then find the value of  $PS$ .
- 135) In the given figure,  $\angle CAB = 90^\circ$ ,  $AD \perp BC$  and  $\triangle BDA \sim \triangle BAC$ . If  $AC = 75$  cm,  $AB = 1$  m and  $BC = 1.25$  m, then find the value of  $AD$ .



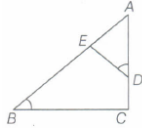
- 136) A vertical stick 1 m long casts a shadow 80 cm long. At the same time a tower casts a shadow 30 m long. Determine the height of the tower.
- 137) ABCD is a trapezium in which  $AB \parallel DC$ . P and Q are points on sides AD and BC respectively such that  $PQ \parallel AB$ . If  $PD = 18$  cm,  $BQ = 35$  cm and  $QC = 15$  cm, find the value of  $AD$ .

- 138) In the given figure, if  $\angle 1 = \angle 2$  and  $\triangle NSQ \cong \triangle MTR$ , prove that  $\triangle PTS \sim \triangle PRQ$

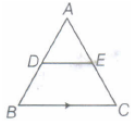


- 139) The diagonals of a rhombus are 30 cm and 40 cm. Find each of the rhombus.

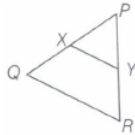
- 140) In  $\triangle ABC$ , if  $\angle ADE = \angle B$ , then prove that  $\triangle ADE \sim \triangle ABC$ . Also, if  $AD = 7.6$  cm,  $AE = 7.2$  cm,  $BE = 4.2$  cm and  $BC = 8.4$  cm, find  $DE$ .



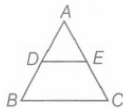
- 141) In  $\triangle ABC$ ,  $DE \parallel BC$ , so that  $AD = (7x - 4)$  cm,  $AE = (5x - 2)$  cm,  $DB = (3x + 4)$  cm and  $EC = 3x$  cm. Then, find the value of  $x$ .



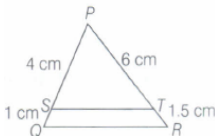
- 142) In the given figure,  $XY \parallel QR$ ,  $PQ / XQ = 7 / 3$  and  $PR = 6.3$  cm. Find the value of  $YR$ .



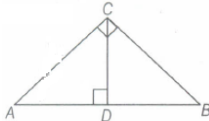
- 143) In  $\triangle ABC$  shown below,  $DE \parallel BC$ . If  $BC = 8$  cm,  $DE = 6$  cm and area of  $\triangle ADE = 45$  cm<sup>2</sup>, what is the area of  $\triangle ABC$ ?



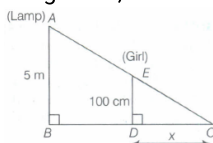
- 144) In the given figure,  $PS, SQ, PT$  and  $TR$  are 4 cm, 1 cm, 6 cm and 1.5 cm respectively. Prove that  $ST \parallel QR$ . Also, find  $\frac{ar(\triangle PST)}{ar(\text{trapezium } QRTS)}$



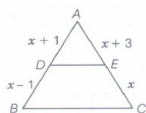
- 145) In the given figure,  $\triangle ACB = 90^\circ$  and  $CD \perp AB$ . Prove that  $\frac{BC^2}{AC^2} = \frac{BD}{AD}$ .



- 146) A girl of height 100 cm is walking away from the base of a lamppost at a speed of 1.9 m/s. If the lamp is 5 m above the ground, find the length of her shadow after 4s.

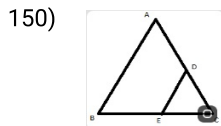


- 147) In  $\triangle ABC$ ,  $DE \parallel BC$ , find the value of  $x$ .



- 148) In the given figure, if  $\angle A = 90^\circ$ ,  $\angle B = 90^\circ$ ,  $OB = 4.5$  cm,  $OA = 6$  cm and  $AP = 4$  cm, then find the  $QB$ .

- 149) In  $\triangle ABC$ , if  $X$  and  $Y$  are points on  $AB$  and  $AC$  respectively such that  $\frac{AX}{XB} = \frac{3}{4}$ ,  $AY=5$  and  $YC=9$ , then state whether  $XY$  and  $BC$  parallel or not.

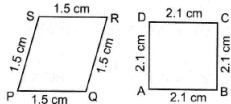


In the figure of  $\triangle ABC$ , the points  $D$  and  $E$  are on the sides  $CA$ ,  $CB$  respectively such that  $DE \parallel AB$ ,  $AD=2x$ ,  $DC=x+3$ ,  $BE=2x-1$  and  $CE=x$ , then find the value of  $x$ .

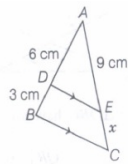
- 151) Are two triangles with equal corresponding sides always similar? Two triangles having corresponding sides equal are similar.
- 152) If ratio of corresponding sides of two similar triangles is  $5 : 6$ , then find ratio of their areas.
- 153)  $ABCD$  is a trapezium such that  $\frac{AO}{OC} = \frac{BO}{OD} = \frac{1}{2}$ ,  $AB \parallel DC$  and  $AB=3$  cm. If the diagonals  $AC$  and  $BD$  intersect at  $O$  such that then calculate  $DC$ .
- 154) In given figure  $DE \parallel BC$ . If  $AD=3$  cm,  $DB=4$  cm and  $AE=6$  cm, then find  $EC$ .
- 155) In the given figure, if  $DE \parallel BC$ , then calculate  $x$ .
- 156) In the figure,  $PQ$  is parallel to  $MN$ . If  $\frac{K}{PM} = \frac{4}{13}$  and  $KN=20.4$  cm, then find  $KQ$ .
- 157) If triangle  $ABC$  is similar to triangle  $DEF$  such that  $2AB = DE$  and  $BC = 8$  cm, then find  $EF$ .
- 158) In an equilateral triangle of side  $3\sqrt{3}$  cm, find the length of the altitude.
- 159) In the given figure,  $\triangle ABC \sim \triangle PQR$ . Find the value of  $y + z$ .
- 160) In the given figure,  $OA = 3$  cm,  $OB = 4$  cm,  $\angle AOB = 90^\circ$ ,  $AC = 12$  cm and  $BC = 13$  cm, prove that  $\angle CAB = 90^\circ$ .
- 161) In an equilateral triangle of side  $24$  cm, find the length of the altitude.
- 162) In  $\triangle ABC$ ,  $AD \perp BC$ , such that  $AD^2 = BD \times CD$ . Prove that  $\triangle ABC$  is right angles at  $A$ .
- 163) Find the altitude of an equilateral triangle when each of its side is ' $a$ ' cm.
- 164) Let  $\triangle ABC \sim \triangle DEF$ . If  $ar(\triangle ABC)=100$  cm<sup>2</sup>,  $ar(\triangle DEF)=196$  cm<sup>2</sup> and  $DE=7$ , then find  $AB$ .
- 165) In the given figure,  $DE \parallel BC$ . If  $AD=1.5$  cm,  $BD=2AD$ , then find  $\frac{ar(\triangle ABC)}{ar(\text{trapezium } BCED)}$ .
- 166) In the given triangle  $PQR$ ,  $\angle OPR = 90^\circ$ ,  $PQ = 24$  cm and  $QR = 26$  cm and in  $\triangle PKR$ ,  $\angle PKR = 90^\circ$  and  $KR = 8$  cm, find  $PK$ .
- 167) The sides  $AB$  and  $AC$  and the perimeter  $P_1$  of  $\triangle ABC$  are respectively three times the corresponding sides  $DE$  and  $DF$  and the perimeter  $P_2$  of  $\triangle DEF$ . Are the two triangles similar? If yes, find  $\frac{ar(\triangle ABC)}{ar(\triangle DEF)}$ .
- 168) In the given figure,  $QA \perp AB$  and  $PB \perp AB$ . If  $AO=20$  cm,  $BO=12$  cm,  $PB=18$  cm, find  $AQ$ .
- 169) Given  $\triangle ABC \sim \triangle DEF$ , find  $\frac{ar(\triangle ABC)}{ar(\triangle DEF)}$ .
- 170) In the given figure,  $G$  is the mid-point of the side  $PQ$  of  $\triangle PQR$  and  $GH \parallel QR$ . Prove that  $H$  is the mid-point of the side  $PR$  of the triangle  $PQR$ .
- 171) In the given figure, in a triangle  $PQR$ ,  $ST \parallel QR$  and  $\frac{PS}{SQ} = \frac{3}{5}$  and  $PR=28$  cm, find  $PT$ .
- 172) In the given figure,  $\angle A = \angle B$  and  $AD=BE$ . Show that  $DE \parallel AB$ .
- 173) In a rectangle  $ABCD$ ,  $E$  is a point on  $AB$  such that  $AE = \frac{2}{3} AB$ . If  $AB=6$  km and  $AD=3$  km, then find  $DE$ .
- 174) In the given figure, find the measure of  $\angle X$ .
- 175) In the given figure,  $PQR$  is a triangle right angled at  $Q$  and  $XY \parallel QR$ . If  $PQ=6$  cm,  $PY=4$  cm and  $PX : XQ = 1 : 2$ . Calculate the lengths of  $PR$  and  $QR$ .

- 176) ABC is a right triangle right angled at C. Let  $BC=1$ ,  $CA=b$ ,  $AB=c$  and  $p$  be the length of perpendicular from C on AB. Prove that  $cp=ab$ .
- 177) In an equilateral triangle ABC, AD is drawn perpendicular to BC meeting BC in D. Prove that  $AD^2=3BD^2$ .
- 178) In the figure, PQRS is a trapezium in which  $PQ \parallel RS$ . On PQ and RS, there are points E and F respectively such that EF intersects SQ at G. Prove the  $EQ \times GS=GQ \times FS$ .
- 179) In the given figure, if  $AB \parallel DC$ , find the value of  $x$ .
- 180) In the given figure,  $CB \parallel QR$  and  $CA \parallel PR$ . If  $AQ = 12$  cm,  $AR = 20$  cm,  $PB = CQ = 15$  cm, calculate PC and BR.
- 181) A man steadily goes 10m due east and then 24 m due north.  
(i) Find the distance from the starting point.  
(ii) Which mathematical concept is used in this problem?

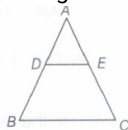
- 182) State whether the following quadrilaterals are similar or not:



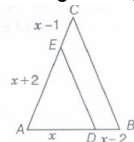
- 183) If  $\triangle ABC$  and  $\triangle DEF$  are two triangles such that  $\frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF} = \frac{4}{7}$ . Find  $\frac{\text{area } \triangle ABC}{\text{area } \triangle DEF}$ .
- 184) Sides of triangles are given below. Determine which of them are right triangles. In case of a right triangle, write the length of its hypotenuse.  
3 cm, 8 cm and 6 cm
- 185) Sides of triangles are given below. Determine which of them are right triangles. In case of a right triangle, write the length of its hypotenuse.  
50 cm, 80 cm, 100 cm
- 186) Sides of triangles are given below. Determine which of them are right triangles. In case of a right triangle, write the length of its hypotenuse.  
13 cm, 12 cm, 5 cm
- 187) In Figure, ABD is a triangle right angled at A and  $AC \perp BD$ . Show that  $AB^2 = BC \times BD$
- 188) In Figure ABD is a triangle right angled at A and  $AC \perp BD$ . Show that  $AC^2 = BC \times DC$
- 189) In Figure, ABD is a triangle right angled at A and  $AC \perp BD$ . Show that  $AD^2 = BD \times CD$
- 190) In an equilateral triangle ABC, D is a point on side BC such that  $BD = \frac{1}{3} BC$ . Prove that  $9 AD^2 = 7 AB^2$
- 191) In the given figure, find the value of  $x$ , if  $DE \parallel BC$ .



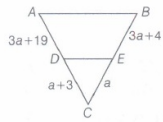
- 192) In  $\triangle ABC$  P and Q are points on AB and AC such that  $PQ \parallel BC$ . If  $AP = 4$  cm,  $AQ = 3$  cm and  $PB = 2$  cm, then find the value of AC.
- 193) In the given figure,  $DE \parallel BC$  if  $AD/DB = 3/5$  and  $AG = 4.8$  cm, then find the value of AE.



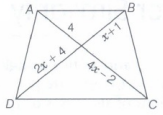
- 194) In the given figure,  $DE \parallel BC$ . If  $AD = x$ ,  $DB = x - 2$ ,  $AE = x + 2$  and  $EC = x - 1$ , then find the value of  $x$ .



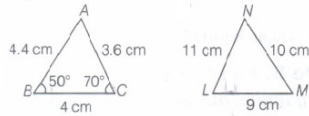
- 195) What value of  $a$  will make  $DE \parallel AB$  in the figure given below?



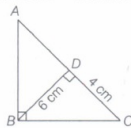
- 196) In the given figure, if  $AB \parallel CD$ , then find the value of  $x$ .



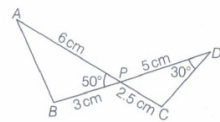
- 197) In the given figures, find  $\angle MLN$ .



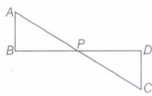
- 198) In the given figure  $\angle ABC = 90^\circ$  and  $BD \perp AC$ . If  $BD = 6$  cm and  $CD = 4$  cm, find the value of  $BC$ .



- 199) In the given figure, two line segments  $AC$  and  $BD$  intersect each other at the point  $P$  such that  $PA = 6$  cm,  $PB = 3$  cm,  $PC = 2.5$  cm,  $PD = 5$  cm,  $\angle APB = 50^\circ$  and  $\angle CDP = 30^\circ$ . Then find  $\angle PBA$



- 200) In the given figure, if  $\angle A = \angle C$ ,  $AB = 6$  cm,  $BP = 15$  cm,  $AP = 12$  cm and  $CP = 4$  cm, find the lengths of  $PD$  and  $CD$ .

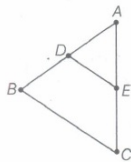


- 201) If two poles 5 m and 15 m high are 100 m apart, then find the height of the point of intersection of the line joining the top of each pole to the foot of the opposite pole.

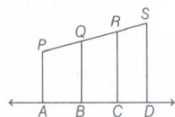
- 202) In  $\triangle ABC$ ,  $DE \parallel BC$ . If  $DE = \frac{2}{3} BC$  and area of  $\triangle ABC = 81 \text{ cm}^2$ , then find the area of  $\triangle DAE$ .

- 203) Given  $\triangle ABC \sim \triangle POR$ , if  $\frac{AB}{PQ} = \frac{1}{3}$ , then find  $\frac{\text{ar } \triangle ABC}{\text{ar } \triangle PQR}$

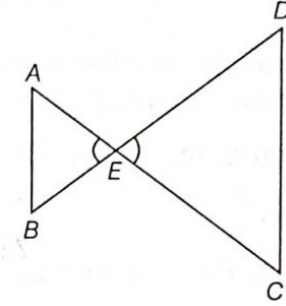
- 204) A park is in the form of a triangle as shown in the given figure. If we divide it into two parts: One triangle and one trapezium, taking as  $AD = 6$  cm,  $AB = 15$  cm,  $AE = 4$  cm and  $AC = 1$  cm. Are the line segment  $DE$  and  $BC$  parallel? Justify it.



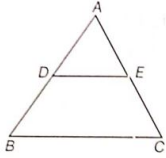
- 205) In the given figure  $PA$ ,  $QB$ ,  $RC$  and  $SD$  are all perpendiculars to a line  $l$ ,  $AB = 6$  cm,  $BC = 9$  cm,  $CD = 12$  cm and  $SP = 36$  cm. Then, find the  $PQ$ ,  $QR$  and  $RS$ .



- 206) In the given figure,  $\frac{EA}{EC} = \frac{EB}{ED}$ , prove that  $\triangle EAB \sim \triangle ECD$



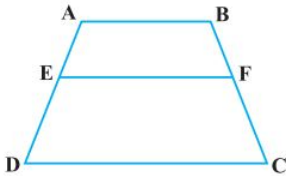
- 207) In the given figure, AD = 2 cm, BD = 3 cm, AE = 3.5 cm and AC = 7 cm. Is DE parallel to BC?



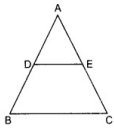
3 Marks

161 x 3 = 483

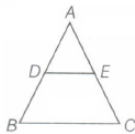
- 208) ABCD is a trapezium with  $AB \parallel DC$ . E and F are points on non-parallel sides AD and BC respectively such that EF is parallel to AB. Show that  $\frac{AE}{ED} = \frac{BF}{FC}$ .



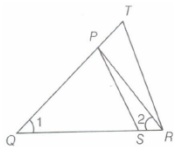
- 209) A girl of height 90 cm is walking away from the base of a lamp-post at a speed of 1.2 m/s. If the lamp is 3.6 m above the ground, find the length of her shadow after 4 seconds.
- 210) Using theorem (Thales theorem), prove that a line drawn through the mid-point of one side of a triangle parallel to another side, bisects the third side. (Recall that you have proved it in Class IX.)



- 211) Using theorem (converse of basic proportionality theorem), prove that the line joining the mid-points of any two sides of a triangle, is parallel to the third side. (Recall that you have done it in Class IX.)

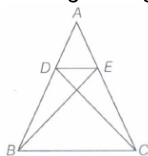


- 212) In the given figure,  $\frac{QR}{QS} = \frac{QT}{PR}$  and  $\angle 1 = \angle 2$ . Show that  $\triangle PQS \sim \triangle TQR$ .



- 213) S and T are points on sides PR and QR of  $\triangle PQR$ , such that  $\angle P = \angle RTS$ . Show that  $\triangle RPQ \sim \triangle RTS$ .

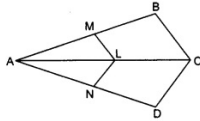
- 214) In the given figure, if  $\triangle ABE \cong \triangle ACD$ , show that  $\triangle ADE \sim \triangle ABC$ .





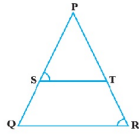
- 215) E is a point on the side AD produced of a parallelogram ABCD and BE intersects CD at F. Show that  $\triangle ABE \sim \triangle CFB$ .

- 216) In the given figure, if LM || CB and LN || CD. Prove that  $\frac{AM}{AB} = \frac{AN}{AD}$ .



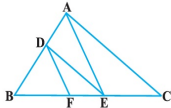
Use the basic proportionality theorem in both  $\triangle ABC$  and  $\triangle ACD$

- 217) In the given figure,  $\frac{PS}{SQ} = \frac{PT}{TR}$  and  $\angle PST = \angle PRQ$ . Prove that PQR is an isosceles triangle.



- 218) If a line intersects sides AB and AC of a  $\triangle ABC$  at D and E respectively and is parallel to BC, prove that  $\frac{AD}{AB} = \frac{AE}{AC}$ .

- 219) In the given figure, if DE || AC and DF || AE. Prove that  $\frac{BF}{FE} = \frac{BE}{EC}$ .

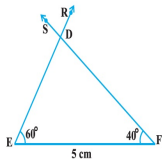


- 220) Draw any angle XAY and on its one arm AX, mark points (say five points) P, Q, D, R and B such that AP = PQ = QD = DR = RB.

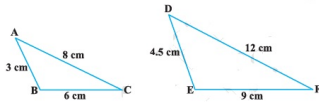
- 221) Draw an angle XAY on your notebook and on ray AX, mark points B<sub>1</sub>, B<sub>2</sub>, B<sub>3</sub>, B<sub>4</sub> and B such that AB<sub>1</sub> = B<sub>1</sub>B<sub>2</sub> = B<sub>2</sub>B<sub>3</sub> = B<sub>3</sub>B<sub>4</sub> = B<sub>4</sub>B.

- 222) If a line divides any two sides of a triangle in the same ratio, then the line is parallel to the third side.

- 223) Draw two line segments BC and EF of two different lengths, say 3 cm and 5 cm respectively. Then, at the points B and C respectively, construct angles PBC and QCB of some measures, say, 60° and 40°. Also, at the points E and F, construct angles REF and SFE of 60° and 40° respectively.

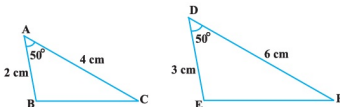


- 224) Draw two triangles ABC and DEF such that AB = 3 cm, BC = 6 cm, CA = 8 cm, DE = 4.5 cm, EF = 9 cm and FD = 12 cm



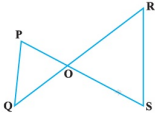
- 225) If in two triangles, sides of one triangle are proportional to (i.e., in the same ratio of) the sides of the other triangle, then their corresponding angles are equal and hence the two triangles are similar.

- 226) Draw two triangles ABC and DEF such that AB = 2 cm,  $\angle A = 50^\circ$ , AC = 4 cm, DE = 3 cm,  $\angle D = 50^\circ$  and DF = 6 cm

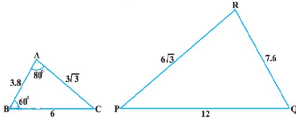


- 227) If one angle of a triangle is equal to one angle of the other triangle and the sides including these angles are proportional, then the two triangles are similar.

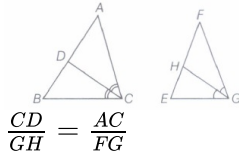
- 228) If  $PQ \parallel RS$ , prove that  $\angle POQ \sim \angle SOR$ .



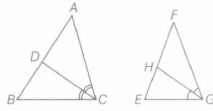
- 229) Observe Figure and then find  $\angle P$ .



- 230) CD and GH are respectively the bisectors of  $\angle ACB$  and  $\angle EGF$  such that D and H lie on sides AB and FE of  $\triangle ABC$  and  $\triangle EFG$  respectively. If  $\triangle ABC \sim \triangle FEG$ , Show that

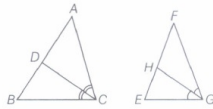


- 231) CD and GH are respectively the bisectors of  $\angle ACB$  and  $\angle EGF$  such that D and H lie on sides AB and FE of  $\triangle ABC$  and  $\triangle EFG$  respectively. If  $\triangle ABC \sim \triangle FEG$ , Show that



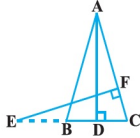
$$\triangle DCB \sim \triangle HGE$$

- 232) CD and GH are respectively the bisectors of  $\angle ACB$  and  $\angle EGF$  such that D and H lie on sides AB and FE of  $\triangle ABC$  and  $\triangle EFG$  respectively. If  $\triangle ABC \sim \triangle FEG$ , Show that

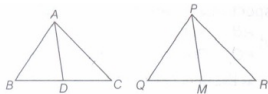


$$\triangle DCA \sim \triangle HGF$$

- 233) In the given figure, E is a point on side CB produced of an isosceles  $\triangle ABC$  with  $AB = AC$ . If  $AD \perp BC$  and  $EF \perp AC$ , prove that  $\triangle ABD \sim \triangle ECF$ .



- 234) Sides AB and BC and median AD of a  $\triangle ABC$  are respectively proportional to sides PQ and QR and median PM of  $\triangle PQR$ . Show that  $\triangle ABC \sim \triangle PQR$ .



- 235) If AD and PM are medians of  $\triangle ABC$  and  $\triangle PQR$ , respectively where  $\triangle ABC \sim \triangle PQR$ , prove that  $\frac{AB}{PQ} = \frac{AD}{PM}$

- 236) Give two examples of pair of similar and non-similar figures.

- 237) P and Q are the points on sides AB and AC, respectively of  $\triangle ABC$ . If  $AP = 3$  cm,  $PB = 6$  cm,  $AQ = 5$  cm and  $QC = 10$  cm, show that  $BC = 3PQ$ .

- 238) A street light bulb is fixed on a pole 6 m above the level of the street. If a woman of height 1.5 m casts a shadow of 3 m, find how far is she away from the base of the pole?

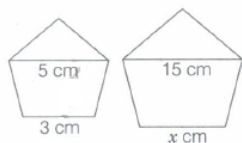
- 239) If the lengths of the diagonals of rhombus are 16 cm and 12 cm. Then, find the length of the sides of the rhombus.

- 240) For going to city B from city A, there is a route via city C such that  $AC \perp CB$ ,  $AC = 2x$  km and  $CB = 2(x + 7)$  km. It is proposed to construct a 26 km highway, which directly connects the two cities A and B. Find how much distance will be saved in reaching city B from city A after the construction on the highway?

- 241) A guy wire attached to a vertical pole of height 18 m is 24 m long and has a stake attached to the other end. How far from the base of the pole should the stake be driven so that the wire will be taut?

- 242) ABC is a triangle. PQ is a line segment intersecting AB at P and AC at Q such that  $PQ \parallel BC$  and divides  $\triangle ABC$  into two parts equal in area. Find BP / AB.

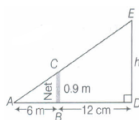
- 243) The given shapes are mathematically similar. Calculate the unknown side.



- 244) If  $\triangle ABC \sim \triangle PQR$ , AB = 6.5 cm, PQ = 10.4 cm and perimeter of  $\triangle ABC$  = 60 cm, find the perimeter of  $\triangle PQR$ .

- 245) It is given that  $\triangle ABC \sim \triangle EDF$  such that AB = 5 cm, AC = 7 cm, DF = 15 cm and DE = 12 cm. Find the lengths of the remaining sides of the triangles.

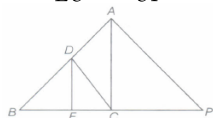
- 246) Find the value of the height 'h' in the adjoining figure. at which the tennis ball must be hit, so that it will just pass over the net and land 6 m away from the base of the net.



- 247) In  $\triangle ABC$ , points P and Q are on CA and CB, respectively such that CA = 16 cm, CP = 10 cm, CB = 30 cm and CQ = 25 cm. Is  $PQ \parallel AB$ ?

- 248) If D and E are points on the respective sides AB and AC of  $\triangle ABC$  such that AD = 6 cm, BD = 9 cm, AE = 8 cm, EC = 12 cm. Prove that  $DE \parallel BC$ .

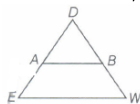
- 249) In the given figure of  $\triangle ABC$ ,  $DE \parallel AC$ . If  $DC \parallel AP$ , where point P lies on BC produced, then prove that  $\frac{BE}{EC} = \frac{BC}{CP}$ .



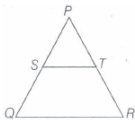
- 250) In the given figure,  $DE \parallel BC$ . If AD = 3 cm, DB = 4 cm and AE = 6 cm, find EC.



- 251) In  $\triangle DEW$ ,  $AB \parallel EW$ . If AD = 4 cm, DE = 12 cm and DW = 24 cm, find the value of DB.

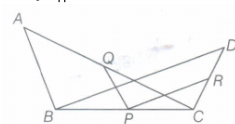


- 252) In  $\triangle PQR$ ,  $ST \parallel QR$ ,  $\frac{PS}{SQ} = \frac{3}{5}$  and PR = 28 cm, find PT.

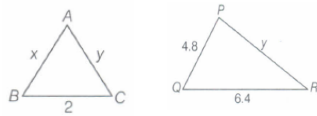


- 253) In  $\triangle ABC$ , D and E are points on the sides AB and AC respectively, such that  $DE \parallel BC$ . If AD = 4x - 3, AE = 8x - 7, BD = 3x - 1 and CE = 5x - 3, find the value of x.

- 254) In the given figure,  $\triangle ABC$  and  $\triangle DBC$  have same base BC and lie on the same side of BC. If  $PQ \parallel BA$  and  $PR \parallel BD$ , then prove that  $QR \parallel AD$ .

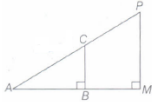


- 255) Find the value of unknown variables, if  $\triangle ABC$  and  $\triangle PQR$  are similar.

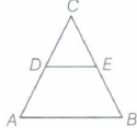


- 256) In  $\triangle PQR$  and  $\triangle MST$ ,  $\angle P = 55^\circ$ ,  $\angle Q = 25^\circ$ ,  $\angle M = 100^\circ$  and  $\angle S = 25^\circ$ . Is  $\triangle QPR \sim \triangle TSM$ ? Why?

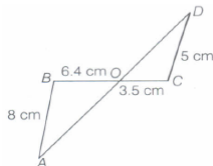
- 257)  $\triangle ABC$  and  $\triangle AMP$  are two right angled triangles. right angled at B and M, respectively. Prove that  $CA \times MP = PA \times BC$



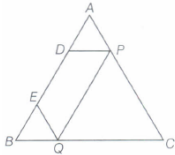
- 258) In the following figure, if  $\frac{AD}{DC} = \frac{BE}{EC}$  and  $\angle CDE = \angle CED$  then prove that  $\triangle CAB$  is an isosceles triangle?



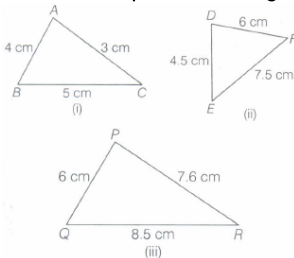
- 259) In the given figure,  $\triangle OAB \sim \triangle OCD$ . If  $AB = 8$  cm,  $BO = 6.4$  cm,  $OC = 3.5$  cm and  $CD = 5$  cm, then find the values of  $OA$  and  $DO$ .



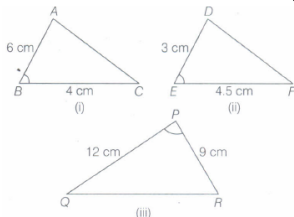
- 260) In the given figure, D and E are two points lying on side AB, such that  $AD = BE$ . If  $DP \parallel BC$  and  $EQ \parallel AC$ , then prove that  $PQ \parallel AB$ .



- 261) State which pairs of triangles in the given figure are similar? Also, state the similarity criterion used.



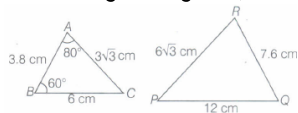
- 262) State which of the two triangles given in the figure are similar? Also, state the similarity criterion used.



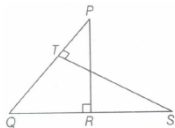
- 263) Find the value of each of the pronumerals in the given pair of triangles. Give reason for your answer.



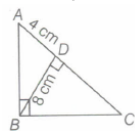
- 264) From the given figures, find  $\angle P$ .



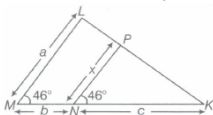
- 265) In the given figure, PQR and QST are two right angled triangles, right angled at R and T, respectively. Prove that  $QR \times QS = QP \times QT$ .



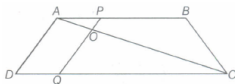
- 266) In the given figure,  $\angle ABC = 90^\circ$  and  $BD \perp AC$ . If  $BD = 8$  cm and  $AD = 4$  cm, then find the value of  $CD$ .



- 267) In the given figure,  $\angle M = \angle N = 46^\circ$ . Express  $x$  in terms of  $a$ ,  $b$  and  $c$ , where  $a$ ,  $b$  and  $c$  are the lengths of  $LM$ ,  $MN$  and  $NK$  respectively.

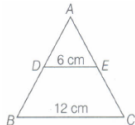


- 268) In the given figure, if  $AB \parallel DC$  and  $AC$ ,  $PQ$  intersect each other at the point  $O$ , then prove that  $OA \cdot CQ = OC \cdot AP$ .



- 269) If  $\triangle ABC \sim \triangle QRP$ ,  $\frac{\text{ar}(\triangle ABC)}{\text{ar}(\triangle QRP)} = \frac{9}{4}$ ,  $AB = 18$  cm and  $BC = 15$  cm, then find  $PR$ .

- 270) In the given figure, if  $DE \parallel BC$ , find the ratio of  $\text{ar}(\triangle ADE)$  and  $\text{ar}(\triangle DECB)$



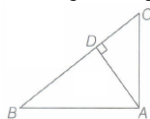
- 271) Diagonals of a trapezium PQRS intersect each other at the point  $O$ ,  $PQ \parallel RS$  and  $PQ = 3RS$ . Find the ratio of the areas of  $\triangle POQ$  and  $\triangle ROS$ .

- 272) Prove that the area of the equilateral triangle described on the side of an isosceles right angled triangle is half the area of the equilateral triangle described on its hypotenuse.

- 273) Equilateral triangles are drawn on the sides of a right angled triangle. Show that the area of the triangle on the hypotenuse is equal to the sum of the areas of triangles on the other two sides.

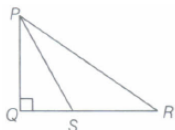
- 274) In an isosceles right angled triangle, if the hypotenuse is  $5\sqrt{2}$  cm, then find the length of the sides of the triangle.

- 275) In the given figure, if  $AD \perp BC$ , prove that  $AB^2 + CD^2 = BD^2 + AC^2$ .

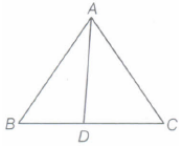


- 276) In  $\triangle PQR$ ,  $PS \perp QR$  and  $PS^2 = QS \times RS$ . Prove that  $\triangle PQR$  is a right angled triangle.

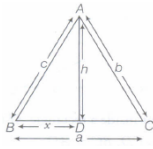
- 277) In the given figure,  $\triangle PQR$  is a right angled triangle in which  $\angle Q = 90^\circ$ . If  $QS = SR$ , show that  $PR^2 = 4 PS^2 - 3PQ^2$ .



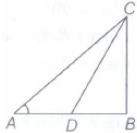
- 278) In the figure,  $\triangle ABC$  is drawn such that  $AD \perp BC$ , then show that  $AC^2 = AB^2 + BC^2 - 2BC \cdot BD$ .



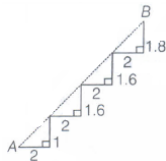
- 279) In the given figure,  $\angle B < 90^\circ$  and segment  $AD \perp BC$ . Show that  $b^2 = h^2 + a^2 + x^2 - 2ax$



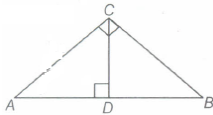
- 280) In the given figure, if  $CD = 17$  m,  $BD = 8$  m and  $AD = 4$  m, find the value of  $AC$ .



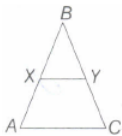
- 281) Find the altitude of an equilateral triangle of side 8 cm.
- 282) There is a staircase as shown in figure connecting points A and B. Measurements of steps are marked in the figure. Find the straight distance between A and B.



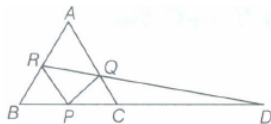
- 283)  $\triangle ABC$  is an isosceles triangle, right angled at C. Prove that  $AB^2 = 2AC^2$ .
- 284)  $\triangle ABC$  is an isosceles triangle with  $AC = BC$ . If  $AB^2 = 2AC^2$ , then prove that  $\triangle ABC$  is a right angled triangle.
- 285) In the given figure,  $\triangle ACB = 90^\circ$  and  $CD \perp AB$ . Prove that  $\frac{BC^2}{AC^2} = \frac{BD}{AD}$



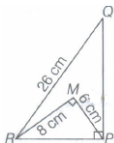
- 286) In the given figure, in  $\triangle ABC$ ,  $XY \parallel AC$  and  $XY$  divides the  $\triangle ABC$  into two regions such that  $ar(\triangle BXY) = 2ar(\triangle ACYX)$ . Determine  $AX / AB$ .



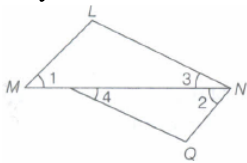
- 287) In the given figure,  $PQ \parallel BA$  and  $PR \parallel CA$ . If  $PD = 12$  cm, then find  $BD \times CD$ .



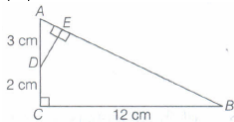
- 288) In the given figure,  $RQ = 26$  cm,  $RM = 8$  cm and  $PM = 6$  cm. If  $\angle M = 90^\circ$ , find the area of  $\triangle PQR$ .



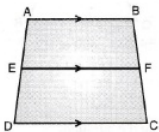
- 289) In figure  $LM \parallel NQ$  and  $LN \parallel PQ$ . If  $MP = \frac{1}{3} MN$ , find the ratio of the area of  $\triangle LMN$  and  $\triangle QNP$ .



- 290) In the given figure, ABC is a right angled triangle, right angled at C and  $DE \perp AB$ .
- Prove that  $\triangle ABC \sim \triangle ADE$
  - Find the lengths of AE and DE.
  - Find the area of  $\triangle ABC$ .



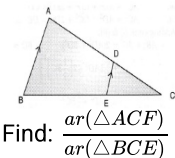
- 291) In right angled  $\triangle ABC$ , right angled at C, P and Q are points of sides CA and CB respectively, which divide these sides in the ratio 2 : 1. Prove that  $9 AQ^2 = 9 AC^2 + 4 BC^2$
- 292) In the given figure, if ABCD is a trapezium in which  $AB \parallel CD \parallel EF$ , then prove that  $\frac{AE}{ED} = \frac{BF}{FC}$ .



- 293) In  $\triangle ABC \sim \triangle PQR$  and AD and PS are bisectors of corresponding angles A and P, then prove that  $\frac{ar(\triangle ABC)}{ar(\triangle PQR)} = \frac{AD^2}{PS^2}$ .

- 294) State whether the given pairs of triangle are similar or not. In case of similarity mention the criterion.

- 295) In given figure, D is a point on AC such that  $AD = 2CD$ , also  $DE \parallel AB$ .



- 296) From an airport, two aeroplanes start at the same time. If speed of first aeroplane due North is 500 km/h and that of other due East is 650 km/h then find the distance between the two aeroplanes after 2 hours.

- 297) Prove that area of the equilateral triangle described on the side of a square is half of the area of the equilateral triangle described on its diagonal.

- 298) In a trapezium ABCD, diagonals AC and BD intersect at O. If  $AB = 3CD$ , then find ratio of areas of triangles COD and AOB.

- 299)  $\triangle ABC$  is right angled at e. If p is the length of the perpendicular from C to AB and a, b, care the lengths of the sides opposite  $\angle A$ ,  $\angle B$  and  $\angle C$  respectively, then prove that  $\frac{1}{p^2} = \frac{1}{a^2} + \frac{1}{b^2}$ .

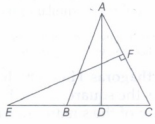
- 300) In MBC,  $DE \parallel Be$ . If  $AD = x + 2$ ,  $DB = 3x + 16$ ,  $AE = x$  and  $EC = 3x + 5$ , then find x.

- 301) If in  $\triangle ABC$ , AD is median and  $AE \perp BC$ , then prove that  $AB^2 + AC^2 = 2AD^2 + \frac{1}{2} BC^2$ .

- 302) ABC is a triangle, PQ is the line segment intersecting AB in P and AC in Q such that  $PQ \parallel BC$  and divides  $\triangle ABC$  into two parts, equal in area, find BP : AB.

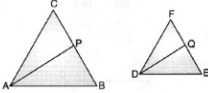
- 303) In the given figure,  $PQ \parallel BA$  and  $PR \parallel CA$ . If  $PD = 12$  cm, find BD x CD.

- 304) In the given figure, ABC is a right angled triangle,  $\angle B = 90^\circ$ . D is the mid-point of BC. Show that  $AC^2 = AD^2 + 3CD^2$ .



- 305) If the diagonals of a quadrilateral divide each other proportionally, prove that it is a trapezium.
- 306) In the given figure, P and Q are the points on the sides AB and AC respectively of  $\triangle ABC$ , such that AP = 3.5 cm, PB = 7 cm, AQ = 3 cm and QC = 6 cm. If PQ = 4.5 cm, find BC.

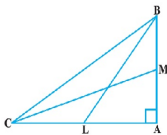
- 307) In given figure  $\triangle ABC \sim \triangle DEF$ . AP bisects  $\angle CAB$  and DQ bisects  $\angle FDE$ .



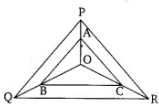
(i)  $\frac{AP}{DQ} = \frac{AB}{DE}$

(ii)  $\triangle CAP \sim \triangle FDQ$ .

- 308) In the given figure,  $DB \perp BC$ ,  $DE \perp AB$  and  $AC \perp BC$ . Prove that  $\frac{BE}{DE} = \frac{AC}{BC}$ .
- 309) In the given figure,  $DE \parallel AB$  and  $FE \parallel DB$ . Prove that  $DC^2 = CF \times AC$ .
- 310) In the given figure,  $\triangle ABC$  and  $\triangle DBC$  are on the same base BC. AD and BC intersect at O. Prove that  $\frac{ar(\triangle ABC)}{ar(\triangle DBC)} = \frac{AO}{DO}$ .
- 311) In the given figure, two triangles ABC and DBC lie on the same side of BC such that  $PQ \parallel BA$  and  $PR \parallel BD$ . Prove that  $QR \parallel AD$ .
- 312) The perpendicular AD on the base BC of a  $\triangle ABC$  intersects BC at D so that  $DB = 3CD$ . Prove that  $2(AB)^2 = 2(AC)^2 + BC^2$ .
- 313) In the given figure,  $\frac{PA}{AQ} = \frac{PB}{BR} = 3$ . If the area of  $\triangle PQR$  is  $32 \text{ cm}^2$ , then find the area of the quadrilateral AQRB.
- 314) Prove that the sum of squares on the sides of a rhombus is equal to sum of squares of its diagonals.
- 315) In the given figure, BL and CM are medians of  $\triangle ABC$ , right angled at A. Prove that  $4(BL^2 + CM^2) = 5BC^2$ .



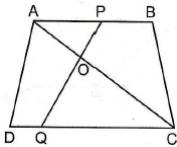
- 316) In a  $\triangle ABC$ , let P and Q be points on AB and AC respectively such that  $PQ \parallel BC$ . Prove that the median AD bisects PQ.
- 317) The diagonals of a trapezium ABCD, in which  $AB \parallel DC$ , intersect at O. If  $AB = 2CD$ , then find the ratio of areas of triangles AOB and COD.
- 318) In the given figure, A, B and C are points on OP, OQ and OR respectively such that  $AB \parallel PQ$  and  $AC \parallel PR$ . Prove that  $BC \parallel QR$ .



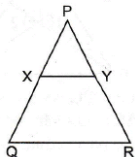
- 319) In the given figure, find the value of x in terms of a, b and c.
- 320) In the given figure,  $BC \parallel PQ$  and  $BC = 8 \text{ cm}$ ,  $PQ = 4 \text{ cm}$ ,  $BA = 6.5 \text{ cm}$ ,  $AP = 2.8 \text{ cm}$ . Find CA and AQ.
- 321) In the given figure, if  $AD \perp BC$ , prove that  $AB^2 + CD^2 = BD^2 + AC^2$ .
- 322) In the given figure,  $CD \parallel LA$  and  $DE \parallel AC$ . Find the length of CL, if  $BE = 4 \text{ cm}$  and  $EC = 2 \text{ cm}$ .
- 323) In the given figure,  $AB = AC$ . E is a point on CB produced. If AD is perpendicular to BC and EF perpendicular to AC. Prove that  $\triangle ABD$  is similar to  $\triangle CEF$ .



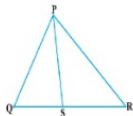
- 324) In the given figure,  $AD \perp BC$  and  $BD = \frac{1}{3} CD$ . Prove that  $2AC^2 = 2AB^2 + BC^2$ .
- 325) If  $ABC$  is an obtuse angled triangle, obtuse angled at  $B$  and if  $AD \perp CB$ . Prove that:  
 $AC^2 = AB^2 + BC^2 + 2BC \times BD$
- 326)  $ABC$  is a right-angled triangle, right-angled at  $A$ . A circle is inscribed in it. The lengths of the two sides containing the right angle are 6 cm and 8 cm. Find the radius of the incircle.
- 327) In a right triangle  $ABC$ , right angled at  $C$ ,  $P$  and  $Q$  are points of the sides  $CA$  and  $CB$  respectively, which divide these sides in the ratio 2 : 1.  
 Prove that :  $9AQ^2 = 9AC^2 + 4BC^2$   
 $9BP^2 = 9BC^2 + 4AC^2$   
 $9(AQ^2 + BP^2) = 13AB^2$ .
- 328) Find the length of the second diagonal of a rhombus, whose side is 5 cm and one of the diagonals is 6 cm.
- 329) Prove that three times the sum of the squares of the sides of a triangle is equal to four times the sum of the squares of the medians of the triangle.
- 330)  $ABC$  is an isosceles triangle in which  $AB = AC = 10$  cm.  $BC = 12$  cm.  $PQRS$  is a rectangle inside the isosceles triangle. Given  $PQ = SR = y$  cm,  $PS = QR = 2x$ . Prove that  $x = 6 - \frac{3y}{4}$ .
- 331) If  $A$  be the area of a right triangle and  $b$  be one of the sides containing the right angle, prove that the length of the altitude on the hypotenuse is  $\frac{2Ab}{\sqrt{b^4 + 4A^2}}$
- 332)  $D$  is the mid-point of side  $BC$  of  $\triangle ABC$  and  $E$  is the mid-point of  $AD$ .  $BE$  produced meets  $AC$  at the point  $M$ . Prove that  $BE = 3EM$
- 333) In fig. if  $AB \parallel DC$  and  $AC$  and  $PQ$  intersect each other at the point  $O$ , prove that  $OA \cdot CQ = OC \cdot AP$



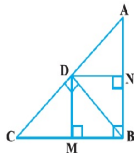
- 334) In the given figure,  $\triangle PQR$  in which  $XY \parallel QR$ ,  $PX = 1$  cm,  $XQ = 3$  cm,  $YR = 4.5$  cm,  $QR = 9$  cm, find  $PY$  and  $XY$ . Further if the area of  $\triangle PXY$  is  $cm^2$ , find in terms of  $A$ , the area of  $\triangle PQR$  and : 33 of trapezium  $XYRQ$ .



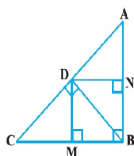
- 335) In the given figure,  $PS$  is the bisector of  $\angle QPR$  of  $\triangle PQR$ . Prove that  $\frac{QS}{SR} = \frac{PQ}{PR}$



- 336) In the given figure,  $D$  is a point on hypotenuse  $AC$  of  $\triangle ABC$ ,  $DM \perp BC$  and  $DN \perp AB$ , Prove that:  
 $DM^2 = DN \cdot MC$

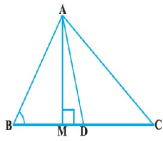


- 337) In the given figure,  $D$  is a point on hypotenuse  $AC$  of  $\triangle ABC$ ,  $DM \perp BC$  and  $DN \perp AB$ , Prove that:  
 $DN^2 = DM \cdot AN$



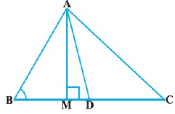
- 338) In the given figure, AD is a median of a triangle ABC and  $AM \perp BC$ . Prove that:

$$AC^2 = AD^2 + BC \cdot DM + \left(\frac{BC}{2}\right)^2$$



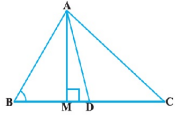
- 339) In the given figure, AD is a median of a triangle ABC and  $AM \perp BC$ . Prove that:

$$AB^2 = AD^2 - BC \cdot DM + \left(\frac{BC}{2}\right)^2$$

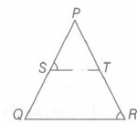


- 340) In the given figure, AD is a median of a triangle ABC and  $AM \perp BC$ . Prove that:

$$AC^2 + AB^2 = 2AD^2 + \frac{1}{2}(BC)^2$$

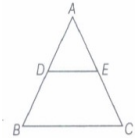


- 341) In the adjoining figure  $\frac{PS}{SQ} = \frac{PT}{TR}$  and  $\angle PST = \angle PRQ$ . Prove that PQR is an isosceles triangle.



- 342) Prove that, if three or more parallel lines are intersected by two transversals, then intercepts made by them on the transversal are proportional.

- 343) In figure,  $DE \parallel BC$  AD = 1cm and BD = 2 cm. What is the ratio of the ar (MBC) to the ar ( $\triangle ADE$ )?



- 344) The areas of two similar triangles are respectively  $25 \text{ cm}^2$  and  $81 \text{ cm}^2$ . Find the ratio of their corresponding sides.

- 345)  $\triangle ABC$  and  $\triangle DEF$  are similar. Area of  $\triangle DEF$  is  $9 \text{ cm}^2$  and area of  $\triangle ABC$  is  $81 \text{ cm}^2$ . If  $DE = 5.1 \text{ cm}$ , then find the value of  $AB$ .

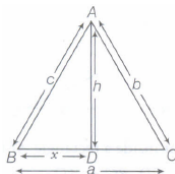
- 346)  $\triangle ABC$  and  $\triangle DEF$  are similar and  $AB = \frac{1}{3}DE$  then find  $\text{ar}(\triangle ABC) : \text{ar}(\triangle DEF)$

- 347) In  $\triangle ABC$ ,  $PQ \parallel AC$  and  $PQ$  divides triangular region ABG into two parts such that  $\text{ar}(\triangle BPQ) = \frac{1}{4} \text{ar}(\triangle PQC)$ . Find  $BP : PA$ .

- 348) In the given figure,  $\triangle AED$  and trapezium EBCD are such that the area of trapezium is three times the area of the triangle. Find the ratio  $\frac{AE}{AB}$ .



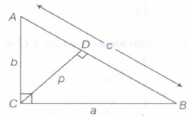
- 349) In the given figure,  $\angle B < 90^\circ$  and segment  $AD \perp BC$ . Show that  $b^2 = h^2 + a^2 + x^2 - 2ax$



- 350) Two isosceles triangles have equal vertical angles and their areas are in the ratio 36 : 25. Find the ratio of their corresponding heights.

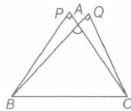
- 351) In an isosceles triangle ABC, if  $AB = AC = 25$  cm and altitude from A on BC is 24 cm, then find BC.

- 352)  $\triangle ABC$  is a right triangle in which  $\angle C = 90^\circ$  and  $CD \perp AB$ . If  $BC = a$ ,  $CA = b$ ,  $AB = c$  and  $CD = p$ , then prove that
- $$\frac{1}{p^2} = \frac{1}{a^2} + \frac{1}{b^2}$$

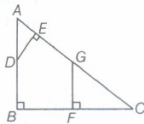


- 353) Two students of class X, discuss on criteria for similarity of triangles. First student explain SSS similarity criterion as in  $\triangle ABC$  and  $\triangle DEF$  such that  $\angle A = \angle D$  and  $\frac{AB}{DE} = \frac{AC}{DF}$ , at once second student said, "It is wrong". If you agree with second student, give correct explanation.

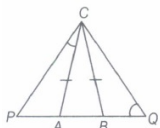
- 354) In  $\triangle ABC$ ,  $\angle A$  is obtuse,  $PB \perp PC$  and  $QC \perp QB$ . Prove that  $AB \times AQ = AC \times AP$ .



- 355) In the given figure, if  $AB \perp BC$ ,  $DE \perp AC$  and  $GF \perp BC$ , then prove that  $\triangle ADE \sim \triangle GCF$ .

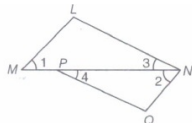


- 356) In given figure, ABC is an isosceles triangle with  $AC = BC$ . AB is produced on either side till P and Q respectively such that  $AP \times BQ = AC^2$ . Prove that  $\angle PCA = \angle CQB$ .



- 357) PB and QA are the perpendiculars to segment AB. If  $PO = 5$  cm,  $QO = 7$  cm and  $\text{ar}(\triangle BOP) = 150 \text{ cm}^2$ , find  $\text{ar}(\triangle QOA)$ .

- 358) In the given figure  $LM \parallel NQ$  and  $LN \parallel PQ$ . If  $MP = \frac{1}{3} MN$ , find the ratio of the area of  $\triangle LMN$  and  $\triangle QNP$ .



- 359) A farmer has a field in the shape of a rightangled triangle with legs (sides other than the hypotenuse) are of lengths 16 m and 8 m. She wants to leave a space in the form of a square of largest area for growing wheat and remaining area for growing vegetables.

- (i) Find the length of the side of such a square.  
(ii) Find the area of the square.

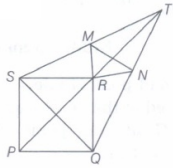
- 360) In  $\triangle ABC$ ,  $\angle BCA = 90^\circ$ , Q is the mid-point of BC, prove that  $(AB)^2 = 4AQ^2 - 3AC^2$ .

- 361) In a  $\triangle PQR$ ,  $PR^2 - PQ^2 = QR^2$  and M is a point on side PR such that  $QM \perp PR$ . Prove that  $QM^2 = PM \times MR$ .

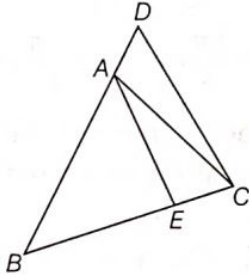
- 362) In a quadrilateral ABCD,  $\angle A + \angle D = 90^\circ$ .  
Prove that  $AC^2 + BD^2 = AD^2 + BC^2$ .

- 363) If S is a point on side PQ of a  $\triangle PQR$  such that  $PS = QS = RS$ , prove that  $PR^2 + QR^2 = PQ^2$ .

- 364) In the given figure, T is the exterior point on the diagonal PR of a parallelogram PQRS. SR produced meets OT at N and QR produced meets ST at M. Prove that  $MN \parallel SQ$ .

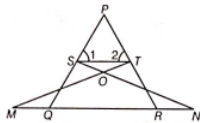


- 365) In the given figure,  $\angle ABC = \angle ACB$  and  $\frac{BC}{BE} = \frac{BD}{AC}$

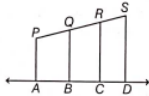


Show that  $\triangle ABE \sim \triangle DBC$  and  $AE \parallel DC$ .

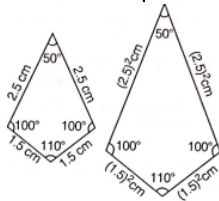
- 366) In the given figure, if  $\angle 1 = \angle 2$  and  $\triangle NSQ = \triangle MTR$ , prove that  $\triangle PTS \sim \triangle PRQ$ .



- 367) In the given figure PA, QB, RC and SD are all perpendiculars to a line,  $AB = 6$  cm,  $BC = 9$  cm,  $CD = 12$  cm and  $SP = 36$  cm. Then, find the PQ, QR and RS.



- 368) Are the two quadrilaterals shown below similar? Give a reason for your answer



Case Study Questions

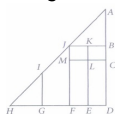
24 x 4 = 96

369)

In a classroom, students were playing with some pieces of cardboard as shown below.



All of a sudden, teacher entered into classroom. She told students to arrange all pieces. On seeing this beautiful image, she observed that  $\triangle ADH$  is right angled triangle, which contains.



(i) right triangles ABJ and IGH.

(ii) quadrilateral GFJI

(iii) squares JKLM and LCBK

(iv) rectangles MLEF and LCDE.

After observation, she ask certain questions to students. Help them to answer these questions.

(i) If an insect (small ant) walks 24 m from H to F, then walks 6 m to reach at M, then walks 4 m to reach at L and finally crossing K, reached at J. Find the distance between initial and final position of insect.

(a) 25m (b) 26m (c) 27m (d) 28m

(ii) If m, n and r are the sides of right triangle ABJ, then which of the following can be correct?

(a)  $m^2 + n^2 = r^2$

(b)  $m^2 + n^2 + r^2 = 0$

(c)  $m^2 + n^2 = 2r^2$

(d) none of these

(iii) If  $\triangle ABJ \sim \triangle ADH$ , then which similarity criterion is used here?

(a) AA (b) SAS (c) AAS (d) SSS

(iv) If  $\angle ABJ = 90^\circ$  and B, J are mid points of sides AD and AH respectively and  $BJ \parallel DH$ , then which of the following option is false?

(a)  $\triangle ABJ \sim \triangle ADH$  (b)  $2BJ = DH$  (c)  $AJ^2 = JB^2 + AB^2$  (d)  $\frac{AB}{BD} = \frac{AJ}{AH}$

(v) If  $\triangle PQR$  is right triangle with  $QM \perp PR$ , then which of the following is not correct?



(a)  $\triangle PMQ \sim \triangle PQR$

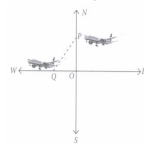
(b)  $QR^2 = PR^2 - PQ^2$

(c)  $PR^2 = PQ + QR$

(d)  $\triangle PMQ \sim \triangle QMR$

370)

An aeroplane leaves an airport and flies due north at a speed of 1200km /hr. At the same time, another aeroplane leaves the same station and flies due west at the speed of 1500 km/hr as shown below. After  $1\frac{1}{2}$  hr both the aeroplanes reaches at point P and Q respectively.



(i) Distance travelled by aeroplane towards north after  $1\frac{1}{2}$  hr is

(a) 1800 (b) 1500 (c) 1400km (d) 1350

km km km km

(ii) Distance travelled by aeroplane towards west after  $1\frac{1}{2}$  hr is

(a) 1600 (b) 1800 (c) 2250km (d) 2400

km km km km

(iii) In the given figure,  $\angle POQ$  is

(a)  $70^\circ$  (b)  $90^\circ$  (c)  $80^\circ$  (d)  $100^\circ$

(iv) Distance between aeroplanes after  $1\frac{1}{2}$  hr is

(a)  $450\sqrt{41}$  km (b)  $350\sqrt{31}$  km (c)  $125\sqrt{12}$  km (d)  $472\sqrt{41}$  km

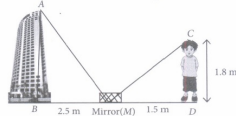
(v) Area of  $\triangle POQ$  is

(a)  $185000\text{km}^2$  (b)  $179000\text{km}^2$

(c)  $186000\text{km}^2$  (d)  $2025000\text{ km}^2$

371)

Rohit's father is a mathematician. One day he gave Rohit an activity to measure the height of building. Rohit accepted the challenge and placed a mirror on ground level to determine the height of building. He is standing at a certain distance so that he can see the top of the building reflected from mirror. Rohit eye level is at 1.8m above ground. The distance of Rohit from mirror and that of building from mirror are 1.5 m and 2.5 m respectively.



Based on the above information, answer the following questions.

(i) Two similar triangles formed in the above figure is

(a)  $\triangle ABM$  and  $\triangle CDM$

(b)  $\triangle AMB$  and  $\triangle CDM$

(c)  $\triangle ABM$  and  $\triangle CDM$

(d)  
None  
of  
these

(ii) Which criterion of similarity is applied here?

(a) AA similarity criterion (b) SSS similarity criterion

(c) SAS similarity criterion (d) ASA similarity criterion

(iii) Height of the building is

(a) 1m (b) 2m (c) 3m (d) 4m

(iv) In  $\triangle ABM$ , if  $\angle BAM = 30^\circ$ , then  $\angle MCD$  is equal to

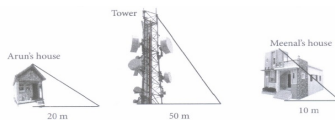
(a)  $40^\circ$  (b)  $30^\circ$  (c)  $65^\circ$  (d)  $90^\circ$

(v) If  $\triangle ABM$  and  $\triangle CDM$  are similar where  $CD = 6$  cm,  $MD = 8$  cm and  $BM = 24$  cm, then  $AB$  is equal to

(a) 16cm (b) 18cm (c) 12cm (d) 14cm

372)

Meenal was trying to find the height of tower near his house. She is using the properties of similar triangles. The height of Meenal's house is 20 m. When Meenal's house casts a shadow of 10m long on the ground, at the same time, tower casts a shadow of 50 m long and Arun's house casts a shadow of 20 m long on the ground as shown below.



Based on the above information, answer the following questions.

(i) What is the height of tower?

(a) 100 m (b) 50 m (c) 15 m (d) 45 m

(ii) What will be the length of shadow of tower when Meenal's house casts a shadow of 15 m?

(a) 45 m (b) 70 m (c) 75 m (d) 72 m

(iii) Height of Arun's house is

(a) 80 m (b) 75 m (c) 60 m (d) 40 m

(iv) If tower casts a shadow of 40 m, then find the length of shadow of Arun's house

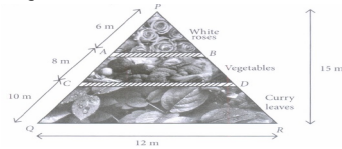
(a) 18 m (b) 17 m (c) 16 m (d) 14 m

(v) If tower casts a shadow of 40 m, then what will be the length of shadow of Meenal's house?

(a) 7 m (b) 9 m (c) 4 m (d) 8 m

373)

In the backyard of house, Shikha has some empty space in the shape of a  $\triangle PQR$ . She decided to make it a garden. She divided the whole space into three parts by making boundaries AB and CD using bricks to grow flowers and vegetables where  $AB \parallel CD \parallel QR$  as shown in figure.



Based on the above information, answer the following questions.

(i) The length of AB is

- (a) 3m (b) 4m (c) 5m (d) 6m

(ii) The length of CD is

- (a) 4m (b) 5m (c) 6m (d) 7m

(iii) Area of whole empty land is

- (a) 90  $m^2$  (b) 60  $m^2$  (c) 32  $m^2$  (d) 72  $m^2$

(iv) Area of  $\triangle PAB$  is

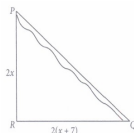
- (a)  $\frac{45}{4} m^2$  (b)  $\frac{45}{8} m^2$  (c)  $\frac{8}{45} m^2$  (d)  $\frac{4}{45} m^2$

(v) Area of  $\triangle PCD$  is

- (a)  $\frac{12}{245} m^2$  (b)  $\frac{245}{12} m^2$  (c)  $\frac{243}{8} m^2$  (d)  $\frac{245}{8} m^2$

374)

Minister of a state went to city Q from city P. There is a route via city R such that  $PR \perp RQ$ .  $PR = 2x$  km and  $RQ = 2(x + 7)$  km. He noticed that there is a proposal to construct a 26 km highway which directly connects the two cities P and Q.



Based on the above information, answer the following questions.

(i) Which concept can be used to get the value of x?

- (a) Thales theorem (b) Pythagoras theorem  
(c) Converse of Thales theorem (d) Converse of Pythagoras theorem

(ii) The value of x is

- (a) 4 (b) 6 (c) 5 (d) 8

(iii) The value of PR is

- (a) 10 km (b) 20 km (c) 15 km (d) 25 km

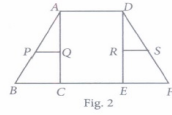
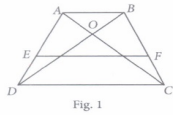
(iv) The value of RQ is

- (a) 12 km (b) 24 km (c) 16 km (d) 20 km

(v) How much distance will be saved in reaching city Q after the construction of highway?

- (a) 10 km (b) 9 km (c) 4 km (d) 8 km

- 375) Class teacher draw the shape of quadrilateral on board. Ankit observed the shape and explored on his notebook in different ways as shown below.



Based on the above information, answer the following questions.

(i) In if ABCD is a trapezium with  $AB \parallel CD$ , E and F are points on non-parallel sides AD and BC respectively such that  $EF \parallel AB$ , then  $\frac{AE}{ED} =$

- (a)  $\frac{BE}{CD}$  (b)  $\frac{AB}{CD}$  (c)  $\frac{BF}{FC}$  (d) None of these

(ii) In if  $AB \parallel CD$ , and  $DO = 3x - 19$ ,  $OB = x - 5$ ,  $OC = x - 3$  and  $AO = 3$ , then the value of x can be

- (a) 5 or (b) 8 or (c) 10 or (d) 13 or

8 9 12 14

(iii) In if  $OD = 3x - 1$ ,  $OB = 5x - 3$ ,  $OC = 2x + 1$  and  $AO = 6x - 5$ , then the value of x is

- (a) 0 (b) 1 (c) 2 (d) 3

(iv) In  $\triangle ABC$ , if  $PQ \parallel BC$  and  $AP = 2.4$  cm,  $AQ = 2$  cm,  $QC = 3$  cm and  $BC = 6$  cm, then  $AB + PQ$  is equal to

- (a) 7.2 (b) 5.9 (c) 2.6 (d) 8.4

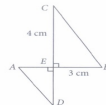
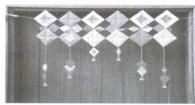
cm cm cm cm

(v) In  $\triangle DEF$ , if  $RS \parallel EF$ ,  $DR = 4x - 3$ ,  $DS = 8x - 7$ ,  $ER = 3x - 1$  and  $FS = 5x - 3$ , then the value of x is

- (a) (b) 5.9 (c) 2.6 (d) 8.4

1 cm cm cm

- 376) Ankita wants to make a toran for Diwali using some pieces of cardboard. She cut some cardboard pieces as shown below. If perimeter of  $\triangle ADE$  and  $\triangle BCE$  are in the ratio 2: 3, then answer the following questions.



(i) If the two triangles here are similar by SAS similarity rule, then their corresponding proportional sides are

- (a)  $\frac{AE}{CE} = \frac{DE}{BE}$  (b)  $\frac{BE}{AE} = \frac{CE}{DE}$  (c)  $\frac{AD}{CE} = \frac{BE}{DE}$  (d) None of these

(ii) Length of BC =

- (a) 2 (b) (c) 5 (d) None of these

cm 4 cm cm

(iii) Length of AD =

- (a) 10/3 (b) 9/4 (c) 5/3 (d) 4/3

cm cm cm cm

(iv) Length of ED =

- (a) 4/3 (b) 8/3 (c) 7/3 (d) None of these

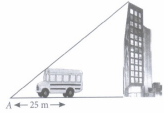
cm cm cm

(v) Length of AE =

- (a)  $\frac{2}{3} \times BE$  (b)  $\sqrt{AD^2 - DE^2}$  (c)  $\frac{2}{3} \times \sqrt{BC^2 - CE^2}$  (d) All of these

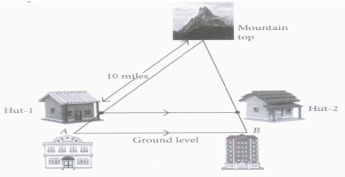


- 377) Aruna visited to her uncle's house. From a point A, where Aruna was standing, a bus and building come in a straight line as shown in the figure.  
Based on the above information, answer the following questions.



- (i) Which similarity criteria can be seen in this case, if bus and building are considered in a straight line?  
**(a) AA (b) SAS (c) SSS (d) ASA**
- (ii) If the distance between Aruna and the bus is twice as much as the height of the bus, then the height of the bus is  
**(a) 40 (b) 12.5 (c) 15 (d)**  
**m m m 20 m**
- (iii) If the distance of Aruna from the building is twelve times the height of the bus, then the ratio of the heights of bus and building is  
**(a) 3:1 (b) 1:4 (c) 1:6 (d) 2:3**
- (iv) What is the ratio of the distance between Aruna and top of bus to the distance between the tops of bus and building?  
**(a) 1:5 (b) 1:6 (c) 2:5 (d) Can't be determined**
- (v). What is the height of the building?  
**(a) 50 (b) 75 (c) 120 (d)**  
**m m m 30 m**

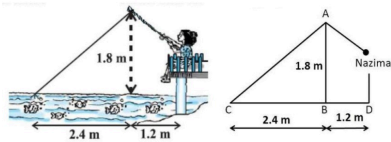
- 378) Two hotels are at the ground level on either side of a mountain. On moving a certain distance towards the top of the mountain two huts are situated as shown in the figure. The ratio between the distance from hotel B to hut-2 and that of hut-2 to mountain top is 3: 7.



- Based on the above information, answer the following questions.
- (i) What is the ratio of the perimeters of the triangle formed by both hotels and mountain top to the triangle formed by both huts and mountain top?  
**(a) 5: 2 (b) 10: 7 (c) 7: 3 (d) 3: 10**
- (ii) The distance between the hotel A and hut-1 is  
**(a) 2.5 (b) 29 (c) 4.29 (d) 1.5**  
**miles miles miles miles**
- (iii) If the horizontal distance between the hut -1 and hut -2 is 8 miles, then the distance between the two hotels is  
**(a) 2.4 (b) 11.43 (c) 9 (d) 7**  
**miles miles miles miles**
- (iv) If the distance from mountain top to hut-1 is 5 miles more than that of distance from hotel B to mountain top, then what is the distance between hut-2 and mountain top?  
**(a) 3.5 (b) 6 (c) 5.5 (d) 4**  
**miles miles miles miles**
- (v) What is the ratio of areas of two parts formed in the complete figure?  
**(a) 53: 21 (b) 10: 41 (c) 51: 33 (d) 49:51**

379)

Nazima is fly fishing in a stream. The tip of her fishing rod is 1.8 m above the surface of the water and the fly at the end of the string rests on the water 3.6 m away and 2.4 m from a point directly under the tip of the rod. She is pulling the string at the rate of 5 cm per second. Nazima's friend observe her position and draw a rough sketch by using A, B, C and D positions of tip, point directly under the tip of the rod, fish and Nazima's position (see the below figure). Assuming that her string (from the tip of her rod to the fly) is taut, answer the following questions:



(a) What is the length AC?

- (a) 2 m    (b) 3 m    (c) 4 m    (d) 5 m

(b) What is the length of string pulled in 12 seconds?

- (a) 6 m    (b) 0.3 m    (c) 0.6 m    (d) 3 m

(c) What is the length of string after 12 seconds?

- (a) 2.4 m    (b) 2.7 m    (c) 2 m    (d) 2.2 m

(d) What will be the horizontal distance of the fly from her after 12 seconds?

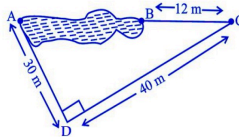
- (a) 2.7 m    (b) 2.78 m    (c) 2.58 m    (d) 2.2 m

(e) The given problem is based on which concept?

- (a) Triangles    (b) Co-ordinate geometry    (c) Height and Distance    (d) None of these

380)

Points A and B are on the opposite edges of a pond as shown in below figure. To find the distance between the two points, Ram makes a right-angled triangle using rope connecting B with another point C at a distance of 12 m, connecting C to point D at a distance of 40 m from point C and then connecting D to the point A which is at a distance of 30 m from D such that  $\angle ADC = 90^\circ$ .



(i) Which property of geometry will be used to find the distance AC?

- (a) Similarity of Triangles    (b) Thales Theorem    (c) Pythagoras Theorem    (d) Quadratic Equation

(ii) What is the distance AC?

- (a) 50m    (b) 12m    (c) 100m    (d) 70m

(iii) Which of the following does not form a Pythagoras triplet?

- (a) (7, 24, 25)    (b) (15, 8, 17)    (c) (5, 12, 13)    (d) (21, 20, 28)

(iv) Find the length AB.

- (a) 12m    (b) 38m    (c) 50m    (d) none of these

(v) Find the length of the rope used.

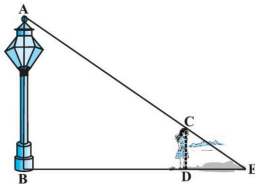
- (a) 120m    (b) 70m    (c) 82m    (d) none of these

- 381) Rahul is studying in X Standard. He is making a kite to fly it on a Sunday. Few questions came to his mind while making the kite. Give answers to his questions by looking at the figure.



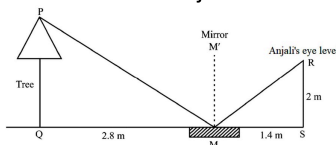
- (i) Rahul tied the sticks at what angles to each other?  
**(a) 30° (b) 60° (c) 90° (d) 60°**
- (ii) Which is the correct similarity criteria applicable for smaller triangles at the upper part of this kite?  
**(a) RHS (b) SAS (c) SSA (d) AAS**
- (iii) Sides of two similar triangles are in the ratio 4:9. Corresponding medians of these triangles are in the ratio,  
**(a) 2:3 (b) 4:9 (c) 81:16 (d) 16:81**
- (iv) In a triangle, if square of one side is equal to the sum of the squares of the other two sides, then the angle opposite the first side is a right angle. This theorem is called as,  
**(a) Pythagoras theorem (b) Thales theorem (c) Converse of Thales theorem (d) Converse of Pythagoras theorem**
- (v) What is the area of the kite, formed by two perpendicular sticks of length 6 cm and 8 cm?  
**(a) 48 cm<sup>2</sup> (b) 14 cm<sup>2</sup> (c) 24 cm<sup>2</sup> (d) 96 cm<sup>2</sup>**

- 382) On one day, a poor girl of height 90 cm is looking for a lamp-post for completing her homework as in her area power is not there and she finds the same at some distance away from her home. After completing the homework, she is walking away from the base of a lamp-post at a speed of 1.2 m/s. The lamp is 3.6 m above the ground (see below figure).



- (i) Find her distance from the base of the lamp post.  
**(a) 1.2 m (b) 3.6 m (c) 4.8 m (d) none of these**
- (ii) Find the correct similarity criteria applicable for triangles ABE and CDE.  
**(a) AA (b) SAS (c) SSS (d) AAS**
- (iii) Find the length of her shadow after 4 seconds.  
**(a) 1.2 m (b) 3.6 m (c) 4.8 m (d) none of these**
- (iv) Sides of two similar triangles are in the ratio 9:16. Find the ratio of Corresponding areas of these triangles.  
**(a) 9:16 (b) 3:4 (c) 81:256 (d) 18:32**
- (v) Find the ratio AC:CE.  
**(a) 1:3 (b) 3:1 (c) 1:4 (d) 4:1**

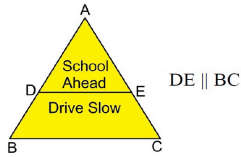
- 383) Anjali places a mirror on level ground to determine the height of a tree (see the diagram). She stands at a certain distance so that she can see the top of the tree reflected from the mirror. Anjali's eye level is 2 m above the ground. The distance of Anjali and the tree from the mirror are 1.4 m and 2.8 m respectively.



- (i) What are the two  $\triangle$  s formed in the above diagram, which are used to calculate the height of the tree?  
**(a)  $\triangle$  s QMM' and PQM (b)  $\triangle$  s PQM and RSM (c)  $\triangle$  s RM'M and MRS (d)  $\triangle$  s PM'M and RM'M**
- (ii) State the criterion of similarity, that will be used in the above found triangles.  
**(a) RHS (b) SSS (c) SAS (d) AA**
- (iii) What is the height of the tree?  
**(a) 4 m (b) 5 cm (c) 6 m (d) 7 cm**
- (iv) What is the distance between Rashmi and Gulmohar tree?  
**(a) 3.2 m (b) 5.2 m (c) 4.2 m (d) 2.2 m**

384)

A group of students to volunteer are working in making a safety board for school. They prepared once triangular safety board for their school with title "School Ahead" and "Drive Slow" in two parts of the triangular board as shown in below figure.



(i) If  $AD = 2$  cm,  $BD = 5$  cm and  $AE = 3$  cm, then,  $EC = ?$

- (a)  $\frac{15}{2}$       (b)  $\frac{3}{5}$       (c)  $\frac{1}{5}$       (d)  $\frac{6}{5}$

(ii) If  $AD = 3$  cm,  $AB = 9$  cm,  $BC = 6$  cm, then  $DE = ?$

- (a) 4 cm    (b) 3 cm    (c) 2 cm    (d) 1 cm

(iii) If  $\angle A = 60^\circ$  and  $\angle ADE = 50^\circ$  then  $\angle C = ?$

- (a)  $70^\circ$     (b)  $75^\circ$     (c)  $85^\circ$     (d)  $40^\circ$

(iv) Which of the following is correct?

- (a)  $\triangle ADE \sim \triangle ABC$       (b)  $\triangle ADE \cong \triangle ABC$

- (c) (d)  
Both None  
(i) & of  
(ii) these

(v) What is the ratio of  $\text{ar}(\triangle ADE)$  to  $\text{ar}(\triangle ABC)$  ?

- (a)  $\frac{\text{ar}(\triangle ADE)}{\text{ar}(\triangle ABC)} = \frac{AD^2}{AB^2}$     (b)  $\frac{\text{ar}(\triangle ADE)}{\text{ar}(\triangle ABC)} = \frac{AD}{AB}$     (c)  $\frac{\text{ar}(\triangle ADE)}{\text{ar}(\triangle ABC)} = 1$     (d) None of these

385)

A scale drawing of an object is the same shape as the object but a different size. The scale of a drawing is a comparison of the length used on a drawing to the length it represents. The scale is written as a ratio. The ratio of two corresponding sides in similar figures is called the scale factor.

$$\text{Scale factor} = \frac{\text{length in image}}{\text{corresponding length in object}}$$



If one shape can become another using resizing, then the shapes are similar. Hence, two shapes are similar when one can become the other after a resize, flip, slide or turn. In the photograph below showing the side view of a train engine. Scale factor is 1:200.

This means that a length of 1 cm on the photograph above corresponds to a length of 200 cm, or 2 metres, on the actual engine. The scale can also be written as the ratio of two lengths.

(a) If the length of the model is 11 cm, then the overall length of the engine in the photograph above, including the couplings (mechanism used to connect) is

- (i) 22 cm    (ii) 220 cm    (iii) 220 m    (iv) 22 m

(b) What will affect the similarity of any two polygons?

- (i) They are flipped horizontally    (ii) They are dilated by a scale factor.  
(iii) They are translated down    (iv) They are not the mirror image of one another

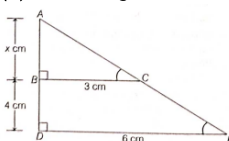
(c) What is the actual width of the door if the width of the door in photograph is 0.35 cm?

- (i) 0.7 m    (ii) 0.7 cm    (iii) 0.07 cm    (iv) 0.07 m

(d) If two similar triangles have a scale factor of 5 : 3, which statement regarding the two triangles is true

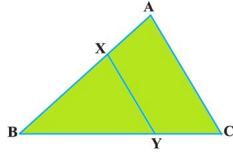
- (i) The ratio of their perimeters is 15 : 1    (ii) Their altitudes have a ratio 25 : 15  
(iii) Their medians have a ratio 10 : 4    (iv) Their medians have a ratio 10 : 4

(e) The length of AB in the given figure is



- (i) 8 cm    (ii) 6 cm    (iii) 4 cm    (iv) 0.07 m

- 386) In one of the residential colony of city, there is a triangular park ABC available. The Resident Welfare Association of the colony wishes to divide this park into two parts of equal areas. One for planting trees and raising a lawn and the other for providing place for children park for playing activities. One of the members Ram suggested to draw a line segment  $XY \parallel BC$  for the same.



(i) Which is the correct similarity criteria is used for above triangles ABC and XBY?

- (a) SSS (b) AAA (c) RHS (d) ASA

(ii) What is the ratio of areas of  $\triangle ABC : \triangle XBY$ ?

- (a) 1 : 2 (b) 2 : 1 (c) 1 : 4 (d)  $1 : \sqrt{2}$

(iii) If  $\angle BXY = 60^\circ$  then  $\angle BAC$  is :

- (a)  $80^\circ$  (b)  $60^\circ$  (c)  $140^\circ$  (d)  $100^\circ$

(iv) If the ratio of areas of  $\triangle BXY : \triangle ABC$  is 1 : 2, then  $XB : AB$  is

- (a) 1 : 2 (b) 1 : 4 (c) 2 : 4 (d)  $1 : \sqrt{2}$

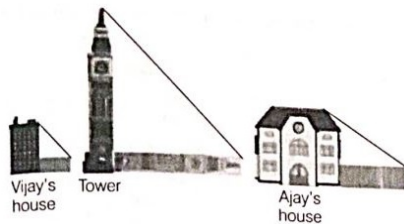
(v) If the area of  $\triangle AXY$  is  $128 \text{ m}^2$ , then what will be area of  $\triangle CXY$ .

- (a)  $128 \text{ m}^2$  (b)  $248 \text{ m}^2$  (c)  $256 \text{ m}^2$  (d)  $48 \text{ m}^2$

- 387) Vijay is trying to find the average height of a tower near his house. He is using the properties of similar triangles.

The height of Vijay's house, if 20 m when Vijay's house casts a shadow 10m long on the ground.

At the same time, the tower casts a shadow 50 m long on the ground and the house of Ajay casts 20 m shadow on the ground.



(i) What is the height of the tower?

- (a) 20 m (b) 50 m (c) 100 m (d) 200 m

(ii) What will be the length of the shadow of the tower when Vijay's house casts a shadow of 12 m?

- (a) 75 m (b) 50 m (c) 45 m (d) 60 m

(iii) What is the height of Ajay's house?

- (a) 30 m (b) 40 m (c) 50 m (d) 20 m

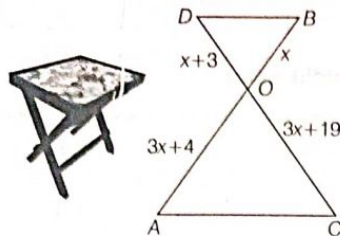
(iv) When the tower casts a shadow of 40 m, same time what will be the length of the shadow of Ajay's house?

- (a) 16 m (b) 32 m (c) 20 m (d) 8 m

(v) When the tower casts a shadow of 40 m, same time what will be the length of the shadow of Vijay's house?

- (a) 15 m (b) 32 m (c) 16 m (d) 8 m

- 388) In the figure given below, a folding table is shown. The legs of the table are represented by line segments AB and CD intersecting at O. Join AC and BD. Considering table top is a parallel to the ground and  $OB = x$ ,  $OD = x + 3$ ,  $OC = 3x + 19$  and  $OA = 3x + 4$ , answer the following questions.



(i) Prove that  $\triangle OAC$  is similar to  $\triangle OBD$

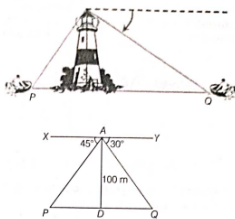
(ii) Prove that  $\frac{OA}{AC} = \frac{OB}{BD}$

(iii) (a) Observe the figure and find the value of  $x$ . Hence, find the length of  $OC$ .

Or

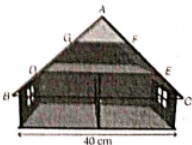
(b) Observe the figure and find  $\frac{BD}{AC}$ .

- 389) A boy is standing on the top of light house. He observed that Boat Pand Boat Qare approaching the light house from opposite directions. He finds that angle of depression of Boat P is  $45^\circ$  and angle of depression of Boat Q is  $30^\circ$ . He also knows that height of the light house is 100 m.



Based on the above information, answer the following questions.

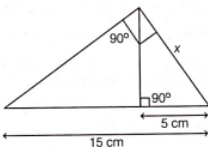
- What is the measure of  $\angle APD$ ?
  - If  $\angle YAQ 30^\circ$ , then  $\angle AQD$  is also  $30^\circ$ . Why?
  - How far is Boat P from the light house? Or How far is Boat Q from the light house?
- 390) Three villages X, Y and Z are situated at the three ends of a triangular region bounded by three roads. The lengths of the roads connecting X to Y, Y to Z and Z to X are in the ratio 5 : 3 : 4. The total lengths of the three roads are 180 km.
- A new road is to be constructed parallel to the longest road. A team of three researchers Mayank, Biju and Shanti work on the technical specifications of the new road construction. Each of them makes a scale drawing of the region using different scale factors. Based on the above information, answer the following questions.
- Which types of triangles are included in their scale drawings, similar or congruent? Why?
  - The proposed road will meet the road between Y and Z in the middle. How far is the Village Y (in km) from the meeting point of the roads?
  - In all the three scale drawings, the actual length of the new road is provided. Would the road length be the same in their maps? Justify your answer.
- 391) A dollhouse with a triangular roof is shown below



The front and back triangles are equilateral triangles with side lengths 45 cm each. Panels parallel to the floor of the dollhouse are used to make the attic. The sides DE and GF of the panels divide the sides AB and AC into three equal parts.

Based on the above information, answer the following questions.

- Which criteria of similar triangles do not apply to  $\triangle AGF$  and  $\triangle ADE$ ?
  - AAA
  - SSS
  - SAS
  - RHS
- The area of  $\triangle ABC$  is  $692 \text{ cm}^2$ , What is the area of the plank AGF?
- What is the height (in cm) of the attic?
- Two Overlapping right triangles are shown below. What is the value of x?



- 4 cm
- $5\sqrt{3}$  cm
- 10 cm
- 37.5 cm

- 392) Some concrete water towers have been built to supply water to the localities nearby. They are usually mounted with a cylindrical tank. A water tower for a locality is 40 m high.



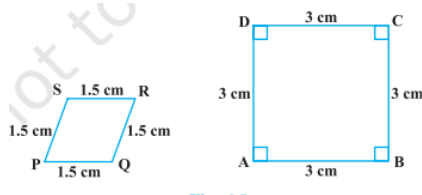
Based on the above information, answer the following questions.

- (i) The water tower cast a shadow of 25 m. At the same time, a tree near it casts a shadow of 5 m. What is the height of the tree?
- (a) 3.12 m  
(b) 8 m  
(c) 20 m  
(d) 25 m
- (ii) A scale model of the water tower of 100 cm height is created. The height of its pillars is 75 cm each. What is the height of a pillar (in m) in the actual water tower?
- (a) 7.5  
(b) 25  
(c) 30  
(d) 53.4
- (iii) Dharmendra made a scale model of a water tower for another locality. The radius of the reservoir in the model is 6 cm and its volume is  $216\text{cm}^3$ . The radius of the actual water reservoir is 2.5 m. What is its volume?

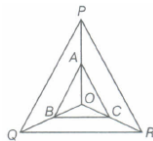
5 Marks

134 x 5 = 670

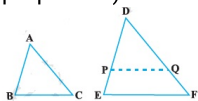
- 393) State whether the following quadrilaterals are similar or not.



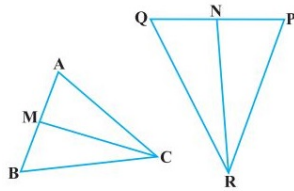
- 394) In the given figure, A, B and C are points on OP, OQ and OR respectively, such that  $AB \parallel PQ$  and  $AC \parallel PR$ . Show that  $BC \parallel QR$ .



- 395) The diagonals of a quadrilateral ABCD intersect each other at the point O, such that  $\frac{AO}{BO} = \frac{CO}{DO}$ . Show that ABCD is a trapezium.
- 396) Diagonals AC and BD of a trapezium ABCD with  $AB \parallel DC$  intersect each other at the point O. Using a similarity criterion for two triangles, show that  $\frac{OA}{OC} = \frac{OB}{OD}$ .
- 397) D is a point on the side BC of  $\triangle ABC$  such that  $\angle ADC = \angle BAC$ . Show that  $CA^2 = CB \times CD$ .
- 398) A vertical pole of length 6 m casts a shadow 4 m long on the ground and at the same time a tower casts a shadow 28 m long. Find the height of the tower.
- 399) Sides AB and AC and median AD of  $\triangle ABC$  are respectively proportional to sides PQ and PR and median PM of another  $\triangle PQR$ . Show that  $\triangle ABC \sim \triangle PQR$ .
- 400) If in two triangles, corresponding angles are equal, then their corresponding sides are in the same ratio (or proportion) and hence the two triangles are similar.

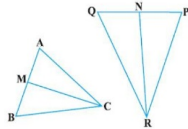


- 401) In figure CM and RN are respectively the medians of  $\triangle ABC$  and  $\triangle PQR$ . If  $\triangle ABC \sim \triangle PQR$ , prove that :  
 $\triangle AMC \sim \triangle PNR$

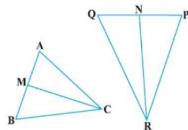


- 402) If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, the other two sides are divided in the same ratio.

- 403) In figure CM and RN are respectively the medians of  $\triangle ABC$  and  $\triangle PQR$ . If  $\triangle ABC \sim \triangle PQR$ , prove that :  
 $\frac{CM}{RN} = \frac{AB}{PQ}$



- 404) In figure CM and RN are respectively the medians of  $\triangle ABC$  and  $\triangle PQR$ . If  $\triangle ABC \sim \triangle PQR$ , prove that :  
 $\triangle CMB \sim \triangle RNQ$



- 405) If  $\triangle ABC \sim \triangle DFE$  ,  $\angle A = 30^\circ$  ,  $\angle C = 50^\circ$  , AB = 5 cm, AC = 8 cm and DF = 75 cm, then find DE and  $\angle F$

- 406) A 15 m high tower casts a shadow 24 m long at a certain time and at the same time, telephone pole casts a shadow 16 m long. Find the height of the telephone pole.

- 407) Let  $\triangle ABC \sim \triangle DEF$  and their areas be respectively  $64 \text{ cm}^2$  and  $121 \text{ cm}^2$  If EF = 15.4 cm then find BC.

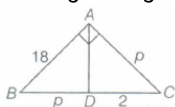
- 408) Two trees of heights x and y are d m apart.  
 (i) Prove that the height of the point of intersection of the line joining the top of each tree to the foot of the opposite trees is given by  $\frac{xy}{x+y}m$   
 (ii) Which mathematical concept is used in this problem?  
 (iii) What are the values depicted here?

- 409) Shweta prepared two posters on National Integration for decoration on Independence day on triangular sheets (say ABC and DEF). The sides AB and AC and the perimeter  $P_1$  of  $\triangle ABC$  are respectively four times the corresponding sides DE and DF and the perimeter  $P_2$  of  $\triangle DEF$  . Are the two triangular sheets similar? If yes, find  $\frac{ar(\triangle ABC)}{ar(\triangle DEF)}$  . What values can be indicated through celebration of national festivals?

- 410) A man steadily goes 8 m due East and then 6 m due North.

- (i) Find the distance from initial point to last point.  
 (ii) Which mathematical concept is used in this problem?  
 (iii) What value is indicated in this question?

- 411) In the given figure, if  $\triangle ADB \sim \triangle ADC$  , then find the value of p.



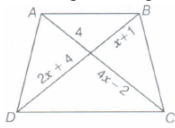
- 412) Prove that the line segments joining the mid-points of the sides of a triangle form four triangles, each of which is similar to the original triangle.

- 413) ABCD is a trapezium with  $AB \parallel DC$  . If  $\triangle AED \sim \triangle BEC$  , then prove that AD = BC.

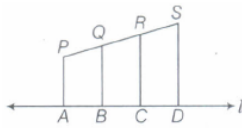
- 414) In a  $\triangle ABC$  , P and Q are points in AB and AC, respectively and  $PQ \parallel BC$  . Prove that the median bisects PQ.



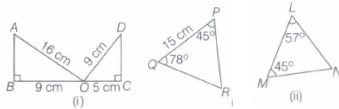
- 415) In the given figure, if  $AB \parallel CD$ , then find the value of  $x$ .



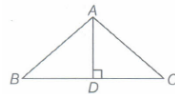
- 416) In the given figure, PA, QB, RC and SD are all perpendiculars to a line  $l$ ,  $AB = 6$  cm,  $BC = 9$  cm,  $CD = 12$  cm and  $SP = 36$  cm. Find PQ, QR and RS.



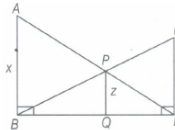
- 417) State whether the given pairs of triangles are similar or not. In case of similarity, mention the criterion.



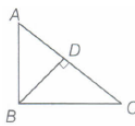
- 418) In the given figure, if  $\angle BAC = 90^\circ$  and  $AD \perp BC$ , prove that  $AD^2 = BD \cdot CD$ .



- 419) In the given figure,  $AB \parallel PQ \parallel CD$ ,  $AB = x$  units,  $CD = y$  units and  $PQ = z$  units. Prove that  $\frac{1}{x} + \frac{1}{y} = \frac{1}{z}$ .



- 420) In the adjoining figure, ABC is a triangle right angled at B and  $BD \perp AC$ . If  $AD = 4$  cm and  $CD = 5$  cm, find BD and AB.



- 421) Prove that the area of an equilateral triangle described on one side of a square is equal to half the area of any equilateral triangle described on one its diagonals.

- 422) AD is an altitude of an equilateral  $\triangle ABC$ . In AD as base another equilateral triangle is ADE is constructed. Prove that  $ar(\triangle ADE) = ar(\triangle ABC) = 3 : 4$ .

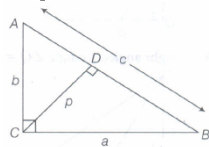
- 423) A ladder 17 m long, reaches at a window of a building 15 m above the ground. Find the distance of the foot of the ladder from the building.

- 424) In  $\triangle PQR$ ,  $PD \perp QR$  such that D lies on QR. If  $PQ = a$ ,  $PR = b$ ,  $QD = c$  and  $DR = d$ , then prove that  $(a + b)(a - b) = (c + d)(c - d)$ .

- 425)  $\triangle ABC$  is a right triangle in which  $\angle C = 90^\circ$  and  $CD \perp AB$ . If  $BC = a$ ,  $CA = b$ ,  $AB = c$  and  $CD = p$ , then prove that

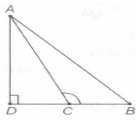
(i)  $cp = ab$

(ii)  $\frac{1}{p^2} = \frac{1}{a^2} + \frac{1}{b^2}$

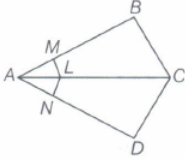


- 426) D is a point on the side BC of an equilateral triangle ABC, such that  $DC = \frac{1}{4}BC$ . Prove that  $AD^2 = 13CD^2$ .

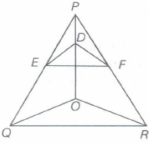
- 427) In  $\triangle ABC$ ,  $\angle C$  is an obtuse angle,  $AD \perp BC$  and  $AB^2 = AC^2 + 3BC^2$ . Prove that  $BC = CD$ .



- 428) In the given figure, if  $LM \parallel CB$  and  $LN \parallel CD$ , prove that  $\frac{AM}{AB} = \frac{AN}{AD}$ .

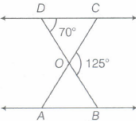


- 429) In the given figure,  $DE \parallel OQ$  and  $DF \parallel OR$ . Show that  $EF \parallel QR$ .



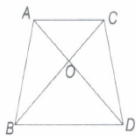
- 430) ABCD is a trapezium, in which  $AB \parallel DC$  and its diagonals intersect each other at the point O. Show that  $\frac{AO}{BO} = \frac{CO}{DO}$ .

- 431) In the given figure,  $\triangle ODC \sim \triangle OBA$ ,  $\angle BOC = 125^\circ$  and  $\angle CDO = 70^\circ$ . Find  $\angle DOC$ ,  $\angle DCO$  and  $\angle OAB$ .



- 432) Diagonals of a trapezium ABCD with  $AB \parallel DC$  intersect each other at the point O. If  $AB = 2CD$ , then find the ratio of the areas of  $\triangle AOB$  and  $\triangle COD$ .

- 433) In the given figure, ABC and DBC are two triangles on the same base BC. If AD intersects BC at O, then show that  $\frac{ar(\triangle ABC)}{ar(\triangle DBC)} = \frac{AO}{DO}$ .



- 434) If the areas of two similar triangles are equal, then prove that they are congruent.

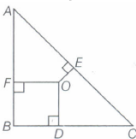
- 435) D, E and F are respectively the mid-points of sides AB, BC and CA of  $\triangle ABC$ . Find the ratio of the areas of  $\triangle DEF$  and  $\triangle ABC$ .

- 436) Prove that the area of an equilateral triangle described on one side of a square is equal to half the area of an equilateral triangle described on one of its diagonals.

- 437) ABC is an equilateral triangle of side 2a. Find each of its altitudes.

- 438) Prove that the sum of the squares of the sides of a rhombus is equal to the sum of the squares of its diagonals.

- 439) In the given figure, O is a point in the interior of a  $\triangle ABC$ ,  $OD \perp BC$ ,  $OE \perp AC$  and  $OF \perp AB$ .



$$OA^2 + OB^2 + OC^2 - OD^2 - OE^2 - OF^2 = AF^2 + BD^2 + CE^2$$

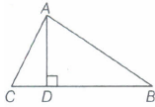
- 440) A ladder 10 m long reaches a window 8 m above the ground. Find the distance of the foot of the ladder from base of the wall.

- 441) An aeroplane leaves an airport and flies due North at a speed of 1000 km/h. At the same time, another aeroplane leaves the same airport and flies due West at a speed of 1200 km/h. How far apart will be the two planes after  $1\frac{1}{2}$  h?

- 442) Two poles of heights 6 m and 11 m stand on a plane ground. If the distance between the feet of the poles is 12 m, find the distance between their tops.

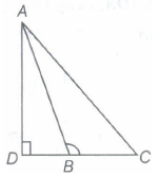
- 443) D and E are points on the sides CA and CB respectively of  $\triangle ABC$  right angled at C. Prove that  $AE^2 + BD^2 = AB^2 + DE^2$

- 444) The perpendicular from A on side BC of a  $\triangle ABC$  intersects BC at D such that  $DB = 3 CD$  (see figure).  
Prove that  $2 AB^2 = 2 AC^2 + BC^2$

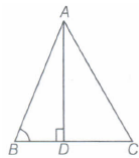


- 445) In an equilateral triangle, prove that three times the square of one side is equal to four times the square of one of its altitudes.

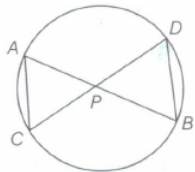
- 446) In the given figure, ABC is a triangle in which  $\angle ABC > 90^\circ$  and  $AD \perp CB$  produced. Prove that  $AC^2 = AB^2 + BC^2 + 2 BC \cdot BD$



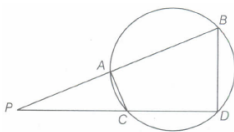
- 447) In the given figure, ABC is a triangle in which  $\angle ABC < 90^\circ$  and  $AD \perp BC$ . Prove that  $AC^2 = AB^2 + BC^2 - 2 BC \cdot BD$



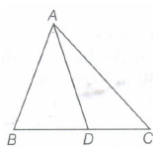
- 448) In the adjoining figure, two chords AB and CD intersect each other at the point P. Prove that  $\triangle APC \sim \triangle DPB$



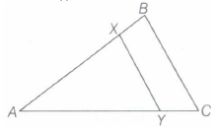
- 449) In the given figure, two chords AB and CD of a circle intersect each other at the point P (when produced) outside the circle. Prove that  $\triangle PAC \sim \triangle PDB$



- 450) In the given figure, D is a point on side BC of  $\triangle ABC$ , such that  $\frac{BD}{CD} = \frac{AB}{AC}$ . Prove that AD is the bisector of  $\angle BAC$ .

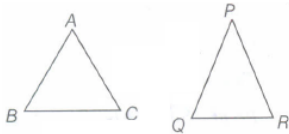


- 451) There is a triangular park ABC in a colony (as shown in figure). The Resident Welfare Association of the colony wishes to divide this park into two parts of equal areas - one for planting trees and raising a lawn and the other for providing place for children playing activities. One of the members Salma suggested to draw a line segment  $XY \parallel BC$  for this purpose.



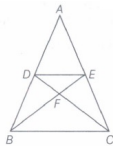
- (i) State how this line segment XY can be drawn, so that X and Y lie on AB and AC, respectively?  
(ii) What value is depicted from this action?

- 452) Consider two similar  $\triangle ABC$  and  $\triangle PQR$  as shown in the following figure.

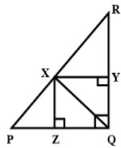


- (i) Prove that, if the areas of  $\triangle ABC$  and  $\triangle PQR$  are equal, then the  $\triangle ABC$  and  $\triangle PQR$  are always congruent.  
(ii) If the sides of two similar triangles are in the ratio 2 : 5, then find the ratio of the areas of these triangles.  
(iii) If the shape of the two triangles are same but size is different, then both the triangles are congruent. Is this statement true? Justify it.  
(iv) Suppose, a person wants to select the triangle having maximum area. For maximum area, he has to select the  $\triangle PQR$ . What his decision shows?

- 453) In the given figure, if  $DE \parallel BC$  and  $AD : DB = 5 : 4$ , then find  $\frac{\text{ar}(\triangle DFE)}{\text{ar}(\triangle CFB)}$ .



- 454)

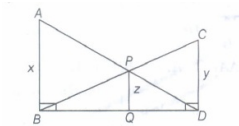


$\triangle PQR$  is right angled at Q.  $QX \perp PR$ ,  $XY \perp RQ$  and  $XZ \perp PQ$  are drawn. Prove that  $XZ^2 = PZ \times ZQ$ .

- 455) In  $\triangle ABC$ , the mid-points of sides BC, CA and AB are D, E and F respectively. Find ratio of  $\text{ar}(\triangle DEF)$  to  $\text{ar}(\triangle ABC)$ .  
456) In  $\triangle ABC$ , if  $\angle ADE = \angle B$ , then prove that  $\triangle ADE \sim \triangle ABC$ . Also, if  $AD = 7.6$  cm,  $AE = 7.2$  cm,  $BE = 4.2$  cm and  $BC = 8.4$  cm, then find DE.  
457) In the figure,  $\angle BED = \angle BDE$  and E is the middle point of BC. Prove that  $\frac{AF}{CF} = \frac{AD}{BE}$ .  
458) In the right triangle, B is a point on AC such that  $AB + AD = BC + CD$ . If  $AB = x$ ,  $BC = h$  and  $CD = d$ , then find x (in term of h and d).  
459) In  $\triangle ABC$ , AD is a median and O is any point on AD. BO and CO on producing meet AC and AB at E and F respectively. Now AD is produced to X such that  $OD = DX$  as shown in figure.  
Prove that:  
(i)  $EF \parallel BC$   
(ii)  $AO : AX = AF : AB$   
460) ABCO is a rhombus whose diagonal AC makes an angle  $\alpha$  with AB. If  $\cos \alpha = \frac{2}{3}$  and  $OB = 3$  cm find the length of its diagonals AC and BD.  
461) Triangle ABC is right angled at B and O is the mid-point BC. Prove that  $AC^2 = 4AD^2 - 3AB^2$ .  
462) If the area of two similar triangles are equal. prove that they are congruent.  
463) In  $\triangle ABC$ , AD is the median to BC and in PQR, PM is the median to QR. If. Prove that  $\triangle ABC \sim \triangle PQR$ .

464) In the following figure,  $\triangle FEC \cong \triangle GBD$  and  $\angle 1 = \angle 2$ . Prove that  $\triangle ADE \sim \triangle ABC$ .

465) In the given figure,  $AB \parallel PQ \parallel CD$ ,  $AB = x$  units,  $CD = y$  units and  $PQ = z$  units, prove that  $\frac{1}{x} + \frac{1}{y} = \frac{1}{z}$ .



466) In the given figure, D and E trisect BC. Prove that  $8AE^2 = 3AC^2 + 5AD^2$ .

467) Let ABC be a triangle and D and E be two points on side AB such that  $AD = BE$ . If  $DP \parallel BC$  and  $EQ \parallel AC$ , then prove that  $PQ \parallel AB$ .

468) Prove that the ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding medians.

469) Prove that in a right triangle, the square of the hypotenuse is equal to sum of squares of other two sides. Using the above result, prove that, in rhombus ABCD,  $4AB^2 = AC^2 + BD^2$ .

470) Vertical angles of two isosceles triangles are equal. If their areas are in the ratio 16 : 25, then find the ratio of their altitudes drawn from vertex to the opposite side.

471) In the figure, ABC is a right triangle, right angled at B. AD and CE are two medians drawn from A and C respectively. If  $AC = 5$  cm and  $AD = \frac{3\sqrt{5}}{2}$  cm, find the length of CE.

472) If a line drawn parallel to one side of a triangle to intersect the other two sides in distinct points, the other two sides are divided in the same ratio. Prove it.

473) In a trapezium ABCD,  $AB \parallel DC$  and  $DC = 2AB$ .  $EF \parallel AB$ , where E and F lie on BC and AD respectively such that  $\frac{BE}{EC} = \frac{4}{3}$ . Diagonal DB intersects EF at G. Prove that,  $7EF = 11AB$ .

474) In ABC,  $AD \perp BC$  and point D lies on BC such that  $2DB = 3CD$ . Prove that  $5AB^2 = 5AC^2 + BC^2$ .

475) There are three villages A, B and C such that the distance from A to B is 7 km, from B to C is 5 km and C to A is 8 km. The gram-pradhan wants to dig a well in such a way that the distance of the well from each village is equal.

(i) Which mathematical concept is used to solve the above question?

(ii) What should be the location of the well?

(iii) Which value is depicted by gram-pradhan?

476) A vertical row of trees 12m long casts a shadow 8m long on the ground. At the same time a tower casts the shadow 40 m long on the ground.

(i) Determine the height of the tower.

(ii) Which mathematical concept is used in this problem?

(iii) What is the value of the trees in our life?

477) Two trees of height a and b metre apart.

(i) Prove that the height of the point of intersection of the lines joining the top of each tree to the foot of the opposite trees is given by  $\frac{ab}{a+b} m$ .

(ii) Which mathematical concept is used in this problem?

(iii) What is the value of trees in our life?

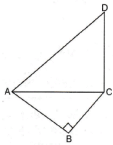
478) Show that in a right angle, the square of the hypotenuse is equal to the sum of the squares of the other two sides.

479) A ladder reaches a window which is 12 m above the ground on one side of the street, keeping its foot at the same point, the ladder is turned to the other side of the street to reach a window 9 m high. Find the width of the street if the length of the ladder is 15 m.

480) A ladder 25 m long reaches a window of a building 20 m above the ground. Determine the distance of the foot of the ladder from the building.

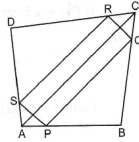
481) A ladder is placed in such a way that its foot is at a distance of 5 m from a wall and its tip reaches a window 12 m above the ground. Determine the length of the ladder.

- 482) In a quadrilateral ABCD,  $\angle B = 90^\circ$ ,

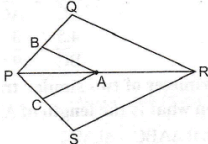


$AD^2 = AB^2 + CD^2 + BC^2$ . prove that  $\angle ACD = 90^\circ$ .

- 483) In the given fig. ABCD is a quadrilateral P, Q, R and S are the points of trisection of the sides AB, BC, CD and DA respectively. Prove that PQRS is a parallelogram.

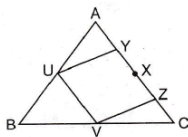


- 484) In figure,  $BA \parallel QR$ , and  $CA \parallel SR$ .



Prove that  $\frac{QB}{BP} = \frac{SC}{CP}$

- 485) In  $\triangle ABC$ , X is any point on AC. If Y, Z, U and V are the middle points on AX, XC, AB and BC respectively, then, prove that  $UY \parallel VZ$  and  $UV \parallel YZ$ .



- 486) In figure,  $LM \parallel NO$  and  $LN \parallel PQ$ . If  $MP = \frac{1}{3} MN$  find the ratio of the areas of  $\triangle LMN$  and  $\triangle QNP$ .

- 487) Equiangular triangles are drawn on the sides of right angled triangle in which perpendicular is double of the base. Show that area of the triangle on the hypotenuse is the sum of the areas of the other two triangles.

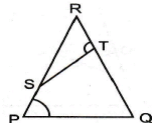
- 488) ABCD is a trapezium in which AB is parallel to DC and the diagonals AC, BD cut at X. A line is drawn through C parallel to DA to cut DB, produced if necessary at Y. Prove that :

(i)  $\triangle AXD$ ,  $\triangle BXC$  are equal in area

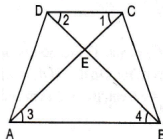
(ii)  $\triangle AXD \sim \triangle CXY$

(iii)  $\frac{XB}{XY} = \frac{XA^2}{XC^2}$

- 489) If  $\angle P = \angle RTS$ ,  
Then show that  $\angle PQR = \angle RST$

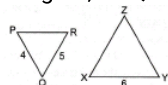


- 490) In fig  $\angle 1 = \angle 3$ ,  $\angle 2 = \angle 4$

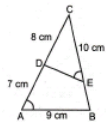


$DE = 4$ ,  $CE = x + 1$ ,  $AE = 2x + 4$ ,  $BE = 4x - 2$ . Find x.

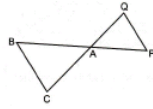
- 491) In figure,  $\triangle PQR \sim \triangle XYZ$ . If  $PQ = 4$  cm,  $QR = 5$  cm and  $XY = 6$  cm, then find YZ



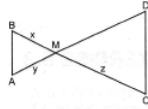
- 492) In the figure, if  $\angle A = \angle CED$ ,  $AB = 9\text{ cm}$ ,  $AD = 7\text{ cm}$ ,  $CD = 8\text{ cm}$  and  $CE = 10\text{ cm}$ . Find  $DE$ .



- 493) In the given figure,  $\triangle ACB \sim \triangle AQP$ . If  $BC = 8\text{ cm}$ ,  $PQ = 4\text{ cm}$ ,  $BA = 6.5\text{ cm}$ .  $AQ = 2.8\text{ cm}$ , find  $CA$  and  $PA$ .

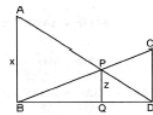


- 494) In the given figure,  $\triangle AMB \sim \triangle CMD$

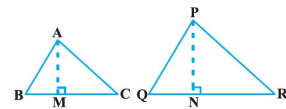


Determine  $MD$  in terms of  $x$ ,  $y$  and  $z$ .

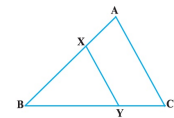
- 495) In figure  $AB \parallel PO \parallel CD$ ,  $AB = x$  units,  $CD = y$  units and  $PQ = z$  units, prove that  $\frac{1}{x} + \frac{1}{y} = \frac{1}{z}$



- 496) The ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding sides. We are given two triangles  $ABC$  and  $PQR$  such that  $\triangle ABC \sim \triangle PQR$ .



- 497) In the line segment  $XY$  is parallel to side  $AC$  of  $\triangle ABC$  and it divides the triangle into two parts of equal areas. Find the ratio  $\frac{AX}{AB}$ .

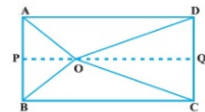


- 498) In a right triangle, the square of the hypotenuse is equal to the sum of the squares of the other two sides.

- 499) In a triangle, if square of one side is equal to the sum of the squares of the other two sides, then the angle opposite the first side is a right angle.

- 500) A ladder is placed against a wall such that its foot is at a distance of  $2.5\text{ m}$  from the wall and its top reaches a window  $6\text{ m}$  above the ground. Find the length of the ladder.

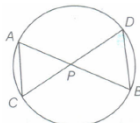
- 501)  $O$  is any point inside a rectangle  $ABCD$ . Prove that  $OB^2 + OD^2 = OA^2 + OC^2$ .



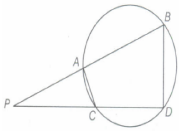
- 502)  $PQR$  is a triangle right angled at  $P$  and  $M$  is a point on  $QR$  such that  $PM \perp QR$ . Show that  $PM^2 = QM \cdot MR$ .

- 503) Prove that the sum of the squares of the diagonals of parallelogram is equal to the sum of the squares of its sides.

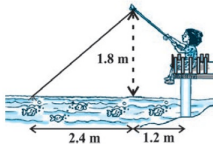
- 504) In the adjoining figure, two chords  $AB$  and  $CD$  intersect each other at the point  $P$ . Prove that  $AP \cdot PB = CP \cdot DP$



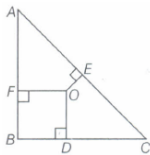
- 505) In the given figure, two chords AB and CD of a circle intersect each other at the point P (when produced) outside the circle. Prove that  
 $PA \cdot PB = PC \cdot PD$



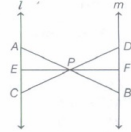
- 506) Nazima is fly fishing in a stream. The tip of her fishing rod is 1.8 m above the surface of the water and the fly at the end of the string rests on the water 3.6 m away and 2.4 m from a point directly under the tip of the rod. Assuming that her string (from the tip of her rod to the fly) is taut, how much string does she have out see Figure? If she pulls in the string at the rate of 5 cm per second, what will be the horizontal distance of the fly from her after 12 seconds?



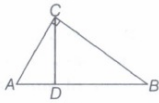
- 507) In the given figure, O is a point in the interior of a  $\triangle ABC$ ,  $OD \perp BC$ ,  $OE \perp AC$  and  $OF \perp AB$ .  
 $AF^2 + BD^2 + CE^2 = AE^2 + CD^2 + BF^2$



- 508) In the given figure,  $l \parallel m$  and line segments AB, CD and EF are concurrent at point P. Prove that  
 $\frac{AE}{BF} = \frac{AC}{BD} = \frac{CE}{FD}$



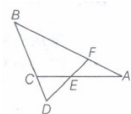
- 509) PQRS is a trapezium with  $PQ \parallel SR$ . Diagonals PR and SQ intersect at M and  $\triangle PMS \sim \triangle QMR$ . Prove that  $PS = QR$ .
- 510) The ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding sides.
- 511) If a perpendicular is drawn from the vertex of right angle of a right angled triangle to the hypotenuse; then triangles on both sides of the perpendicular are similar to the whole triangle and to each other.
- 512) In figure,  $\angle ACB = 90^\circ$  and  $CD \perp AB$  prove that  $CD^2 = BD \times AD$ .



- 513) A farmer has a piece of land in the shape of an equilateral triangle. He divides his entire land among his four children in equal parts as shown in following figure. P, Q and R are mid-points of sides AB, BC and AC respectively. A student find that ratio of area of  $\triangle PQR$  to the area of  $\triangle ABC$  is 2 : 3. Using properties of similar triangles, a student of class X at once said, "It is false".

- (i) Do you agree with student?  
 (ii) Verify  $PQ = \frac{1}{2}BC$

- 514) In the given figure,  $\angle AEF = \angle AFE$  and E is the mid-point of CA. Prove that  $\frac{BD}{CD} = \frac{BF}{CE}$



- 515) D is the mid-point of side BC of a  $\triangle ABC$ . AD is bisected at the point E and BE produced cuts AC at the point X.