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The Assessment Board selected this paper for the 2018 HKIE Geotechnical Paper Award, for its potential to advance local geotechnical practice and its quality of writing for the readership of practicing geotechnical engineers. It noted:

The paper Kwan et al (2015) documents development of a methodology for rational design of multiple barriers for intercepting mobile landslide debris. It started with Newtonian mechanics, took hints from physical model tests and case records, demonstrated by application to a real design case, and benchmarked against an advanced numerical model. This comprehensive and solid approach won confidence. The proposed methodology promises to fill another gap in Hong Kong's continual search for more reliable and effective design of debris flow barriers. The paper is clearly and logically written, with the support of two very helpful appendices on aspects demanding greater details to make sense of the subject matter. It should be accessible to most geotechnical practitioners with a good grasp of basic mechanics.

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2 **General information of the article**

3 **Type of paper:** Article

4 **Title:** Landslide Mobility Analysis for Design of Multiple Debris-resisting Barriers

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1 **Abstract:** Multiple debris-resisting barriers have been commonly used worldwide to mitigate  
2 debris flows in drainage lines. However, there lacks a well-developed methodology to assess  
3 the mobility of debris flows with consideration of the obstruction of the barriers. Free field  
4 debris flow condition which omits the presence of multiple debris-resisting barriers is  
5 commonly considered in design, although the effects of the barriers could be critical in  
6 determining the dynamics of landslide debris including debris velocity and debris thickness.  
7 This paper proposes a staged debris mobility analysis which accounts for the effects of  
8 multiple debris-resisting barriers. The staged analysis adopts solutions of depth-averaged  
9 debris mobility model. The input parameters of the analysis have been established from field  
10 data and laboratory test results. Rigorous numerical simulations of debris flows intercepted by  
11 multiple debris-resisting barriers have also been undertaken using three dimensional  
12 finite-element program LS-DYNA to provide results for benchmarking the output of the  
13 staged analysis.

14 **Keywords:** multiple debris-resisting barriers, landslide debris mobility analysis, debris  
15 flows, LS-DYNA.

## 1 **Introduction**

2 Multiple debris-resisting barriers (hereinafter referred to as multiple barriers) have been  
3 adopted in many countries to mitigate landslide hazards (WSL 2008; Shieh et al. 2006; Shum  
4 & Lam 2011). In general, multiple barriers comprise rows of single barrier installed at  
5 different strategic positions along the runout path of a given debris avalanche or debris flow.  
6 They are often built with a deposition area upstream to contain the debris. The barriers can  
7 be formed to different sizes and shapes to suit the topography, and a curved upstream surface  
8 may be provided to reduce the debris impact loading on the barrier (Shieh et al. 2006). Each  
9 row of single barrier is designed to retain a portion of landslide volume. Because of this, the  
10 scale of individual barriers, in terms of structural requirements and retaining height, could be  
11 optimized to cope with the site constraints and could also be more effective in minimizing  
12 entrainment (Wong 2009).

13 Experience suggested that multiple barriers can be a practicable means to mitigate  
14 reasonably large debris avalanches and debris flows. Various international publications give  
15 guidance and recommend good practice on certain design aspects of multiple barriers. For  
16 examples, CGS (2004) and NILIM (2007) provide guidelines for calculating retention volume  
17 of barriers, and SWCB (2005) recommends the minimum spacing between barriers. However,  
18 there are so far no well-established design guidelines for assessing the effect of the presence  
19 of multiple barriers on the landslide debris mobility.

20 Speerli et al. (2010) reported several debris flow flume tests to examine the dynamics of  
21 debris overflowing from small-scale ring-net barriers. A mixture of clayey gravelly sand and  
22 water was used in their tests. They observed that debris followed a ballistic projectile path  
23 after overtopping from the barrier and the debris was retarded upon impacting on the flume  
24 bed at the landing position. Debris would then accelerate when it propagated downstream  
25 along the inclined flume. Glassey (2013), who evaluated the effectiveness of the check dams

1 installed in the Illbach channel in Illgraben, Switzerland, mentioned that energy gain and  
2 energy dissipation are involved in the process of debris overflowing from filled-up barriers  
3 and debris landing. Glassey suggested that the height of check dams should be at least the  
4 height of debris flows.

5 Debris mobility assessment for design of multiple barriers calls for consideration of  
6 salient features involved in the debris runout process which include filling-up of barriers,  
7 overflowing from the barrier crest and energy dissipation at the debris landing position. This  
8 paper presents an analysis of debris mobility for the design of multiple barriers based on  
9 pertinent field and laboratory studies. To facilitate multiple barriers design, a staged mobility  
10 analysis is proposed to provide a means for assessing debris mobility dynamics taking into  
11 account the obstructions of multiple barriers. A debris mobility model developed using  
12 computer program LS-DYNA, calibrated against Yu Tung Road debris flow, has also been  
13 adopted to undertake debris flow simulations for benchmarking the results of the staged  
14 mobility analysis.

### 15 **Dynamic analysis of landslide debris**

16 In the design of multiple barriers, due to the lack of well-established methodology for  
17 assessing landslide debris dynamics, it has been assumed that the dynamics could be similar  
18 to that in the free-field conditions, i.e. presence of the multiple barriers is neglected.  
19 According to Wendeler et al. (2012), a series of 13 barriers was built along a drainage line to  
20 mitigate debris flow hazard in Switzerland, and the barrier design was established on the basis  
21 of the maximum debris velocity observed in the field. On the other hand, some researchers  
22 (e.g. Remaitre et al. 2008) have evaluated the influence of a series of filled-up barriers by  
23 considering variations in channel gradient. However, the analysis could not model reduction  
24 in debris volume and hence thickness due to debris retained by intermediate barriers.

25 In the prevailing geotechnical practice, dynamic mobility models have been used in the

1 design of debris-resisting barriers. With specific rheological parameters, numerical analyses  
2 can produce robust estimates of the dynamics of landslide debris for design purposes. Hungr  
3 et al. (2007) summarised details of various rheological and numerical models which were  
4 used in the debris mobility benchmarking exercise held in Hong Kong in 2007 and concluded  
5 that most of the common numerical models produced consistent results with the same specific  
6 rheological models.

7 Common numerical analyses for simulation of dynamics of landslide debris runout adopt  
8 continuum model developed based on depth-averaged shallow-flow equations. The  
9 formulations are made with reference to columns of debris mass above a sliding surface.  
10 DAN-W adopts this type of formulations to simulate the post-failure motion of rapid  
11 landslides. A pre-defined volume of soil or rock would change into a fluid and flows  
12 downslope, following a path of a defined direction and width. The model implements a one  
13 dimensional Lagrangian solution of the equations of motion and is capable of using several  
14 alternative rheological relationships (Hungr 1995). The model has been widely adopted in the  
15 engineering practice in Hong Kong for debris-resisting barrier design and landslide risk  
16 assessment purposes. Another numerical program DMM (stands for Debris Mobility Model),  
17 that allows input of channel section geometry in trapezoidal shape, was developed by Kwan &  
18 Sun (2006) based on modified formulations of Hungr (1995). This model has also been  
19 calibrated for used in Hong Kong. DAN-W is capable of simulating the ballistic flight of  
20 debris overshooting from vertical or sub-vertical runout paths, but DMM is not equipped with  
21 this function. Both DAN-W and DMM are Lagrangian models which discretise the landslide  
22 debris mass into inter-connected slices in their computations. The process of debris filling-up  
23 barriers and the subsequent overflow may not be realistically simulated due to the  
24 connectivity of the slices assumed in the formulations of the models.

25 Eulerian continuum models viz. FLO-2D (O'Brien et al. 1993; Bertolo & Wiczorek

1 2005) and Kanako-2D (Liu et al. 2012) have been used for assessing dynamics of debris flows.  
2 According to Liu et al. (2012), Kanako-2D is able to simulate changes in elevation of debris  
3 runout trail due to deposition or erosion. However, the simulation would not be applicable for  
4 situation when the flow velocity and flow depth change rapidly behind the barrier. In addition,  
5 simulation of ballistic flight of debris from the crest of the barrier is not included in the  
6 formulations of the model. Similar to Kanako-2D, the dynamics of debris ballistic flight is not  
7 explicitly simulated by FLO-2D. The discharge above barrier (or levee) is computed using  
8 weir flow equation.

9 The above commonly used computer programs adopt depth-averaged numerical scheme  
10 and the analyses are essentially two-dimensional. Three-dimensional continuum landslide  
11 mobility analyses have been undertaken by Crosta et al. (2007), who used an  
12 Eulerian-Lagrangian finite element code developed by Roddeman (2002). More recently, Yiu  
13 et al. (2012) reported the use of three-dimensional finite-element package LS-DYNA for  
14 landslide mobility assessment. LS-DYNA stands for Livermore Software – Dial-a-yield  
15 Nonlinear Analysis and it uses explicit time integration to study nonlinear dynamic problems.  
16 The package has been applied widely for stress and deformation analysis of structures subject  
17 to impacts. The program handles scalar advection in an Eulerian grid and solves equations of  
18 motion based on an Arbitrary Lagrangian-Eulerian (ALE) description of finite-element  
19 method. Landslide debris is assumed to be elasto-plastic which follows Drucker-Prager yield  
20 criteria. The computational domain was discretised into an array of hexahedral elements. The  
21 elements record the variables of acceleration, velocity, displacement, strain, stress and kinetic  
22 energy of landslide debris mass at various positions within the computational domain. Debris  
23 mass transport between elements follows the results of the ALE descriptions. The ground  
24 surface on which landslide debris travels on is modelled using rigid shell elements. Coulomb  
25 frictional rule was assumed at the interface between the landslide debris and the shell surface.

1 The LS-DYNA model was benchmarked against several well-documented laboratory and  
2 field studies, including the experiments of dry sand flows over irregular surfaces by Iverson et  
3 al. (2004) and the Yu Tung Road debris flow in Hong Kong (AECOM 2012). In the  
4 simulation of Yu Tung Road debris flow, an additional damping force proportional to the  
5 square of the debris velocity was applied in the LS-DYNA analysis to retard the debris motion.  
6 This damping force accounts for the energy loss due to the turbulence of debris flows. Its  
7 magnitude has been estimated with reference to the velocity-dependent resistance of the  
8 Voellmy rheology (ARUP 2013).

### 9 **A staged analysis for assessment of landslide mobility**

10 The commonly used computer programs which adopt depth-averaged scheme cannot  
11 simulate the entire process of debris filling up the retention zone of a barrier and subsequently  
12 overtopping the barrier. It is suggested that simulation of debris dynamics for the design of  
13 multiple barriers could be carried out based on a staged mobility analysis which adopts  
14 solutions of depth-averaged Lagrangian model. The stage analysis comprises the following  
15 key steps:

- 16 (i) carry out debris mobility analysis using a suitable program (e.g. DMM or DAN-W) to  
17 simulate the dynamics of landslide that travels from the source to the first barrier;
- 18 (ii) use the results of the mobility analysis to determine the velocity at which the debris will  
19 launch into a ballistic flight from the crest of the barrier;
- 20 (iii) calculate the geometry of the ballistic trajectory path and the debris velocity after  
21 landing;
- 22 (iv) carry out debris mobility analysis to model the landslide debris travelling from the  
23 landing position to the next barrier; and
- 24 (v) repeat Steps (ii) to (iv) until landslide debris reaches the terminal barrier.

25 When a landslide impacts on a barrier, a portion of the debris is trapped and retained

1 behind the barrier, which results in a kinetic energy loss of the debris flow. Once the barrier  
2 retention zone is fully filled, the remaining debris launches into a ballistic flight from the crest  
3 of the barrier, carrying the kinetic energy of the remaining landslide debris. For a robust  
4 estimate of the length of debris trajectory ( $x_i$ , see Fig. 1), the velocity at which the debris  
5 launches into a ballistic flight (see also Step (ii) above) may be taken as the maximum  
6 velocity of the remaining debris ( $v_m$ ), assumed to be in horizontal direction. The  $v_m$  is taken as  
7 maximum velocity parallel to channel slope at location ( $x = 0, y = 0$  in Figure B1) and  
8 assumed to act in horizontal direction.

9 In the most common situations, the above assumption would be conservative and  
10 produce a more critical  $x_i$ , since the surface of the debris deposit behind an intermediate  
11 barrier is likely to be sloping at a lower angle than the natural channel. Kwan (2012) had  
12 conducted a review of debris deposition angles behind barriers for the design of retention  
13 capacity from the field observations of many countries. The review showed that the range of  
14 deposition angles behind barriers is between 1/2 and 3/4 of natural channel bed. However,  
15 there may be rare cases where the angle of debris deposition behind a barrier would exceed  
16 the inclination of the natural channel due to reasons such as excavation into the channel to  
17 form a steeper profile for the purposes of increasing the retention volume (Kwan 2012).

18 The  $v_m$  value can be obtained from the velocity output of the debris mobility analysis.  
19 For example, if the Lagrangian type mobility model (e.g. DMM) is used, the mass blocks that  
20 would be trapped by the barrier would be those at the front of the debris chain with a volume  
21 equal to the retention capacity of the barrier, and the maximum velocity of the remaining mass  
22 blocks would be used for trajectory length calculation.

23 With debris launching velocity,  $v_m$  (in m/s) in horizontal direction, height of barrier,  $h$  (in  
24 m), and inclination of the ground profile,  $\theta$  (in degree), the length of debris trajectory,  $x_i$  (in m)  
25 can be calculated using Eq. (1) below, which is derived from energy conservation principle

1 (see Appendix B):

$$2 \quad (1) \quad x_i = \frac{v_m^2}{g} \left[ \tan \theta + \sqrt{\tan^2 \theta + \frac{2gh}{v_m^2}} \right]$$

3 The equation above provides a reasonable estimate as compared with the results of flume tests  
 4 (see Appendix A). If  $v_m$  is acting at an angle rather than horizontal, the horizontal  
 5 component of  $v_m$  can be input to Eq. (1) for calculation.

6 The debris velocity just before landing,  $v_r$  (in m/s), is calculated based on the kinetic  
 7 energy of the remaining debris and the kinetic energy gained in the drop from height as  
 8 follows (see Appendix B):

$$9 \quad (2) \quad v_r = \sqrt{\frac{2[KE_r + m_r g(h + C_x x_i \tan \theta)]}{m_r}}$$

10 where  $m_r$  = mass of remaining debris (in kg),  $KE_r$  = kinetic energy of remaining debris (in J),  
 11 and  $C_x$  = correction factor on  $x_i$ .

12 Under common circumstances, each of the intermediate barriers would be designed to  
 13 retain a certain portion of the debris flow. The remaining debris mass ( $m_r$ ) relates to the  
 14 amount of debris that cannot be trapped by the barrier, i.e. the total volume of debris before  
 15 hitting the barrier less the barrier retention capacity that can be taking into account the  
 16 remaining debris from upstream slope that will overflow the barriers.  $m_r$  and kinetic energy of  
 17 the remaining debris ( $KE_r$ ) can be obtained based on the mass and velocity of the remaining  
 18 mass blocks calculated from Lagrangian debris mobility analysis. If the barrier has been  
 19 filled up completely by the debris materials previously, the retention capacity of the barrier  
 20 should be ignored, and  $m_r$  and  $KE_r$  can be taken as the mass and the kinetic energy of the  
 21 entire landslide debris. The dynamics of subsequent overflow can still be analysed using the  
 22 proposed staged analysis, e.g. for calculations of the overflow trajectory and debris mobility

1 analysis between the debris landing location and the next barrier.

2 Essentially, the frontal portion of the debris flow travels at the highest velocity  
 3 comparing with the portion behind. Experience shows that debris flow velocity attenuates  
 4 from the frontal portion, and the rate of attenuation becomes smaller towards the rear end of  
 5 the debris flow mass. It is therefore expected that the velocity within the remaining debris  
 6 (i.e. within the  $m_r$ ) would not varies significantly, and the use of  $m_r$  in establishing  $v_r$  can be  
 7 considered reasonable. However, if short barrier height is used and the portion of debris  
 8 retained is small, the use of frontal velocity of the remaining mass for establishing  $v_r$  would be  
 9 more appropriate.

10  $x_i$  is the maximum projectile distance which defines the landing position of the frontal  
 11 portion of the remaining debris as it is calculated based on the maximum velocity of the  
 12 remaining debris. Since the velocity of debris varies, a correction factor  $C_x$  is applied to  $x_i$  in  
 13 the equation for the sake of calculating the average projectile length of the overflow. .  
 14 Suggested values of  $C_x$ , correspond to the ratio of the rear velocity to frontal velocity of the  
 15 remaining debris, are listed in Table 1. As field data for establishing  $C_x$  values are limited, the  
 16 values presented in Table 1 are established based on a parametric numerical study of projectile  
 17 lengths over different combinations of barrier height, debris velocity and inclination of  
 18 run-out path (see Appendix B). The program 2d-DMM has been calibrated in a number of  
 19 landslide debris flow cases in Hong Kong and overseas including the 2008 Yu Tung Road  
 20 debris flow considered in the illustrative example presented in this paper (Kwan et al. 2013;  
 21 Chan & Kwan 2012; Kwan et al. 2006). It is considered reasonable to use the well  
 22 calibrated program 2d-DMM for parametric studies to derive  $C_x$ .

23 For carrying out the mobility analysis of landslide debris downstream as stated in  
 24 Step (iv) above, an initial debris velocity is required. This velocity,  $v_i$  (m/s), can be obtained  
 25 by resolving  $v_r$  as shown below (derivations of the equation refer to Appendix B):

$$(3) \quad v_i = Rv_r \cos \left[ \left[ \tan^{-1} \sqrt{\frac{m_r g (h + C_x x_i \tan \theta)}{KE_r}} \right] - \theta \right]$$

where  $R$  = velocity correction factor.

In order to consider the velocity reduction due to the debris impacting on the trail at the landing position, a correction factor of  $R$  should be applied to the above equation. The present study has analysed the results of the flume test by Choi & Ng (2013) with a view to determining a suitable value of  $R$  for design purposes.

The flume test was carried out using dry sand. Appendix A presents details of the test set-up. Instrumentation of the test included high speed cameras, laser sensors and photo sensors. High resolution images were captured during the test to investigate the dynamics of debris impacting and filling up the rigid barrier, then launching into a ballistic flight from the crest of the barrier and resuming its travel on the flume bed upon landing (see figures presented in Appendix A). The image data have been interpreted by the present study using the Particle Image Velocimetry (PIV) technique developed by White et al. (2003) for estimating the velocity reduction at landing.

Typical PIV results are presented in Fig. 2. It shows the velocity at the instant of about 0.5 second after the sand had impacted on the barrier. The sand overflowed from the crest of the barrier at a velocity of about 1 m/s and then launched into a ballistic flight. It followed a projectile trajectory and finally landed on the flume bed at a maximum distance of 0.21 m downstream of the barrier. Due to the release of the potential energy, the sand flow accelerated along the trajectory path. The maximum velocity was up to about 1.8 m/s immediately before landing. Upon landing, the sand flow travelled along the flume bed. The sand flow velocity was reduced after landing. The ratio of the velocity parallel to the flume bed after and before impact has been determined at various times during the test. This velocity ratio ranged from about 0.3 to 0.5. Appendix A presents detailed interpretation of the test

1 results.

2 It should be noted that dry sand is frictional and develops high flow resistance at the  
3 impact point, where the normal momentum of the falling mass creates a large normal force. In  
4 case of saturated materials in the field, however, such an impact may create high pore-water  
5 pressure in the debris, resulting in low effective normal stress and hence small flow  
6 resistance.

7 Flume tests involving ballistic trajectory of dry granular flow comprising rock blocks  
8 had been conducted by Yang et al. (2011). The rock blocks used in their experiments were of  
9 dimension of up to 0.1 m. According to Yang et al. (2012), the granular flows in their tests  
10 involved rolling and bouncing of large granular particles. These flume tests may replicate the  
11 dynamics of debris avalanche. They observed that the granular flow was subjected to velocity  
12 reduction upon landing on the flume bed. Yang et al. (2012) reported that the velocity  
13 immediately after and before landing ranged from 0.41 to 0.75 with an average of 0.65.

14 Head loss of wet debris flows dropping from height has been studied by Chen et al.  
15 (2009). They carried out measurements along debris transport channels equipped with drop  
16 structures, and suggested a formula for estimation of head loss of debris flow dropping from  
17 height. The velocity of the debris flows reported by Chen et al. (2012) ranged from 3 m/s to 6  
18 m/s and the debris transport channels under their study were gently inclined (about 10°).  
19 Based on the suggested formula, it can be estimated that the ratio of velocity in the direction  
20 of the downstream channel after and before landing is in the order of 0.3 for debris flow of  
21 thickness ranging from 0.5 m to 1.5 m with a drop height of 2 m to 4 m.

22 In addition to the above, data reported by Glassey (2013) and videos of Illgarben debris  
23 flows available on internet at [http://www.wsl.ch/fe/gebirgshydrologie/massenbewegungen/  
24 prozesse/murgang/videos/index\\_EN](http://www.wsl.ch/fe/gebirgshydrologie/massenbewegungen/prozesse/murgang/videos/index_EN), <http://www.youtube.com/watch?v=tjWZTP3u9d4>,  
25 <http://www.youtube.com/watch?v=OUtZVn2NwrY>, and <http://www.youtube.com/watch?v>

1 [=tjWZTP3u9d4](#) have been reviewed. Quantitative data has been determined for  
2 investigation on  $R$  factor. Overall, a range of  $R$  factor is between 0.3 and 0.75. The results  
3 are systematically presented in Table 2. The value of  $R$  correlates with channel base materials.  
4 It is noted that  $R$  factor for debris impacting on hard flume channel base varied between 0.5  
5 and 0.7. However, when the flume channel filled up with the debris, the  $R$  factor could  
6 reduce to a range of 0.3 to 0.5. This phenomenon of  $R$  factor reduction is also observed in  
7 the field studies in China and Illgraben when the channel base is filled up with loose materials  
8 or debris. Comparisons between dry sand flows and wet debris flows show that the ranges of  
9  $R$  factor are similar. It is expected that high water content would give a higher value of  $R$   
10 factor because water would act as lubricant. However, the turbulence effects brought about  
11 by the water may contribute energy loss. The field cases in Illgraben with high water content  
12 of debris flows also give similar range of  $R$  factor between 0.4 and 0.7, except after the  
13 channel base is filled up with debris. All in all, the ratio of velocity parallel to debris trail after  
14 and before landing could range from 0.3 to 0.75. The flow dynamics of debris impacting on  
15 the ground is complex. More importantly, the actual water content, particle size distribution  
16 and characteristics of channel bed at landing location which affect the velocity reduction  
17 could vary significantly. It is not easy to define precisely a value of  $R$ . In view of the large  
18 uncertainties involved, a value of  $R$  on the high side, 0.7, is recommended.

19 Debris mobility analysis to model the dynamics of landslide debris travelling from the  
20 landing position to the next barrier would be carried out as per Step (iv) above.  $x_i$ , as  
21 mentioned above, gives the initial position at which the debris mobility analysis would  
22 commence, and  $v_i$  gives the initial velocity of debris for the subsequent analysis. Another two  
23 parameters, i.e. debris length ( $x_d$ ) and debris thickness ( $h_m$ ), are required for carrying out the  
24 analysis. The length of debris,  $x_d$ , is assumed to be the same as that of the remaining debris  
25 before the overflow (i.e. the length of mass blocks that would not be trapped by the barrier). If

1 the length of debris is greater than the length of debris trajectory (i.e.  $x_d > x_i$ ), the debris is taken  
 2 to extend backward from the point of landing to beyond the barrier for calculation purposes.  
 3 Though this is an idealization, it is more robust for design as the debris would start motion again  
 4 with a higher potential energy. An additional reason for adopting  $x_d$  as opposed to  $x_i$  is that the  
 5 latter would have led to greater initial debris thickness for the subsequent mobility analysis  
 6 which could result in unrealistic basal resistance particularly for a Voellmy rheological model  
 7 (Hungr 1995).

8 Debris thickness,  $h_m$ , upon landing can then be determined based on the volume of the  
 9 remaining debris and width of the runout trail. In order to simulate a greater debris frontal  
 10 thickness as normally observed, it is suggested that the maximum thickness of the remaining  
 11 debris at the debris front should be adopted. The thickness of the frontal one-fifth of the mass  
 12 blocks is taken to be the maximum thickness of the remaining debris (i.e. if 50 mass blocks are  
 13 used to model the whole landslide debris, 10 mass blocks at the frontal position is assigned to  
 14 have the maximum thickness of the remaining debris). The debris thickness is then assumed  
 15 tailing off at a profile which corresponds to a volume of the remaining debris.

16 With the four initial conditions viz.  $v_i$ ,  $x_i$ ,  $h_m$  and  $x_d$  as established above, separate  
 17 landslide debris mobility analysis can start off from the landing position to the barrier  
 18 downhill. The impact velocity of landslide debris at the downhill barrier can be then  
 19 calculated.

## 20 **Sensitivity analyses of barrier height and other parameters**

21 Sensitivity analyses have been carried out for different combinations of barrier height  
 22 from 1 m to 5 m and a range of launching flow velocities ( $v_m$ ) from 4 to 10 m/s using the  
 23 proposed staged analysis (see Equations 1 to 3) to investigate the effect to the debris velocity  
 24 after landing ( $v_i$ ). The slope inclination between  $5^\circ$  and  $30^\circ$  has been assumed. It is  
 25 observed that multiple barrier system could be more effective in dissipating energy if short

1 barriers are used, as short barriers limit the energy gain of landslide debris during overflows.  
2 Another observation is that the ratio of  $v_i/v_m$  is not sensitivity in the ranges of parameters  
3 considered. Only 15% variation in  $v_i/v_m$  is observed.

#### 4 **Application of the staged mobility analysis**

5 The application of the staged mobility analysis is demonstrated through an illustrative  
6 example pertaining to the design of debris-resisting barriers for protection of Yu Tung Road,  
7 Hong Kong from debris flow hazards. On 7 June 2008, a sizable channelised debris flow  
8 involving an active volume of about 3,400 m<sup>3</sup> occurred in a natural hillside catchment above  
9 Yu Tung Road. A video showing the debris flow event is available online at  
10 <http://youtu.be/R2uTKyK1c9k>. Different pulses are observed in the video that characterize  
11 the mobility of the debris flow. The proposed staged analysis can be applied to analyse the  
12 dynamics of the overflow and debris dynamics between the landing location and the next  
13 barrier. A detailed geotechnical investigation of the event is reported by AECOM (2012).  
14 The debris flow is referred to as Landslide No. 25 (LS08-241), Catchment No. 30 in  
15 AECOM's report.

16 Fig. 3 shows the catchment and the section of natural drainage line, taken after the debris  
17 flow event. The debris flow was a result of a massive landslide with a 2,350 m<sup>3</sup> failure  
18 volume at the head of the drainage line. Severe rainfall was one of the contributing factors of  
19 the landslide. The landslide materials entered into the incised drainage line (see also Fig. 3  
20 and Fig. 4), mixed with surface runoff and developed into a debris flow with an additional  
21 volume of 1,000 m<sup>3</sup>. The debris flow travelled about 600 m and disrupted the traffic of Yu  
22 Tung Road immediately downstream of the drainage line outlet.

23 Before the debris flow, landslide risk of the catchment had been identified and design of  
24 a rigid debris-resisting barrier was underway. Up-to-date, construction of the rigid barrier has  
25 completed. The barrier is located at the outlet of the drainage line (Chainage Ch 525 m; the

1 Chainage starts at the crown of the landslide scar). The design debris retention volume is  
2 taken as 3,500 m<sup>3</sup>. In order to achieve this retention volume, a 7 m high barrier wall was built.  
3 Debris mobility analysis was carried out with an assumption that a volume of 3,500 m<sup>3</sup>  
4 ground mass would detach at the head of the drainage line to establish the debris impact  
5 velocity and debris thickness for design of the rigid barrier. A detailed back-analysis of the  
6 presented Voellmy parameters has been carried out by Kwan et al (2012) to best fit the  
7 observation of the Yu Tung Road case. Voellmy rheological parameters comprising basal  
8 friction coefficient of 0.14 ( $\tan \phi_b$ , where  $\phi_b$  is 8°) and turbulence coefficient of 500 m/s<sup>2</sup> (Kwan  
9 et al. 2012) were adopted in the debris mobility analysis. The design debris impact velocity and  
10 debris impact thickness for the barrier at Ch 525 m are 8 m/s and 2.1 m respectively.

11 To demonstrate the applicability of the staged debris mobility analysis, it is assumed that  
12 two intermediate barriers at Ch 360 m and Ch 480 m were proposed and stage approach is  
13 used for calculation of the impact debris velocity and impact debris thickness of the two  
14 intermediate barriers. This serves as an example to illustrate how the proposed stages  
15 approach is used. The height of the intermediate barriers is 3 m. The corresponding retention  
16 volumes calculated following the guidelines stated in CGS (2004) are 780 m<sup>3</sup> and 700 m<sup>3</sup>.  
17 With the two intermediate barriers, a smaller design debris retention capacity of the terminal  
18 barrier at Ch 525 m would be required, and the barrier wall height is estimated to be 4 m. The  
19 number of intermediate barriers and the barrier height adopted in this illustrative example  
20 have not been optimised. In real design exercise, the number and the height of barriers should  
21 be determined with consideration of the design retention volume, potential visual impact, cost  
22 effectiveness, site accessibility and the actual topography.

23 The staged mobility analysis was carried out using debris mobility program 2d-DMM  
24 (the latest version of 2d-DMM allows for debris mobility analysis with an initial debris  
25 velocity specified as required in the proposed staged analysis). The analysis started off with a

1 debris volume of  $3,500 \text{ m}^3$  at the landslide source area (i.e. the head of drainage line) with a  
2 maximum thickness of about 3 m. Fig. 4 shows the runout profile adopted in the mobility  
3 analysis. The vertical scale of the landslide source thickness and barrier height has been  
4 exaggerated by 50 times for clarity. The same rheological parameters as those of the  
5 conforming design were used. The analysis ran until the debris reaches the first intermediate  
6 barrier at Ch 360 m. Using eqs. (1) to (3), the initial conditions for the next stage of landslide  
7 mobility analysis were established. The next stage analysis was then carried out commencing  
8 at the downstream of the barriers. The procedure repeated until landslide debris reaches the  
9 terminal barrier at Ch 525 m. With the stage analysis, the velocity and thickness of debris  
10 approaching each of the barriers were calculated. Key results and the initial conditions  
11 involved are summarised in Table 3.

12 The stage analysis aims to assess the dynamics of the landslide debris with consideration  
13 of the obstruction of multiple barriers. According to the results of the analysis, the design  
14 debris impact velocity and thickness for the terminal barrier are 7.3 m/s and 1.1 m  
15 respectively. Comparing with the design values established for no intermediate barriers, i.e.  
16 8 m/s and 2.1 m, the analysis shows that the intermediate barriers could lead to a reduction of  
17 9% in debris velocity and 52% in debris thickness.

18 However, construction of the first intermediate barrier could be a technical challenge  
19 because the barrier is required to resist relatively high impact velocity (12.0 m/s) and great  
20 impact thickness (2.8 m). This highlights the importance of location selection for building  
21 intermediate barriers. Ideally, intermediate barriers should be positioned at broad and flat  
22 portions of the drainage line, which provide favourable conditions for slowing down landslide  
23 debris.

24 In order to ensure the function of debris retention, routine maintenance e.g. regular  
25 debris clearance would be needed. If it is assessed to be appropriate, the multiple barriers

1 function as a series of check dams, clearance of landslide debris would not be required. The  
2 filled barriers would contribute to a less steep runout profile that helps to reduce mobility and  
3 runout distance of any subsequent landslide events.

#### 4 **Benchmarking with LS-DYNA analysis**

5 A three dimensional debris mobility analysis using computer program LS-DYNA has  
6 been carried out. The analysis produces data for benchmarking the results of the staged  
7 mobility analysis. LS-DYNA model developed by Yiu et al. (2012) is adopted. The program  
8 handles scalar advection and solves equations of motion based on an Arbitrary  
9 Lagrangian-Eulerian (ALE) description of finite-element method. The runout distance of Yu  
10 Tung Road debris flow exceeds 600 m and the width of some sections of corresponding  
11 runout trail is over 30 m. The computational domain is discretised into an array of uniform  
12 hexahedral elements of dimensions 2 m (wide), 2 m (long) and 0.5 m (deep). Over 930,000  
13 elements are used in the model.

14 Drucker-Prager yield criteria are assumed to describe the internal rheology of the debris  
15 flow. Key parameters which define the properties of the debris flow materials are listed in  
16 Table 4. ARUP (2013) reported that the analysis result is not sensitive to Poisson's ratio ( $\nu$ ).  
17 A typical value of  $\nu$  of 0.3 is adopted.

18 The bulk density ( $\rho$ ) and stiffness parameters, including  $E$  and  $\nu$ , are found not sensitive  
19 to the results of the analysis (ARUP 2013). Typical values commonly adopted in geotechnical  
20 analysis for design purposes are therefore assumed (Kwan et al 2012). The Yu Tung Road  
21 debris flow was watery as shown in the video record and the sedimentology of the event could  
22 mainly comprise sandy and coarse materials (AECOM 2012). In theory, it is a cohesionless  
23 material. However, specification of a non-zero value of cohesion is required for LS-DYNA  
24 analysis. Therefore, a nominal value, or a very low value of cohesion, 0.1 kPa, is assumed.  
25 The internal friction angle ( $\phi_{int}$ ) affects the mobility of landslide debris in the LS-DYNA

1 analysis, and has been back-calculated based on the velocity determined from the video  
 2 record and the super-elevation data mapped on site (see Fig. 5) based on the best-fit model  
 3 parameters.

4 In addition to  $\varphi_{int}$ , resistance to landslide debris motions modeled in the analysis affects  
 5 the simulated debris mobility. The resistance applied in the model comprises (i) basal friction  
 6 at the interface of the landslide debris and the surface of the runout trail, and (ii) damping  
 7 force proportional to the debris velocity. The basal friction is assumed to be of Coulomb type  
 8 and is proportional to the normal stress acting at the debris/ground interface. Basal friction  
 9 coefficient ( $\tan \varphi_b$ , where  $\varphi_b$  is  $8^\circ$ ) of 0.14 same as the 2d-DMM analysis is adopted. The  
 10 damping force ( $F_d$ ) is calculated as per eq. (4):

$$11 \quad (4) \quad F_d = \xi_d m v^2$$

12 where  $F_d$  is damping force,  $m$  is mass of debris,  $v$  is debris velocity, and  $\xi_d$  is proportional  
 13 constant.

14 This damping force is applied to simulate the energy dissipation due to turbulence. In  
 15 depth-averaged calculations, similar resistance, proportional to  $v^2$ , is considered in the  
 16 Voellmy rheology (Hungri 1995). The turbulence resistance ( $F_{turb}$ ) in the Voellmy rheology is  
 17 defined as:

$$18 \quad (5) \quad F_{turb} = m g v^2 / \zeta h$$

19 where  $F_{turb}$  is turbulence resistance,  $g$  is gravitational acceleration,  $h$  is debris thickness, and  $\zeta$   
 20 is turbulence coefficient.

21 Voellmy rheology has proven to produce reasonable simulations of channelised debris  
 22 flows (GEO 2011). The damping force applied in LS-DYNA analysis is therefore established  
 23 with reference to the Voellmy rheology. The accelerations (or decelerations) resulted from  $F_d$   
 24 is pegged to that of  $F_{turb}$  (i.e.  $F_d / m = F_{turb} / m$ ). It follows that

1 (6)  $\xi_d = g / \xi h.$

2 According to GEO (2011),  $\xi$  should be taken as  $500 \text{ m/s}^2$  for modeling channelised  
 3 debris flows for design purposes. Using eq. (6) and on the basis of the field mapping results  
 4 that the average debris thickness of the debris flow event is in the order of magnitude of 2 m,  
 5  $\xi_d$  for the LS-DYNA analysis is taken as  $0.01 \text{ m}^{-1}$ .

6 Fig. 5 shows the frontal debris flow velocity of Yu Tung Road debris flow calculated by  
 7 2d-DMM and LS-DYNA. Both numerical models produced comparable results which  
 8 generally matched the debris velocity determined based on the video record and  
 9 super-elevation data mapped in the field. The differences would be caused by the localised  
 10 channel surface conditions which have not been modelled explicitly. Also, the water content  
 11 of debris flow may also affect the turbulence effect on the velocity at certain locations with  
 12 various topography conditions. It is difficult to obtain sufficient original specific  
 13 information throughout debris flow path after the event had been occurred. In the light of  
 14 information, a constant best-fit set of rheological parameters has been applied throughout the  
 15 debris flow profile. Also, the field observations were estimated from the super-elevations  
 16 instead of instrumental measurements which could be associated with some degrees of  
 17 uncertainties. 2d-DMM and LS-DYNA adopt different numerical strategies. 2d-DMM is  
 18 developed based on depth average approach, whereas LS-DYNA is a full 3-dimensional  
 19 analysis with consideration of the yield criteria of the materials being modelled. The  
 20 2d-DMM analysis requires a pre-defined debris trail width whereas LS-DYNA does not.  
 21 These factors may also contribute to the difference between the two simulation results. The  
 22 internal friction angle ( $\phi_{int}$ ) used in the LS-DYNA analysis is  $15^\circ$ . The LS-DYNA analysis is  
 23 undrained in nature,  $\phi_{int}$  should be regarded as an apparent friction angle which incorporates  
 24 the effects of pore water pressure. In view that the debris flow is watery, this back-calculated  
 25 internal friction angle (i.e.  $15^\circ$ ) is of a reasonable order of magnitude. In addition to debris

1 velocity, the LS-DYNA analysis reproduced debris flow length (~200 m) similar to that  
2 observed in the video and is consistent with the debris length ( $x_d$ ) of the staged analysis (see  
3 Table 2 and Fig. 6). The maximum thickness of debris at Ch 360 m and Ch 480 m calculated  
4 by LS-DYNA analysis are 3.5 m and 2.5 m respectively. The calculated values are similar to  
5 the maximum debris thickness estimated in the field, which is between 2 m and 3m (AECOM  
6 2012).

7 The calibrated LS-DYNA model has been modified to include two intermediate barriers  
8 at Ch 360 m and Ch 480 m. The barriers are modelled using rigid plate element, firmly  
9 attached to the topography. The barriers are 3 m high and assumed to be 2 m thick. Material  
10 properties and resistance parameters same as those adopted in the above calibration run are  
11 used. In contrast to staged analysis, LS-DYNA analysis simulates explicitly the dynamics of  
12 debris flows and debris retention behind intermediate barriers (see Fig. 7).

13 Fig. 8 shows the velocity vector plots of the flow field in the proximity of the first  
14 intermediate barrier at Ch 360 m. The figure reveals the debris flow dynamics involved and  
15 the debris-barrier interaction. When debris flow reaches the barrier, it is impeded by the  
16 obstruction of the barrier. Debris at the frontal portion runs up against the barrier. A plug is  
17 formed by the debris stopped and trapped behind the barrier. The extent of the plug develops  
18 when further debris is stopped behind the barrier. Debris flow subsequently rides on the plug  
19 and overtops the barrier. Debris overflowing from the barrier launches into a ballistic flight,  
20 and resumes its travel on the runout trail after landing.

21 Key results produced by the staged analysis and the LS-DYNA simulation are compared  
22 in Table 5. The adopted  $C_x$  value of the staged analysis is 0.8. The staged analysis generally  
23 gives results comparable with the LS-DYNA simulation, albeit on a relatively high side. The  
24 debris approaching velocity calculated by the staged analysis is 5% to 11% higher. Similarly,  
25 the thickness of debris approaching barriers calculated by the staged analysis is greater

1 compared with the LS-DYNA analysis. In addition, both LS-DYNA simulation and staged  
2 analysis give similar remaining kinetic energy of about 40% comparing to the free-field  
3 condition at the location of Ch 525 m, i.e. about 60% of kinetic energy is dissipated by the  
4 two multiple barriers. Usually, hydrodynamic equation would be used to calculate the  
5 dynamic impact pressure in sizing rigid barriers, of which the pressure is proportional to the  
6 velocity square. For this illustrative example, the difference in dynamic impact pressure  
7 obtained from the velocities of 2d-DMM and LS-DYNA is 20% maximum, which is  
8 considered acceptable in engineering design purpose.

9 Two sets of additional analyses assuming that intermediate barriers are 2 m and 4 m high  
10 respectively were carried out as a sensitivity study. It is observed that when smaller barriers  
11 of 2 m high are used, the debris impact thickness of the second and the terminal barrier is  
12 greater comparing with the 3 m high barriers, as the retention volume of the intermediate  
13 barrier is lesser. If higher intermediate barriers of 4 m high are used, the impact debris  
14 velocity and impact debris thickness of the second and the terminal barriers reduce by 15%  
15 and 10% respectively because of the reduction in the mass of overflow debris from  
16 intermediate barriers.

17 A sensitivity analysis has also been carried out using different combinations of internal  
18 friction angles of  $5^{\circ}$  to  $30^{\circ}$ . It is noted that when internal friction angle does not exceed  $20^{\circ}$ ,  
19 the effect of the internal friction angle on the calculated debris thickness is limited. However,  
20 when the internal friction angle is higher than  $20^{\circ}$ , the calculated debris thickness increases  
21 with the internal friction angle. The reason may relate to the internal pressure of the debris  
22 mass. The internal pressure reduces with the internal friction angle, and the reduced internal  
23 pressure tends to result in a more intact debris mass i.e. less elongation and thicker debris  
24 mass.

25

## 1 Discussion

2 For the Yu Tung Road site, the staged analysis and LS-DYNA simulation produce  
3 comparable results for design of multiple barriers, although the results of the stage analysis is  
4 relatively higher on the debris impact velocity and thickness. The results of the staged  
5 analysis can be adjusted to match LS-DYNA's output by lowering the value of velocity  
6 correction factor  $R$  (see eq. (3)), as this will lead to a greater velocity reduction after landing.  
7 Nevertheless, calibration of the  $R$  value against LS-DYNA analysis for general use may not be  
8 appropriate because the  $R$  value would be dependent on the actual composition of the debris  
9 flow, and roughness and materials of the landslide trail at the debris landing location. The use  
10 of the recommended value of  $R$  (i.e. 0.7), which is on the high side of available data reported  
11 in literature, is selected with a view to achieving a suitably robust design of debris-resisting  
12 barriers.

13 The staged analysis has been undertaken using depth-averaged computer program. It is a  
14 simplified methodology for assessing dynamics of landslide debris that accounts for the  
15 obstruction of multiple barriers. Dynamic landslide simulations by advanced numerical  
16 package LS-DYNA provide a more complete picture of debris mobility against the barriers. It  
17 could provide insights pertinent to the understanding of landslide debris-barrier interaction  
18 and could stimulate advancement in engineering design of mitigation measures against debris  
19 flows. Continuous research and development work including validation and calibration of  
20 three-dimensional numerical models for assessing landslide debris dynamics could bring  
21 positive impacts to engineering practice.

22 Another two observations can be made based on the present study:

23 (a) Height of intermediate barriers should not be excessive - debris overflowing from a  
24 barrier launches into a ballistic flight. The overflowing debris gains potential energy and is  
25 not subject to any basal resistance during the flight at the same time. The gain would increase

1 when the debris runout path is steep, since a steeper runout profile would result in a larger  
2 drop height. In order to minimise the gain in potential energy, barrier height should not be too  
3 large. Otherwise, the impedance to debris flow brought about by the intermediate barriers may  
4 be off-set and a net increase in the kinetic energy of landslide debris may be resulted in.  
5 Glassey (2013) also mentioned that the distance of debris overflow should be limited because  
6 it would induce an increase in velocity. The present study is useful for practitioners to  
7 consider the flow dynamics and overflow mechanism for an effective barrier height design.

8 (b) Time delay in debris flow reaching outlet of drainage line - with presence of multiple  
9 barriers, landslide debris may take a longer time for travelling from the landslide source to the  
10 drainage outlet. The LS-DYNA simulation unveiled that Yu Tung Road debris flow might  
11 have reached the drainage outlet at 50 s after the onset of the landslide (see Fig. 6(f)). With  
12 the presence of intermediate barriers, 10 more seconds would be required for the landslide  
13 debris to travel from the landslide source to the drainage outlet (see Fig. 8(d); debris arrives at  
14 Ch 525 m at 60 s after landslide onsets). The additional time could be crucial in emergency  
15 situations because it could provide more lead time for the people/traffic affected to take  
16 emergency actions (e.g. road closure using automatic gate, etc.), albeit it appears to be limited.  
17 The time delay could be lengthened by placing additional intermediate barriers at suitable  
18 locations. With installation of a system of sensors to detect impacts of landslide debris on  
19 intermediate barriers for provision of early warning, the multiple barrier scheme could be a  
20 robust mitigation measure for managing landslide risk.

## 21 **Conclusions**

22 A staged debris mobility analysis which considers the obstruction of multiple  
23 debris-resisting barriers has been proposed. The staged analysis makes use of Lagrangian  
24 depth-averaged solutions computed by computer programs viz. DAN-W and 2d-DMM. The  
25 input parameters required for the staged analysis, e.g. correction factor to account for the

1 velocity reduction at landing, have been established on the basis of available experimental  
2 data reported in literature and results of flume test of dry sand flows.

3 In order to illustrate the applicability of the stage analysis, the design debris impact  
4 thickness and velocity of a multiple barrier scheme to mitigate debris flow site are calculated  
5 using the staged analysis. The results have been benchmarked with a three-dimensional  
6 dynamic landslide mobility assessment undertaken using LS-DYNA. The debris mobility  
7 model of LS-DYNA has been developed to consider turbulence resistance. Calibration of the  
8 LS-DYNA model is carried out using the debris velocity data corroborated by a video record  
9 and field mapping results. The results of the stage analysis and the LS-DYNA assessment are  
10 comparable, although the stage analysis produces higher design parameters in general.

11 The dynamics of debris flows obstructed by barriers are complicated, involving filling up  
12 and overflowing of barriers. The suggested staged mobility analysis is a simplified procedure  
13 which does not explicitly simulate these dynamics. The results generated are benchmarked  
14 with LS-DYNA analysis in one test site. Further review of the suitability of the staged  
15 analysis by means of field and laboratory experiments is worthwhile.

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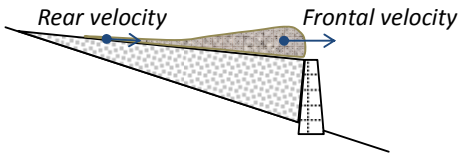
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Tables

Table 1. Suggested Values of  $C_x$

Ratio of rear velocity to frontal velocity of the remaining debris	$C_x$
< 0.2	0.6
0.2 to 0.66	0.8
$\geq 0.67$	1.0



**Table 2.** R factor determined from the field and laboratory tests

Cases	Water content	Bedding	Water in channel at impact	Channel gradient	R factor
1. Bouldery granular flow* (Yang et al, 2011)	Dry	Hard flume base	No	10°	0.4-0.7
2. Debris flow mixture from clay to gravel* (Speerli et al, 2010)	25-30% by mass	Hard flume base	No	9° - 14°	0.5-0.7
3. Sand flow* (Choi & Ng, 2013)	Dry	Hard flume base (1 <sup>st</sup> surge)	No	26°	0.5
		Sand base			0.3-0.4
4. Watery debris flow# (Chen et al, 2009)	High	Soft channel base	Yes	10°	0.3
5. Bouldery granular flow# (Information from the Illgraben debris flows observations in Switzerland on 3 June 2000, 28 June 2000, 22 July 2013 and 28 July 2014)	50% by volume	Gravelly base (1 <sup>st</sup> surge)	Yes	5° -10°	0.4-0.7
		Bouldery deposit (rear surges)			0.3-0.5

Notes:

\*Experimental flume tests

#Field tests

**Table 3.** Key results and initial conditions involved in the staged mobility analysis

		<b>First intermediate barrier (Ch 360 m)</b>	<b>Second intermediate barrier (Ch 480 m)</b>	<b>Terminal barrier (Ch 525 m)</b>
<b>Design parameters</b>	<b>Debris approaching velocity</b>	12.0 m/s	8.3 m/s	7.3 m/s
	<b>Debris approaching thickness</b>	2.8 m	1.9 m	1.1 m
<b>Initial conditions for next stage analysis starts at downstream of the barrier</b>	$v_i$	10.4 m/s	6.1 m/s	---
	$x_i$	15 m	7 m	---
	$h_m$	3 m	3 m	---
	$x_d$	192 m	186 m	---

**Table 4.** Key parameters of material property

<b>Material property</b>	<b>Parameter</b>
Bulk density, $\rho$	1,900 kg/m <sup>3</sup>
Elastic modulus, $E$	10 MPa
Poisson's ratio, $\nu$	0.3
Internal friction angle, $\phi_{int}$	15°
Apparent cohesion, $c$	1 kPa

**Table 5.** Comparison between the results of the staged analysis and the LS-DYNA analysis

	<b>Ch 360 m</b>		<b>Ch 480 m</b>		<b>Terminal Barrier</b>	
	<b>Debris approaching velocity</b>	<b>Debris approaching thickness</b>	<b>Debris approaching velocity</b>	<b>Debris approaching thickness</b>	<b>Debris approaching velocity</b>	<b>Debris approaching thickness</b>
<b>Staged Analysis</b>	12.0 m/s	2.8 m	8.3 m/s	1.9 m	7.5 m/s	1.1 m
<b>LS-DYNA</b>	11.0 m/s	1.5 m	7.9 m/s	1.1 m	6.7 m/s	1.0 m

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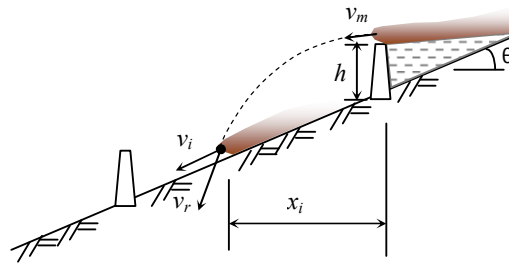
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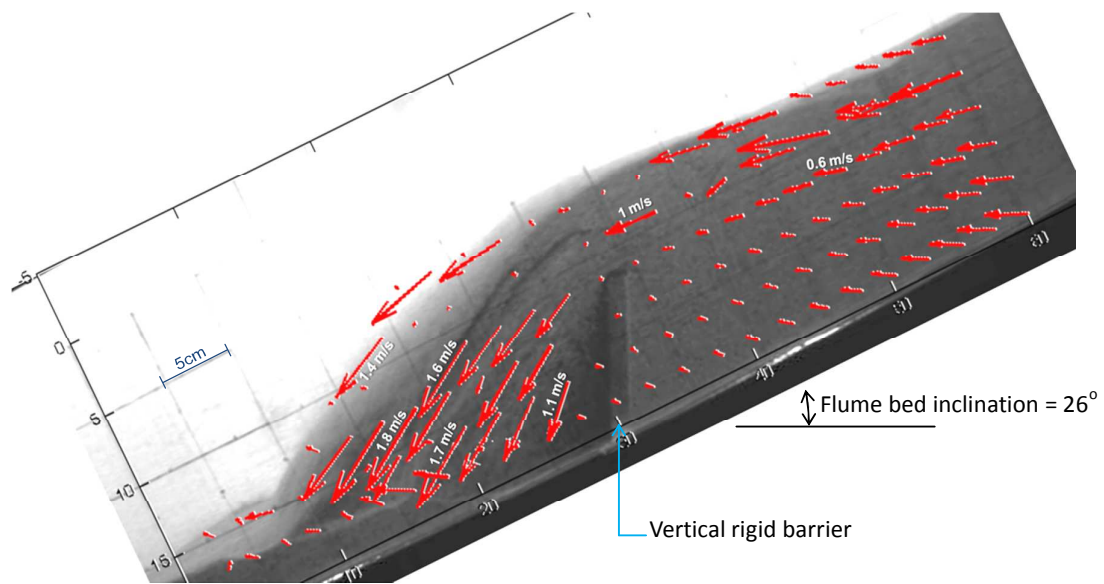
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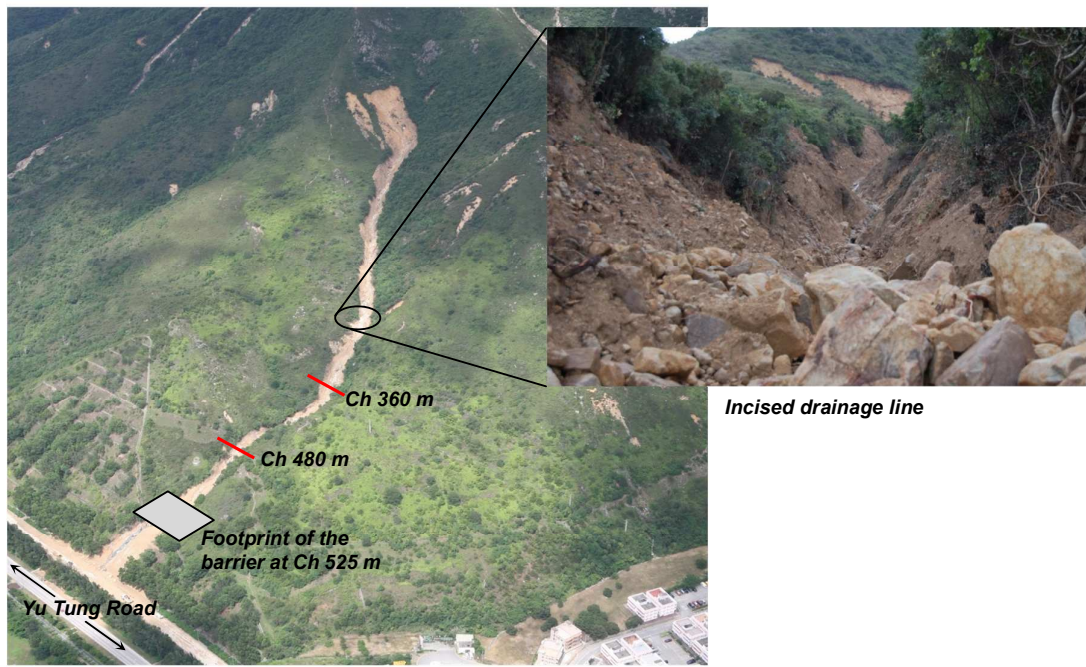


- $x_i$  = horizontal length of debris trajectory
- $v_m$  = debris launch velocity
- $v_r$  = debris velocity just before landing
- $v_i$  = debris velocity after landing, parallel to runout path
- $\theta$  = inclination of runout path
- $h$  = height of barrier

Fig. 1. Design parameters for assessing dynamic motion of landslide debris overflowing from barrier



**Fig. 2.** Debris overflows from crest of rigid barrier



**Fig. 3.** Catchment of the Yu Tung Road debris flow

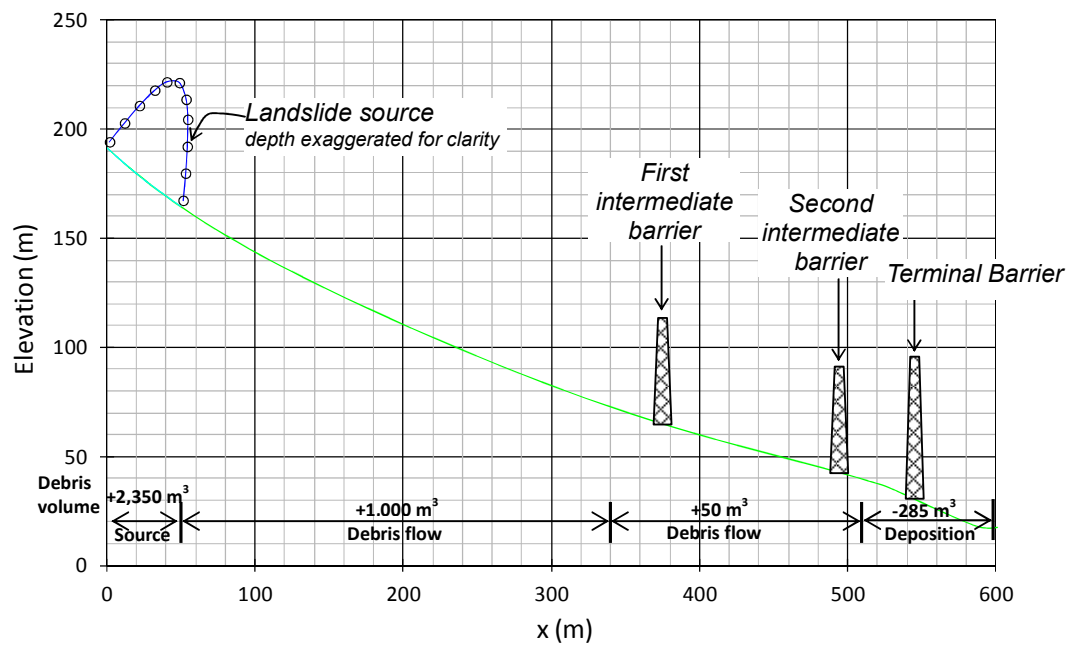


Fig. 4. Runout profile of the mobility analysis

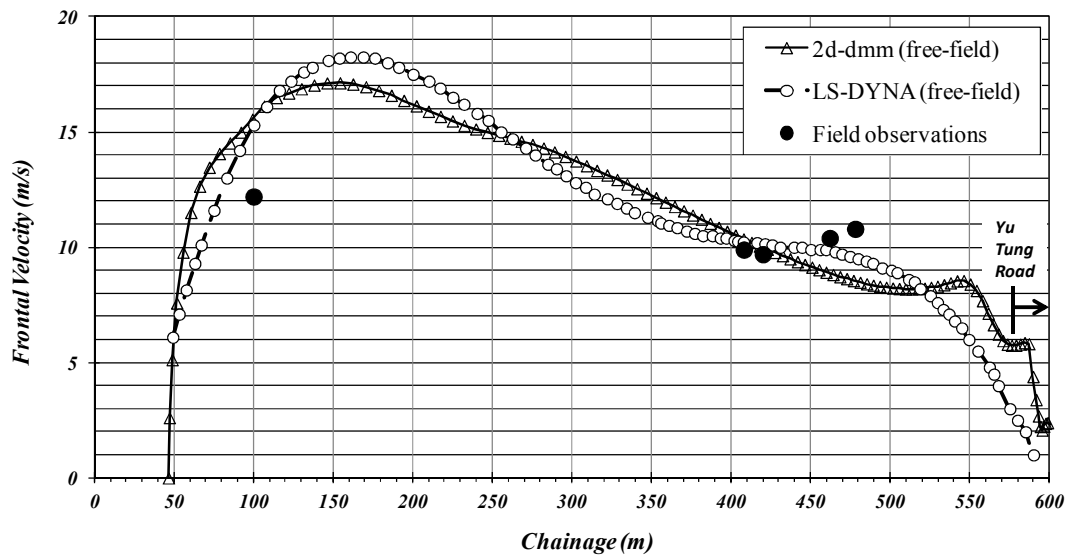
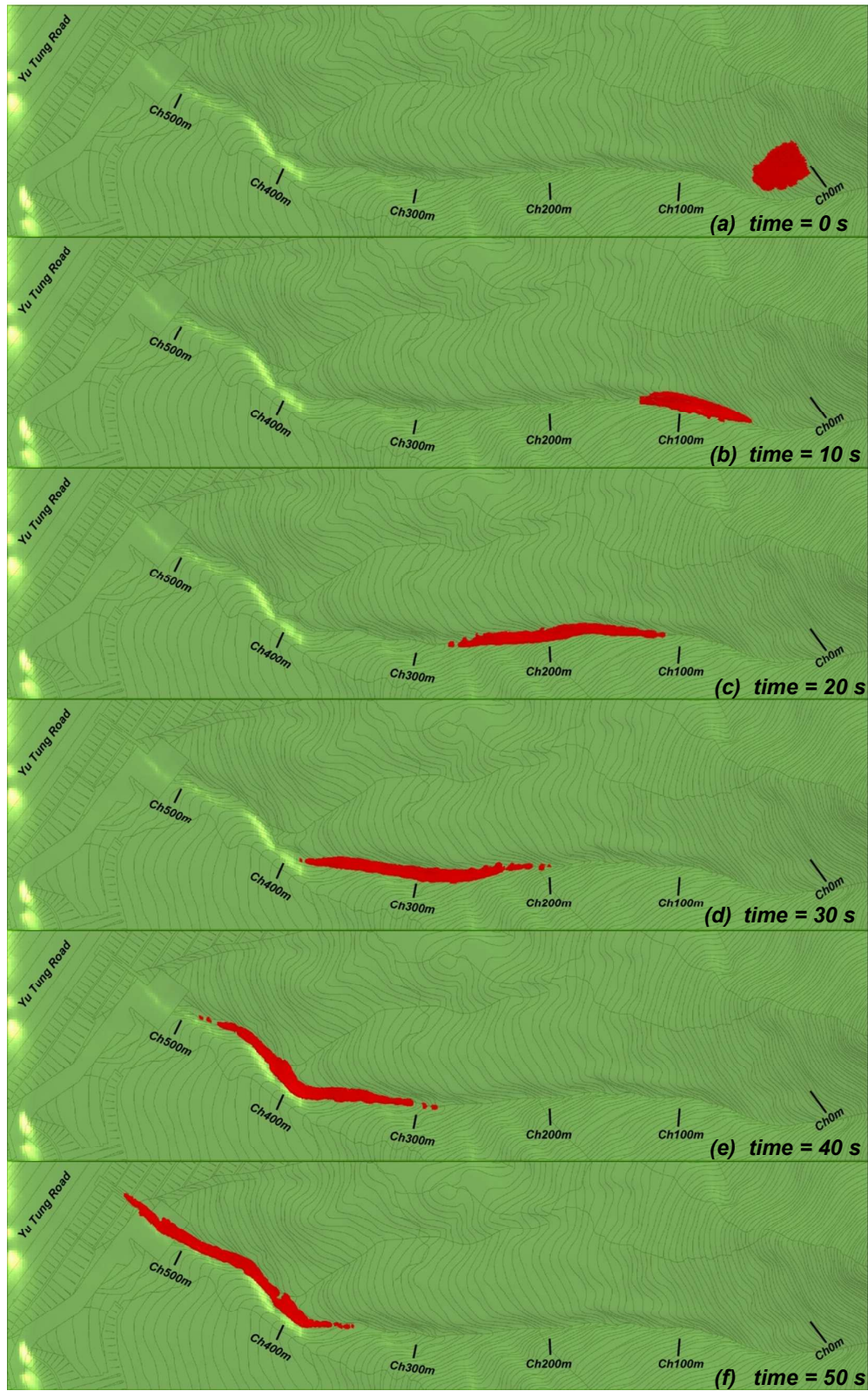


Fig. 5. Frontal debris flow velocity against chainage



**Fig. 6.** Simulation of Yu Tung Road debris flow using LS-DYNA analysis

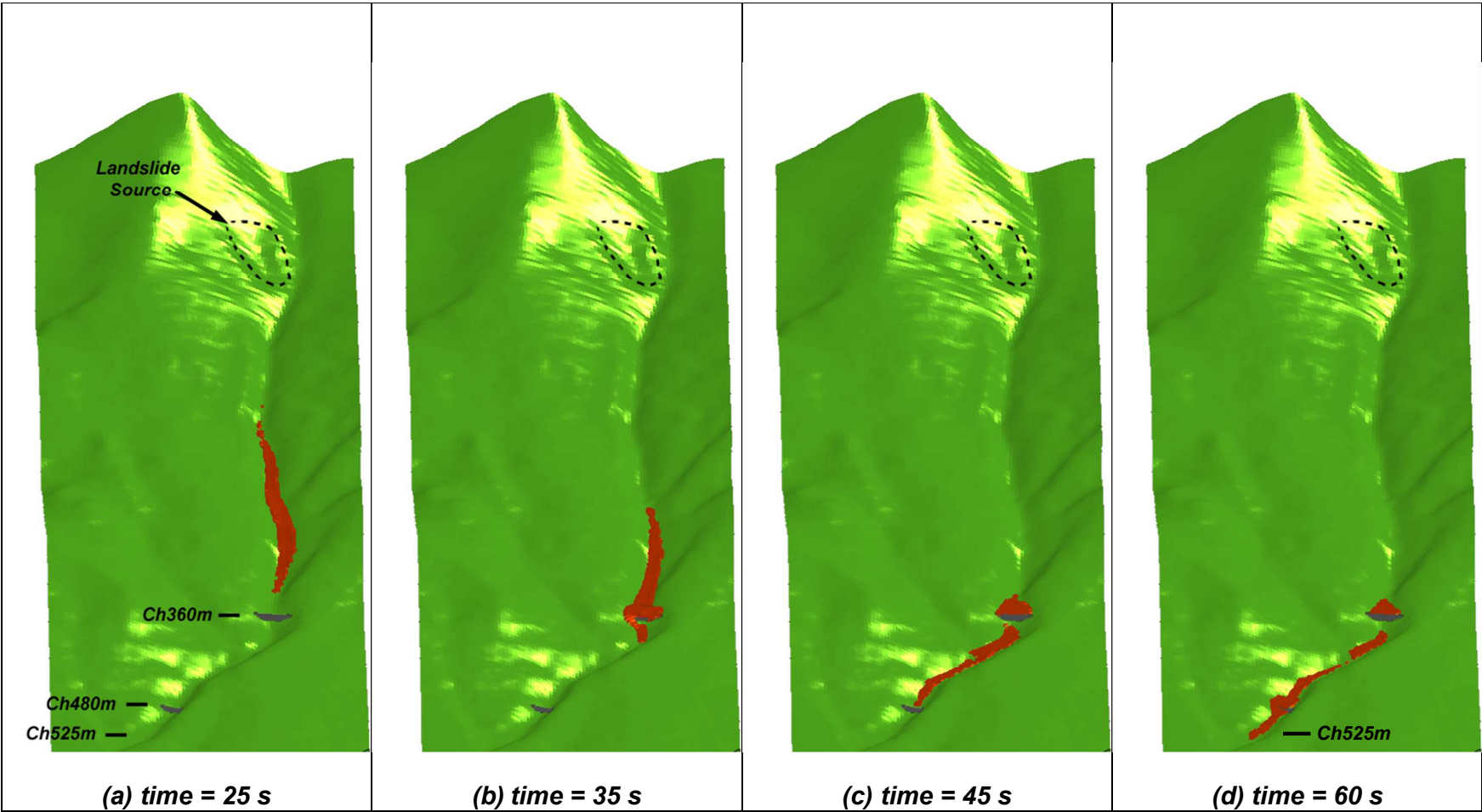
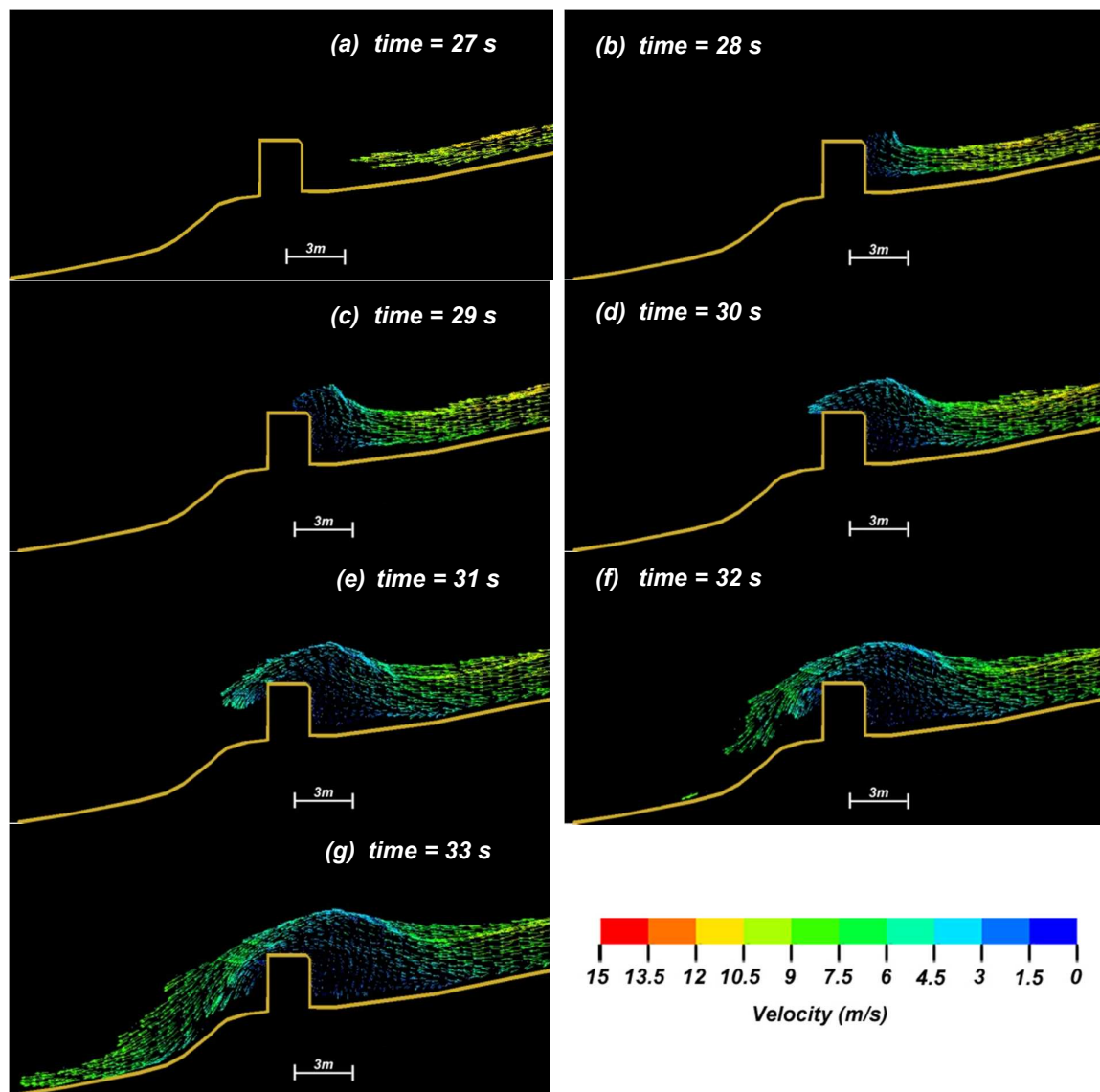


Fig. 7. Simulation of debris flow obstructed by multiple barriers



**Fig. 8.** Simulation of debris flow velocity vector plots (barrier at Ch 360 m)

## 1 Appendix A

2

### 3 A Flume Test of Landslide Debris Overflowing

#### 4 from Rigid Barrier

5

#### 6 Introduction

7 The test was carried out in a 5 m long flume with a channel base width of 0.2 m. Side  
8 walls are about 0.5 m in height, perpendicular to the channel bed. Dry Leighton Buzzard  
9 Fraction C sand is composed of fairly uniform silica grains with specific gravity of 2.65 g/cm<sup>3</sup>,  
10 was used in this series of flume tests. The particle size of the sand ranges between 300 µm and  
11 600 µm. The angle of repose of the sand is 33° and the friction angle between the sand and  
12 flume bed is 23°. The initial bulk density of the sand mass is about 1680 kg/m<sup>3</sup>. At the top end  
13 of the flume is a sand storage tank. Sand can be released into the flume by opening a flip gate  
14 that is attached to the tank. Details of the flume and the sand release mechanism are presented  
15 in Choi et al. (2014).

16 The vertical barrier model used in the flume test is 0.1 m high and made up of a 10 mm  
17 thick aluminum plate. It is firmly secured within the flume at midway of the channel. The  
18 scaling factor of the wall dimension is about 1/50 to typical prototype.

19 Several trials were carried out to establish an appropriate flume inclination. It was  
20 subsequently decided that the flume should be inclined at 26° based on the consideration of  
21 the Froude number of the sand flow. Froude number ( $F_r = v / (g h)^{0.5}$ , where  $v$  is debris  
22 velocity,  $g$  is gravitational acceleration and  $h$  is debris depth normal to the flume bed) is a  
23 dimensionless parameter usually adopted to characterise the inertia of debris flow. In design  
24 practice of Hong Kong, the value of  $F_r$  of debris flows in typical design scenarios for barrier  
25 design is about 3, given that design impact velocity is about 10 m/s and a flow depth of about

1 1 m (i.e.  $F_r = 10 / (10 \times 1)^{0.5} = 3.2$ ). When the inclination of the flume is  $26^\circ$ , the sand flow in  
2 the flume would attain a velocity of about 2.6 m/s with an approaching depth of around  
3 0.08 m at the location of the model barrier. This corresponds to a Froude number of  
4 2.9 ( $= 2.6 / (10 \times 0.08)^{0.5}$ ). A series of experiments with different source volumes of dry sands  
5 overflow the rigid barrier has been carried out. The range of R factors observed from the  
6 experiments has been reported.

## 7 **Experimental Results**

8 The flume test was recorded with the use of a high-speed camera which could capture  
9 100 images per second. Figure A1 shows the image records in sequence.

10 Fig. A1(a) shows the instant when the dry sand flow arrived at the barrier location. For  
11 discussion purposes, the time of this instant is denoted as  $t = 0.0$  s. After 0.1 second, the sand  
12 flow filled up the retention zone behind the barrier and splashing of the sand is also evident.  
13 At  $t = 0.25$  s, debris that was not trapped behind the barrier started the overtopping process  
14 and launched into a ballistic flight. Subsequently, debris overflowing from the crest of the  
15 barrier travelled along a projectile path and landed on the flume bed at a distance about 0.2 m  
16 downstream of the barrier (see Fig. A1(d)). This process continued for about 16 seconds. At  
17 the end of the test, sands piled up behind the barrier and the deposition angle was about  $33^\circ$ .

18 In this present study, the velocity of the sand flow has been determined using the  
19 'geoPIV' computer package developed by White et al. (2003). This package is developed  
20 based on close-range photogrammetry techniques capable of tracking movements of soil  
21 grains captured in high-resolution images. It produces displacement and velocity vectors of  
22 the soil grains. Typical results of the PIV analysis are shown in Fig. 2.

## 23 **Velocity Reduction at Landing**

24 Velocity reduction upon immediate landing at the end of the ballistic flight has been

1 studied. Table A1 summarises the velocity parallel to the flume before and after landing as  
2 well as the velocity ratio. The velocity ratio ranges from about 0.3 to 0.5.

### 3 **Projectile Length**

4 Eq. 1 is developed to calculate the length of projectile for debris overflowing from the  
5 crest of barrier. The velocity and trajectory length data presented in Fig. 1 are used to verify  
6 this equation. As shown in the figure, debris overflowing velocity at the barrier crest is about  
7 1.0 m/s. Using Equation 1, the estimated length of trajectory is 0.18 m. The trajectory length  
8 as observed in the test was 0.2 m. The difference of the trajectory length between the  
9 calculated value by eq. 1 and laboratory observation is within 10%, which is considered to be  
10 acceptable. However, the predicted result on reality may have larger discrepancy, since the  
11 debris materials and scale of barriers could be quite different to the laboratory test.

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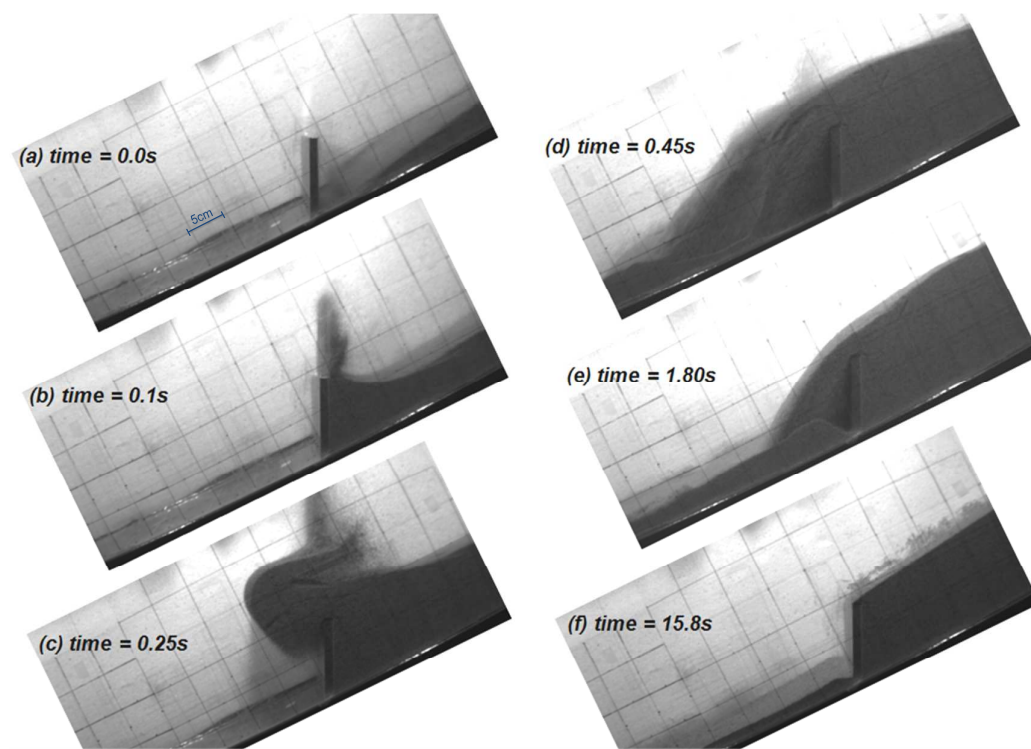
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**Table**

**Table A1.** Velocity data for calculating velocity reduction at landing

<b>Time (s)</b>	<b>Velocity Parallel to the Flume Just <u>Before</u> Landing (<math>V_b</math>) (m/s)</b>	<b>Velocity Parallel to the Flume Immediately <u>After</u> Landing (<math>V_a</math>) (m/s)</b>	<b><math>V_a/V_b</math></b>
0.46	1.3	0.6	0.46
0.51	1.4	0.6	0.43
0.61	1.6	0.7	0.44
1.11	1.6	0.4	0.25
1.31	1.3	0.4	0.31

Figure

**Fig. A1.** High-speed camera images (Choi & Ng 2013)

1 **Appendix B**

2

3 **Derivation of Equations (1) to (3)**

4

5 **Derivation of eq. (1) for calculation of  $x_i$** 

6 Fig. B1 shows notations of different parameters relevant to debris overflow from barrier.

7  $x$ -coordinate of the trajectory path of landslide debris:

8 (B1)  $x = v_m t$

9 where  $t$  is time after debris launches from the barrier crest and  $v_m$  is the maximum velocity of  
 10 debris which cannot be trapped by barrier.

11 (B2)  $y = h - \frac{1}{2} g t^2$

12 where  $g$  is gravitational acceleration.

13 Substitute eq. (B1) into (B2) to obtain the equation of the trajectory path of landslide  
 14 debris:

15 (B3)  $y = h - \frac{1}{2} g (x / v_m)^2$

16 Equation of the runout path:

17 (B4)  $y = -\tan\theta x$

18 Solve eq. (B3) and (B4) to obtain  $x_i$ ,

19 (B5)  $x_i = \frac{v_m^2}{g} \left[ \tan\theta + \sqrt{\tan^2\theta + \frac{2gh}{v_m^2}} \right]$

20 **Derivation of eqs. (2) and (3) for calculation of  $v_r$  and  $v_i$** 21  $v_r$  can be estimated based on energy conservation principle, i.e.

1 (B6)  $\frac{1}{2} m_r v_r^2 = KE_1 - KE_2 + m_r g (h + C_x x_i \tan \theta)$

2 where  $m_r$  = mass of debris overflow from barrier,  $v_r$  = velocity of remaining debris just before  
 3 landing,  $KE_1$  = total kinetic energy of debris before intercepted by barrier, and  $KE_2$  = kinetic  
 4 energy of debris retained by barrier.

5 The last term in eq. (B6) corresponds to potential energy gained in the ballistic flight.  $x_i$   
 6 is horizontal distance that landslide debris could travel, it is calculated using the maximum  
 7 velocity of debris overflowing from barrier (see eq. (B1)). Since ratio of rear velocity to  
 8 frontal velocity of overflowing debris varies, a correction factor  $C_x$  is proposed to establish an  
 9 average value of  $x_i$  relevant to the energy calculation. The value of  $C_x$  depends on the ratio of  
 10 the rear and frontal velocities of the overflowing debris, and can be calculated using eq. (B5)  
 11 based on a combination of selected barrier height, debris velocity and inclination of runout  
 12 profile with consideration of different velocity ratios. The leading portion of the debris flow  
 13 typically has the highest velocity and kinetic energy. Therefore, the minimum spacing  
 14 between barriers ( $x_i$ ) should be calculated using the debris frontal velocity as presented in this  
 15 study. However, the velocity of the rear portion of the overflow debris would be much slower.  
 16 The use of the highest debris velocity as the initial condition of the debris mobility analysis of  
 17 the next stage would result in grossly overestimation of the impact on the barrier downstream.  
 18 It is suggested not design the overflow kinetic energy too conservative to avoid over-sizing of  
 19 the barriers. Therefore, the attenuation of overflow debris mobility is considered. Fig. B2  
 20 shows a plot of  $C_x$  against velocity ratio. The data are generated based on combinations of a  
 21 range of debris velocity up to 15 m/s, barrier heights of 1 m to 5 m, and ruout path  
 22 inclinations of 20° to 60°. Values of  $C_x$  which envelop the upper limit of the data are  
 23 recommended for using in the stage analysis (see also Table 1).

24 Eq. (B6) can be simplified to the following form:

$$1 \quad (B7) \quad v_r = \sqrt{\frac{2[KE_r + m_r g(h + C_x x_i \tan \theta)]}{m_r}}$$

2 where  $KE_r = KE_1 - KE_2$  (i.e. the kinetic energy of the overflow debris which can be obtain  
3 from debris mobility analysis).

4  $v_r$  is velocity of remaining debris just before landing, it is in a direction tangential to the  
5 trajectory path. The velocity for inputting to the dynamic analysis of landslide debris at next  
6 stage (i.e. debris velocity after landing,  $v_i$ ) is parallel to the inclination of the runout profile  
7 which can be calculated as follows:

8 Noting that  $\beta$  denotes angle between  $v_r$  and debris runout path (see Fig. B3), and  $\beta + \theta$  is  
9 inclination of  $v_r$  to horizontal i.e.

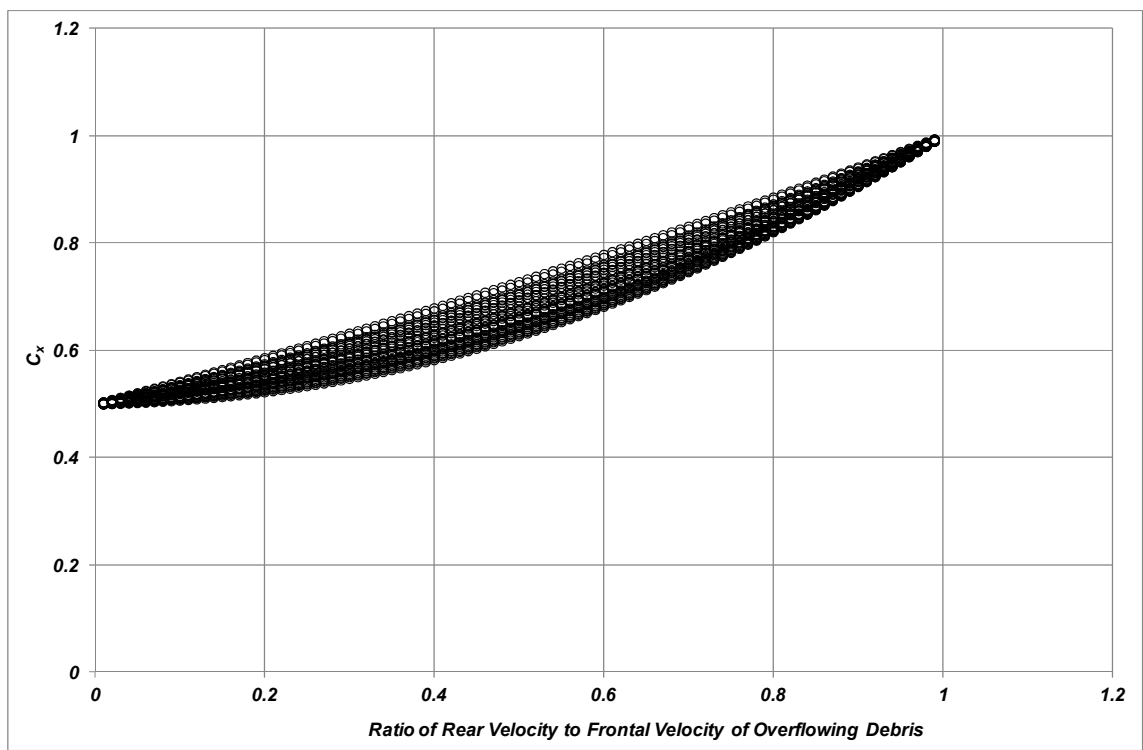
$$10 \quad (B8) \quad \beta + \theta = \tan^{-1} \sqrt{\frac{m_r g(h + C_x x_i \tan \theta)}{KE_r}} \quad \text{and}$$

$$11 \quad (B9) \quad v_i = v_r \cos \beta$$

12 Combining eqs. (B8) and (B9) and applying velocity reduction factor ( $R$ ) to account for  
13 the velocity reduction at landing, eq. (B10) is obtained:

$$14 \quad (B10) \quad v_i = Rv_r \cos \left[ \left[ \tan^{-1} \sqrt{\frac{m_r g(h + C_x x_i \tan \theta)}{KE_r}} \right] - \theta \right]$$





**Fig. B2.** Study of the value of  $C_x$