

CHAPTER 2

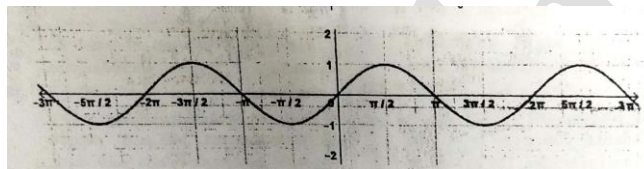
RELATIONS & FUNCTIONS

IMPROVEMENT 2019

1. a) If f is a signum function, then Consider a real valued function $f(100) = \dots\dots\dots$ (1)
- b) Let $f = \{(1,1), (2,3), (0,-1), (-1,-3)\}$ be a function from \mathbb{Z} to \mathbb{Z} defined by $f(x) = ax + b$, for some integers a and b . Determine a and b . (2)
- c) Let $g(x) = 2 - 3x, x \in \mathbb{R}, x > 0$ and $h(x) = x^2 - 3x + 2, x \in \mathbb{R}$ be two functions. Find: i) the range of $g(x)$ (2)
ii) domain of $\frac{g(x)}{h(x)}$. (1)

MARCH 2019

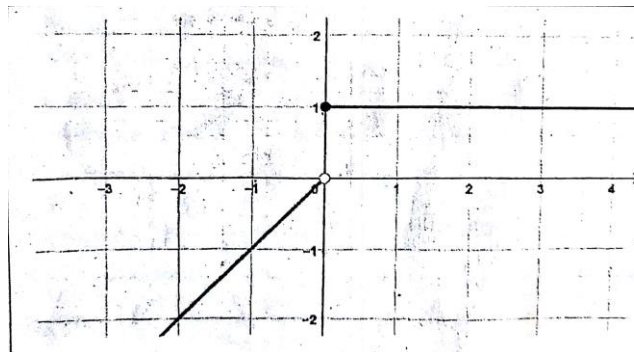
2. Consider the graph of the function $f(x)$



- a) Identify the function $f(x) = \dots\dots\dots$ (1)
 - i) $f(x) = \sin x$
 - ii) $f(x) = \cos x$
 - iii) $f(x) = \tan x$
 - iv) $f(x) = \operatorname{cosec} x$
- b) Using the function $f(x)$ find:

$$\lim_{x \rightarrow \frac{\pi}{2}} \frac{f(x) - f\left(\frac{\pi}{2}\right)}{x - \frac{\pi}{2}} \quad (2)$$

3. The figure shows the graph of the function $f(x)$.



- a) Write the domain and range of $f(x)$. (2)
- b) Find $f(0)$ and $f(-0.01)$. (1)
- c) Check the existence of $\lim_{x \rightarrow 0} f(x)$. [Chapter 13] (1)

IMPROVEMENT 2018

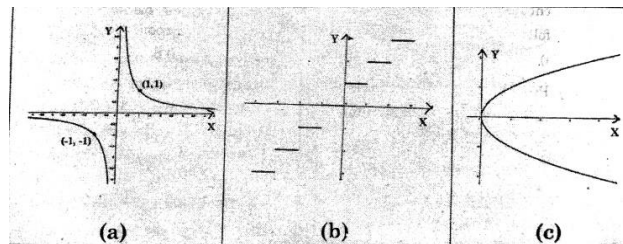
4. Consider a real valued function

$$f(x) = \frac{x-3}{x^2 - x - 6}.$$

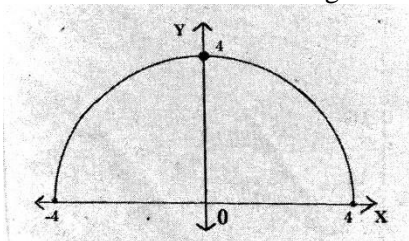
- a) Find the domain of $f(x)$ (2)
- b) Evaluate: $\lim_{x \rightarrow 3} f(x)$ (1)
[Chapter 13]
5. a) If $\left(\frac{x+3}{2}, \frac{y-1}{3}\right) = (4, 2)$, find the value of x and y . (2)
- b) Consider the function $f(x) = |x| - 3$, draw the graph of $f(x)$. (2)
- c) Write the domain and range of $f(x)$. (2)

MARCH 2018

6. Consider the following graphs:



- a) Which graph does not represent a function? (1)
- b) Identify the function $f(x) = \frac{1}{x}$ from the above graph. (1)
- c) Draw the graph of the function $f(x) = (x-1)^2$ (2)
7. The figure shows the graph of a function $f(x)$ which is a semi-circle centred at origin.



- a) Write the domain and range of $f(x)$. (2)
- b) Define the function $f(x)$. (2)

IMPROVEMENT 2017

8. a) $A = \{2, 3\}$, $B = \{1, 3, 5\}$ then the number of relations from A to B is (1)
- i) 2 ii) 32
iii) 64 iv) 62
- b) R is a relation defined on the set $A = \{1, 2, 3, \dots, 14\}$ by $R = \{(x, y) : 3x - y = 0, xy \in A\}$
Write the domain, co-domain and the range. (3)
- c) Let $f(x) = x^2$ and $g(x) = 2x + 1$ be two real functions. Find $(f \cdot g)(x)$ and $(f + g)(x)$. (2)

MARCH 2017

9. a) The domain of the function $f(x) = \frac{1}{x-1}$ is
i) $\{1\}$ ii) R

- iii) $R - \{1\}$ iv) $R - \{0\}$ (1)
- b) A relation R on the set of natural numbers is defined by $R = \{(x, y) : y = x; x \text{ is a natural number less than } 4, x, y \in N\}$
- i) Write the relation in Roster form. (1)
- ii) Write the domain and range of the relation. (2)
- c) Draw the graph of the function $f(x) = |x|, x \in R$ (2)

IMPROVEMENT 2016

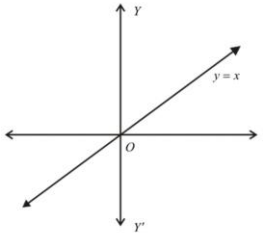
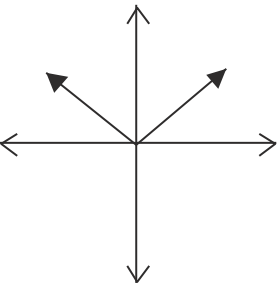
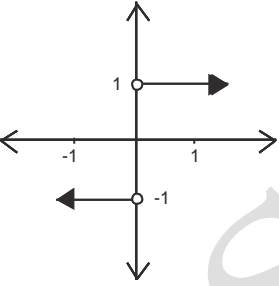
10. a) If $P = \{m, n\}$, $Q = \{n, m\}$; State whether the following is TRUE or FALSE.
 $P \times Q = \{(m, n), (n, m)\}$. (1)
- b) Write the relation $R = \{(x, x^3) : x \text{ is a prime number } < 10\}$, in roster form. (2)
- c) Let $A = \{1, 2, 3, 4\}$, $B = \{1, 5, 9, 11, 15, 16\}$ and $f = \{(1, 5), (2, 9), (3, 1), (4, 5), (2, 1)\}$. State with the reason whether f is a relation or a function. (3)

MARCH 2016

11. a) If $(x+1, y-2) = (3, 1)$, write the values of x and y. (1)
- b) Let $A = \{1, 2, 3, 4, 5\}$ and $B = \{4, 6, 9\}$ be two sets. Define a relation R from A to B by $R = \{(x, y) : x - y \text{ is a positive integer}\}$, find $(x+1, y-2) = (3, 1)$, and hence write R in the Roster form. (2)
- c) Define the modulus function. What is its domain? Draw a rough sketch. (3)

IMPROVEMENT 2015

12. a) Match the following: (3)

i)		1) Modulus function $f : R \rightarrow R$ by $f(x) = x $
ii)		2) Signum function $f : R \rightarrow R$ by $f(x) = \begin{cases} x & x \neq 0 \\ 0 & x = 0 \end{cases}$
iii)		3) Identity function $f : R \rightarrow R$ by $f(x) = x$
		4) Greatest integer function $f : R \rightarrow R$ by $f(x) = [x]$

- b) $A = \{1, 2, 3, \dots, 14\}$. R is a relation from A to A defined by $R = \{(x, y) : 3x - y = 0; x, y \in A\}$. Write the domain, range and co-domain of R. (3)

MARCH 2015

13. a) Find the domain and range of function

$$f(x) = \frac{x^2 + 3x + 5}{x^2 - 5x + 4} \quad (2)$$

- b) Sketch the graph of the function
 $f(x) = |x + 1|$ (1)
- c) Consider $A = \{1, 2, 3, 5\}$ and $B = \{4, 6, 9\}$. Define a relation $R : A \rightarrow B$ by
 $R = \{(x, y) : x - y \text{ is odd}, x \in A, y \in B\}$.
 Write R in roster form and find the range of R. (3)

IMPROVEMENT 2014

14. Let $A = \{1, 2, 3, 4, 5, 6\}$ be a set. Define a relation R from A to A by $R = \{(x, y) : y = x + 1\}$.

- a) Express R in roster form. (1)
- b) Represent the relation R using an arrow diagram. (1)
- c) Write the domain and range of R (1)
15. a) Let $A = \{1, 2, 3, 4\}$, $B = \{1, 5, 9, 11, 15, 16\}$ and
 $f = \{(1, 5), (2, 9), (3, 1), (4, 5), (2, 11)\}$
 Is f a function from A to B? Why? (1)
- b) Draw the graph of the function, $y = |x|$ (2)

MARCH 2014

16. a) Let $P = \{1, 2\}$ Find $P \times P \times P$.
- b) Let $A = \{1, 2, 3, \dots, 13, 14\}$. R is a relation on A defined by $R = \{(x, y) : 3x - y = 0; x, y \in A\}$
- i) Write R in roster form (1)
- ii) Find the domain and range of R (1)
17. a) Draw the graph of the function

$$f(x) = \begin{cases} 1, & \text{if } x > 0 \\ 0, & \text{if } x = 0 \\ -1, & \text{if } x < 0 \end{cases} \quad (3)$$

- b) Write the range of the above function. (1)

IMPROVEMENT 2013

18. Consider the function $f : R \rightarrow R$ defined by

$$f(x) = -|x|.$$

- a) Find the domain and range of f . (2)
b) Draw the graph of f . (2)

MARCH 2013

19. a) Let $A = \{7, 8\}$ and $B = \{5, 4, 2\}$,
Find $A \times B$ (1)
b) Determine the domain and range of the relation R defined by
 $R = \{(x, y) : y = x + 1, x \in \{0, 1, 2, 3, 4, 5\}\}$ (2)

20. Draw the graph of the function:

$$f(x) = |x| + 1, x \in R$$
 (3)

IMPROVEMENT 2012

21. i) If $\left(\frac{2x}{5} + 1, y - \frac{3}{4}\right) = \left(\frac{1}{5}, \frac{1}{4}\right)$ find x and y . (1)
ii) If $f = \{(2, 5), (3, 1), (5, 2), (8, 5), (10, 2), (11, 5)\}$ is a function, write its range. (1)

2012 MARCH

22. Let $A = \{1, 2, 3, 4, 5\}$ and R be relation on A defined by $R = \{(a, b) : b = a^2\}$
a) Write R in the roster form. (1)
b) Find the range of R . (1)
23. Consider the real function $f(x) = \frac{x+2}{x-2}$
a) Find the domain and range of the function. (1)
b) Prove that $f(x) \cdot f(-x) + f(0) = 0$ (2)

IMPROVEMENT 2011

24. Let $A = \{1, 2, 3\}$, $B = \{a, b\}$ be two sets.
a) Write the universal relation from A to B . (1)
b) What is the number of non-empty relations from A to B ? (1)
25. a) Find the range of the function
 $f(x) = [2x], -\frac{1}{3} \leq x \leq \frac{8}{3}$
b) Draw the graph of the function:
 $f(x) = \begin{cases} 1+x, & -1 \leq x \leq 0 \\ 1-x, & 0 < x \leq 1 \end{cases}$

MARCH 2011

26. Let $A = \{1, 2, 3, 4, 6\}$ and R be a relation on A defined by
 $R = \{(a, b) : a, b \in A; b \text{ is exactly divisible by } a\}$
a) Write R in the roster form
b) Find the domain and range of R
27. Consider the real function $f(x) = \frac{x^2 + 2x + 3}{x^2 - 8x + 12}$
a) Find the value of x if $f(x) = 1$
b) Find the domain of f .

IMPROVEMENT 2010

28. The Cartesian product $P \times P$ has 9 elements among which are found $(-a, 0)$ and $(0, a)$.
A relation from P to P is defined as
 $R = \{(x, y) : x + y = 0\}$
a) Find P .
b) Depict the relation using an arrow diagram.
c) Write down the domain and range of R .
d) How many relations are possible from P to P ?

MARCH 2010

29. Consider the functions

$$f(x) = \sqrt{x-2}, \quad g(x) = \frac{x+1}{x^2-2x+1}$$

- a) Domain of f (1)
- b) Domain of g (1)
- c) $(f+g)(x)$ (1)
- d) $(fg)(x)$ (1)

IMPROVEMENT 2009

30. Let $A = \{1, 2, 3, \dots, 14\}$ R is a relation on A defined

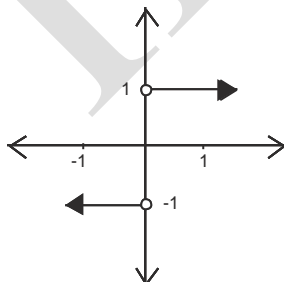
$$\text{by } R = \{(x, y) : 3x - y = 0, x, y \in A\}$$

[2015 Improvement]

- a) Write R in tabular form. (1)
 - b) Find the domain and range of R. (1)
31. Consider the function
- $$f(x) = 2 - 3x, \quad x \in R, \quad x \geq 0$$
- a) Find its range. (1)
 - b) Draw its graph in the given domain. (2)

MARCH 2009

32. a) Let $A = \{1, 2\}, B = \{3, 4\}$. Choose the number of relations from A to B from the bracket: (4, 16, 32, 64). (1)
- c) Determine the domain and range of the relation R, where $R = \{(x, x^3) : x \text{ is a prime number less than } 15\}$
- d) From the below graph, write the name and equation of the function.



(2)