

papergrid

Date: / /

$$1) \begin{cases} x + y = 5 \\ 2x + 2y = 10 \end{cases}$$

$$x = 5 - y$$

$$2(5 - y) + 2y = 10$$

$$10 - 2y + 2y = 10$$

No solution

$$7x - 15y = 2 \quad \text{--- (1)}$$

$$x + 2y = 3 \quad \text{--- (2)}$$

x - form in Eq (2)

$$x + 2y = 3$$

$$x = 3 - 2y$$

Putting $x = 3 - 2y$ in Eq (1)

$$7x - 15y = 2$$

$$7(3 - 2y) - 15y = 2$$

$$21 - 14y - 15y = 2$$

$$-29y = 2 - 21$$

$$+29y = +19$$

$$y = \frac{19}{29}$$

Putting $y = \frac{19}{29}$ in x - form

$$x = 3 - 2\left(\frac{19}{29}\right)$$

$$x = \frac{3}{1} - \frac{38}{29}$$

$\times 29 \quad \times 1$

$$x = \frac{87 - 38}{29}$$

$$x = \frac{49}{29}$$

$$\left(\frac{49}{29}, \frac{19}{29}\right)$$

$$4x + 3y = 25 \quad \text{--- (2)}$$

$$3x + 4y = 24 \quad \text{--- (1)}$$

Step 1 : $3x + 4y = 24$

$$3x = 24 - 4y$$

$$x = \frac{24 - 4y}{3}$$

x-form

Step : 2 Putting equation (2) in equation (1)

$$4x + 3y = 25$$

$$4\left(\frac{24 - 4y}{3}\right) + 3y = 25$$

$$\begin{array}{r} 96 \\ 75 \\ \hline 21 \end{array}$$

$$4(24 - 4y) + 3y = 25 \times 3$$

$$4(24 - 4y) + 3y = 75$$

$$96 - 4y + 3y = 75$$

$$96 - 7y = 75$$

$$96 - 75 = 7y$$

$$21 = 7y$$

$$y = \frac{21}{7} = 3$$

Step :- Putting $y = 3$ in x-form

$$x = \frac{24 - 4(3)}{3}$$

$$x = \frac{24 - 12}{3}$$

$$x = \frac{12}{3} = 4$$

Ans = (4, 3)

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$$5 \quad \frac{3x}{x^2} - \frac{5y}{x^2} = \frac{-2}{x^6}$$

$$\frac{x}{3} + \frac{y}{2} = 13$$

$$9x - 10y = -12 \quad \text{--- (1)}$$

$$2x + 3y = 13 \quad \text{--- (2)}$$

x -form in Eq (2)

$$2x + 3y = 13$$

$$2x = 13 - 3y$$

$$x = \frac{13 - 3y}{2}$$

Putting x -form in Eq (1)

$$9x - 10y = -12$$

$$9\left(\frac{13 - 3y}{2}\right) - 10y = -12$$

$$\frac{117 - 27y}{2} - 10y = -12$$

$$117 - 37y = -12 \times 2$$

$$117 - 37y = -24$$

$$-37y = -24 - 117$$

$$+37y = -141$$

$$y = \frac{-141}{37}$$

$$y = 3$$

Putting $y = 3$ in x -form

$$x = \frac{13 - 3(3)}{2}$$

$$x = \frac{4}{2}$$

$$x = 2$$

$$(2, 3)$$

Cross-multiplication

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$$\begin{aligned} 1 \quad 8x + 5y &= 9 \\ 3x + 2y &= 4 \end{aligned}$$

$$8x + 5y - 9 = 0$$

$$3x + 2y - 4 = 0$$

x		y		1
5	-9	8		5
2	-4	3		2

x	y	1
$5(-4) - 2(-9)$	$-9(3) - (-4)(8)$	$8(3) - 3(5)$

x	y	1
$-20 + 18$	$-27 + 32$	$16 - 15$

x	y	1
-2	5	1

Now $\frac{x}{-2} = \frac{1}{1}$ $\frac{y}{5} = \frac{1}{1}$

$$x = -2 \qquad y = 5$$
$$(x, y) = (-2, 5)$$

$$x - 3y - 7 = 0$$

$$3x - 3y - 15 = 0$$

<u>x</u>	<u>y</u>	<u>1</u>
-3	-7	1
-3	-15	3

<u>x</u>	<u>y</u>	<u>1</u>
$-3(-15) - (-3)(-7)$	$-7(3) - (-15)(1)$	$1(-3) - (3)(-7)$

<u>x</u>	<u>y</u>	<u>1</u>
45 - 21	-21 + 15	-3 + 9

<u>x</u>	<u>y</u>	<u>1</u>
24	-6	6

$$\frac{x}{24} = \frac{1}{6}$$

$$\frac{y}{-6} = \frac{1}{6}$$

$$x = \frac{24}{6}$$

$$y = \frac{-6}{6}$$

$$(4, -1)$$

2 $7x + 4y = 12$
 $3x + 4y = -4$

$7x + 4y - 12 = 0$
 $3x + 4y + 4 = 0$

x		y		1
7 4		-12	7	4
3		4	3	4

$\frac{x}{4(4) - 4(-12)} = \frac{y}{-12(3) - 4(7)} = \frac{1}{7(4) - 3(4)}$

$\frac{x}{16 + 48} = \frac{y}{-36 - 28} = \frac{1}{28 - 12}$

$\frac{x}{64} = \frac{y}{-64} = \frac{1}{16}$

$\frac{x}{64} = \frac{1}{16}$ $\frac{y}{-64} = \frac{1}{16}$

$x = \frac{64}{16}$ $y = \frac{-64}{16}$

$x = 4$ $y = -4$

$(4, -4)$

$$\begin{cases} 4x + 3y = 28 \\ 9x - 5y = 63 \end{cases}$$

$$\begin{cases} 4x + 3y - 28 = 0 \\ 9x - 5y - 63 = 0 \end{cases}$$

x		y		1
3		-28	4	3
-5		-63	9	-5

$$\frac{x}{3(-63) - (-28)(9)} = \frac{y}{-28(9) - 63(-54)} = \frac{1}{4(-5) - 9(3)}$$

$$\frac{x}{-189 - 140} = \frac{y}{-252 + 252} = \frac{1}{-20 - 27}$$

$$\frac{x}{-329} = \frac{y}{0} = \frac{1}{-47}$$

$$\frac{x}{-329} = \frac{1}{-47} \qquad \frac{y}{0} = \frac{1}{-47}$$

$$x = \frac{7}{+329} \cdot \frac{+47}{+47}$$

$$y = \frac{0}{-47}$$

$$x = 7$$

$$y = 0$$

$$(7, 0)$$

$$3x - 5y = 3 \times 3$$

$$2x + 3y = -17 \times 5$$

$$9x - 15y = 9$$

$$10x + 15y = -85$$

$$19x = \cancel{94} 76$$

$$x = \frac{76}{19}$$

$$x = 4$$

Putting $x = 4$ in (1)

$$3(-4) - 5y = 3$$

$$-12 - 5y = 3$$

$$-5y = 3 + 12$$

$$-5y = 15$$

$$y = \frac{15}{-5}$$

$$y = -3$$

$$3x + 2y = 53 \quad \times 3$$

$$2x + 3y = 47 \quad \times 2$$

$$9x + 6y = 159$$

$$4x + 6y = 94$$

53

 $\times 3$

159

47

2

94

$$5x = 65$$

$$x = \frac{65}{5} = 13$$

5

159

94

65

$$x = 13$$

Putting $x = 13$ in Equation (2)

$$2(13) + 3y = 47$$

$$26 + 3y = 47$$

$$3y = 47 - 26$$

$$3y = 21$$

$$y = \frac{21}{3}$$

3

$$y = 7$$

$$(x, y) = (13, 7)$$

$$\frac{1}{2x} + \frac{1}{3y} = 2$$

$$\frac{1}{3x} + \frac{1}{2y} = \frac{13}{6}$$

Comparing

$$\frac{1}{2x} = a \quad \frac{1}{y} = b$$

$$\frac{1}{x} = 2 \quad \frac{1}{y} = 3$$

Let $\frac{1}{x} = a$ $\frac{1}{y} = b$

$$x = \frac{1}{2} \quad y = \frac{1}{3}$$

$$\therefore \frac{a}{2} + \frac{b}{3} = \frac{2}{6}$$

$$\left(\frac{1}{2}, \frac{1}{3} \right)$$

$$\frac{a}{3} + \frac{b}{2} = \frac{13}{6}$$

$$3a + 2b = 12 \quad \times 2$$

$$2a + 3b = 13 \quad \times 3$$

$$6a + 4b = 24$$

$$6a + 9b = 39$$

$$-5b = -15$$

$$b = \frac{15}{5}$$

$$b = 3$$

Putting $b = 3$ in Eq (1)

$$3a + 2(3) = 12$$

$$3a + 6 = 12$$

$$3a = 12 - 6$$

$$3a = 6$$

$$a = \frac{6}{3}$$

$$a = 2$$

$$\left(\frac{2}{3} \right)$$

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Comparing

$$\frac{5}{x-1} + \frac{1}{y-2} = 2$$

$$\frac{1}{x-1} = a$$

$$\frac{1}{y-2} = b$$

$$\frac{6}{x-1} - \frac{3}{y-2} = 1$$

$$\frac{1}{x-1} = \frac{1}{3}$$

$$\frac{1}{y-2} = \frac{1}{3}$$

$$\text{Let } \frac{1}{x-1} = a \quad \frac{1}{y-2} = b$$

$$x-1 = 3$$

$$y-2 = 3$$

$$5a + 1b = 2 \times 3$$

$$x = 3 + 1$$

$$y = 3 + 2$$

$$6a - 3b = 1$$

$$x = 4$$

$$y = 5$$

$$15a + 13b = 6$$

(4, 5)

$$6a - 3b = 1$$

$$21a = 7$$

$$a = \frac{7}{21}$$

$$a = \frac{1}{3}$$

Putting $a = \frac{1}{3}$ in Eq (1)

$$5a + b = 2$$

$$5 \left(\frac{1}{3} \right) + b = 2$$

$$6a - 3b = 1$$

$$\frac{2}{3} \left(\frac{1}{3} \right) - 3b = 1$$

$$2 - 3b = 1$$

$$-3b = 1 - 2$$

$$-3b = -1$$

$$b = \frac{-1}{-3}$$

$$\frac{1}{3x+y} + \frac{1}{3x-y} = \frac{3}{4}$$

$$\frac{1}{2(3x+y)} - \frac{1}{2(3x-y)} = \frac{-1}{8}$$

Comparing

$$\frac{1}{3x+y} = a \quad \frac{1}{3x-y} = b$$

$$\frac{1}{3x+y} = \frac{1}{4} \quad \frac{1}{3x-y} = \frac{1}{2}$$

Let $\frac{1}{3x+y} = a$ & $\frac{1}{3x-y} = b$

$$3x+y = 4$$

$$3x-y = 2$$

$$6x = 6$$

$$x = 1$$

$$x = 1$$

$$x = 1$$

$$\frac{a}{x^4} + \frac{b}{x^4} = \frac{3}{x^4}$$

$$\frac{a}{2} - \frac{b}{2} = \frac{-1}{8}$$

$$4a + 4b = 3$$

$$4a - 4b = -1$$

$$8a = 2$$

$$a = \frac{2}{8}$$

$$a = \frac{1}{4}$$

Putting $x=1$ in Eq (1)

$$3(1) + y = 4$$

$$3 + y = 4$$

$$y = 4 - 3$$

$$y = 1$$

$$(1, 1)$$

Putting $a = \frac{1}{4}$ in Eq (2)

$$4\left(\frac{1}{4}\right) + 4b = 3$$

$$1 + 4b = 3$$

$$4b = 3 - 1$$

$$b = \frac{2}{4}$$

$$b = \frac{1}{2}$$

$$\frac{10}{x+y} + \frac{2}{x-y} = 4$$

$$\frac{15}{x+y} - \frac{5}{x-y} = -2$$

Let $\frac{1}{x+y} = a$ $\frac{1}{x-y} = b$

$$10a + 2b = 4 \times 5$$

$$15a - 5b = -2 \times 2$$

$$50a + 10b = 20$$

$$30a - 10b = -4$$

$$80a = 16$$

$$a = \frac{16}{80}$$

$$a = \frac{1}{5}$$

Putting $a = \frac{1}{5}$ in Eq (i)

$$2\left(\frac{1}{5}\right) + 2b = 4$$

$$2 + 2b = 4$$

$$2b = 4 - 2$$

$$b = \frac{2}{2}$$

$$b = 1$$

Comparing

$$\frac{1}{x+y} = a$$

$$\frac{1}{x-y} = b$$

$$\frac{1}{x+y} = \frac{1}{5}$$

$$\frac{1}{x-y} = 1$$

$$x + y = 5$$

$$x - y = 1$$

$$2x = 6$$

$$x = \frac{6}{2}$$

$$x = 3$$

$$x = 3$$

Putting $x = 3$ in (B)

$$3 + y = 5$$

$$y = 5 - 3$$

$$y = 2$$

(3, 2)

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$$1 \quad \begin{aligned} 3x + 4y &= 10 \\ 2x - 2y &= 2 \end{aligned}$$

$$\begin{aligned} 3x + 4y - 10 &= 0 \\ 2x - 2y - 2 &= 0 \end{aligned}$$

$$\begin{array}{ccc} a_1 = 3 & b_1 = 4 & c_1 = -10 \\ a_2 = 2 & b_2 = -2 & c_2 = -2 \end{array}$$

$$\frac{a_1}{a_2} = \frac{3}{2}$$

$$\frac{b_1}{b_2} = \frac{4}{-2} = -2$$

$$\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$$

∴ Equation has unique solution
→ Consistent & Independent graph

$$2 \quad \begin{aligned} 3x - 5y - 20 &= 0 \\ 6x - 10y - 40 &= 0 \end{aligned}$$

$$a_1 = 3$$

$$b_1 = -5$$

$$c_1 = -20$$

$$a_2 = 6$$

$$b_2 = -10$$

$$c_2 = -40$$

$$\frac{a_1}{a_2} = \frac{3}{6} = \frac{1}{2}$$

$$\frac{b_1}{b_2} = \frac{-5}{-10} = \frac{1}{2}$$

$$\frac{c_1}{c_2} = \frac{-20}{-40} = \frac{1}{2}$$

$$\therefore \frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$$

∴ Equation has infinitely many solutions
 ∴ Consistent & Dependent graph

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* Find missing values

$$1) \quad 4x + Py + 8 = 0$$

$$2x + 2y + 2 = 0$$

Find value of P Equation has unique solution

$$a_1 = 4$$

$$b_1 = P$$

$$c_1 = 8$$

$$a_2 = 2$$

$$b_2 = 2$$

$$c_2 = 2$$

Here Equation has unique solution

$$\therefore \frac{a_1}{a_2} \neq \frac{b_1}{b_2}$$

$$\therefore \frac{4}{2} \neq \frac{P}{2}$$

$$P \neq 4$$

$$3 \quad kx + 3y - (k-3) = 0$$

$$12x + ky - k = 0$$

Find value of k
 Equation has infinitely many solutions

$$a_1 = k \quad b_1 = 3 \quad c_1 = (-k+3) - (k-3)$$

$$a_2 = 12 \quad b_2 = k \quad c_2 = -k$$

Here Equation has infinitely many solutions

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2}$$

$$\frac{k}{12} = \frac{3}{k}$$

$$\sqrt{k^2} = \sqrt{36}$$

$$k = \pm 6$$

$$\frac{b_1}{b_2} = \frac{c_1}{c_2}$$

$$\frac{3}{k} = \frac{-(k-3)}{-k}$$

$$3 = k-3$$

$$6 = k$$

$$k = 6$$

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$$\therefore 48b - 6 = 42b$$

$$\therefore 48b - 42b = 6$$

$$\therefore 6b = 6$$

$$b = \frac{6}{6}$$

$$b = 1$$

$$\therefore a = 5b$$

$$a = 5(1)$$

$$a = 5$$

$$a = 5$$

$$b = 1$$

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IMP

Infinitely many solutions

$$4 \quad 2x + 3y = 7$$

$$(a-b)x + (a+b)y = 3a + b - 2$$

$$a_1 = 2$$

$$b_1 = 3$$

$$c_1 = 7$$

$$a_2 = a - b$$

$$b_2 = a + b$$

$$c_2 = 3a + b - 2$$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2}$$

$$\frac{2}{a-b} = \frac{3}{a+b}$$

$$2(a+b) = 3(a-b)$$

$$2a + 2b = 3a - 3b$$

$$2a - 3a = -3b - 2b$$

$$-a = -5b$$

$$a = 5b$$

Now

$$\frac{b_1}{b_2} = \frac{c_1}{c_2}$$

$$\frac{3}{a+b} = \frac{7}{3a+b-2}$$

$$3(3a+b-2) = 7(a+b)$$

$$9a + 3b - 6 = 7a + 7b \quad (a = 5b)$$

$$9(5b) + 3b - 6 = 35b + 7b$$

$$45b + 3b - 6 = 35b + 7b$$

No solution

$$3x + y = 1$$

$$(2k-1)x + (k-1)y = 2k + 1$$

$$a_1 = 3$$

$$b_1 = 1$$

$$c_1 = 1$$

$$a_2 = 2k-1$$

$$b_2 = k-1$$

$$c_2 = 2k + 1$$

Equation has no solution

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2}$$

$$\frac{3}{2k-1} = \frac{1}{k-1}$$

$$3(k-1) = 2k-1$$

$$3k - 3 = 2k - 1$$

$$3k - 2k = -1 + 3$$

$$k = 2$$